Abstract – Modern electronic toll collection (ETC) systems are currently moving towards a system design that is capable of fast and optimal payment handling for a single lane. Thus, the antenna of a roadside reader unit (RSU) needs to provide sufficient coverage over the vehicle lane during a payment cycle. In this paper, a left-hand circularly polarized (LHCP) 2×4 array antenna is proposed for European standard RSU readers at 5.8 GHz. The proposed array antenna consists of patch element antennas with parasitic elements to enhance gain and bandwidth. Sequential phase rotation feeding networks are applied to make the antenna low-profile. By using the optimized nut-shaped metasurface, the antenna can achieve higher gain due to concentrated radiation power in the boresight direction. The antenna has a wide impedance bandwidth of 2.34 GHz (37.73%), axis ratio bandwidth of 2.07 GHz (32.9%), high gain of 17 dBi, and sidelobe level (SLL) lower than -15 dB at 5.8 GHz. Especially, half-power beamwidths are 34° and 17° in horizontal and vertical planes, respectively, which covers sufficient space for a single lane while avoiding interference with other lanes. The performance of the proposed antenna is verified by measured results. It showed that the proposed antenna is a promising candidate for ETC applications.

Index Terms – circularly polarized antenna, FFETC, high gain, metasurface, RSU antenna, wideband antenna.
An FFETC system is set up as shown in Fig. 1. The RSU is mounted on the gate at the height of \( h_{RSU} \), and made with the vertical axis at an angle \( \beta \), \( \theta_v \) is the half-power beamwidth (HPBW) of the antenna in the vertical plane. An OBU is installed on a vehicle whose distance to the road surface is \( h_{OBU} \). To ensure a payment cycle takes place, the distance MN must be long enough (or \( \theta_v \) must be wide enough) when the vehicle is traveling in one payment cycle at the allowed speed of \( v \). There are two main loss factors influencing communication between RSU and OBU: the first one is free space loss \( L_{\text{space}} \) and the second is loss from car windows \( L_{\text{win}} \). \( L_{\text{space}} \) depends on the instantaneous distance between OBU and RSU \( r \), while \( L_{\text{win}} \) depends on the material of car windows. For accurate communications, the received OBU power \( P_r \) must be greater than -43 dBm [3]. Based on the Friis transmission equation, \( P_r \) is represented by equation (1). Parameters \( P_t \), \( L_{\text{space}} \), \( L_{\text{win}} \) and \( G_r \) are factors outside RSU. So the only solution to make sure the received signal is large enough is to increase \( G_r \).

Thus, our design criteria that need to be achieved for the RSU antenna are high gain, vertical HPBW \( \theta_v \) wide enough, horizontal HPBW \( \theta_h \leq 20^\circ \) and SLL \( \leq -15 \) dB. According to European standards, \( h_{RSU} \leq 5.5 \) m [3] and assuming \( h_{OBU} = 1.5 \) m. Therefore, the relationship between vehicle speed \( v \) and \( \theta_v \) is given in Table 1.

\[
P_r(t) = P_t + G_r(\theta) - L_{\text{space}}(r) - L_{\text{win}} + G_r, \quad (1)
\]

The paper [5] also proposed an antenna with a radiation pattern with a vertical beam of 30° and a horizontal beam of 15°. However, the antenna SLL is high, about -12.5 dB. Recently, there has been some research on antenna design for RSU. In [6], a 10×10 antenna array is proposed with a high gain of up to 14.3 dB. The antenna used a Woodward and Lawson feeding structure to achieve a low SLL of -28.2 dB. But, it has a symmetrical radiation pattern of about 37° in both vertical and horizontal planes, a fairly wide beam, and can cause interference to adjacent lanes. In addition, in the operating frequency range, the axis ratio value of 2.7 dB represents a low circular polarization purity. The 12-element antenna array in [4] is more optimally designed for the EN12253 standard. It has a wide bandwidth of 1.13 GHz with 15 MHz high polarization isolation, HPBW of 23°, gain of 14.7 dBi at 5.8 GHz, and peak gain of 17 dBi at 5.9 GHz. In particular, its SLL is low, about -17 dB, thanks to the use of a Chebyshev feeding network. But, its beamwidths have not been optimized based on the vehicle’s speed to cover a distance for a payment circle. Similarly, this is a weak point of the antennas in [7,11].

In [12], a 2×4 antenna array was introduced with high gain, vertical (V), and horizontal (H) beamwidths of 33.2° and 17.1°, respectively. However, the SLL is quite high, around -13 dB, and its performance has not been verified by measurement. Therefore, this study will continue to improve it to meet the requirements for an RSU antenna as mentioned above. The double circle unit cell is analyzed and optimized to get characteristics of the metasurface with both negative permittivity (\( \varepsilon < 0 \)) and negative permeability (\( \mu < 0 \)) to enhance the performance of the proposed antenna by reducing SLL and improving AR bandwidth. Compact size is another advantage of the proposed antenna by utilizing a sequential phase rotation feeding network. FR-4 is used for fabrication to obtain a low-cost antenna. Finally, the performance of the proposed antenna is verified by measured results.

The paper is organized into three parts. Part II presents the antenna design process, which will analyze the antenna components including the unit cell, element antenna, 2×2 array antenna, and 2×4 array antenna with the reflector. Some conclusions and discussions are given in Part III.

### II. ANTENNA DESIGN

#### A. Unit cell

LHCP patch antennas are widely used for ETC applications. However, they are generally low gain, so improving gains for these antennas is a challenge for researchers. Several solutions have been proposed, for example, using parasitic sheets [13,14], deploying stacked patches [15,16] and implementing metamaterials [17,18,27,31]. The use of the parasitic patch in [15] can improve gain very well, and it can also extend the circular polarization bandwidth for antennas deployed on the same plane. However, the disadvantage of this structure is that the antenna size may be larger. In [15], deploying two patch layers was proposed. Simulation and measured results show that the gain of the antenna is significantly improved from 5

![Fig. 1. The communication between OBU and RSU.](image)

<table>
<thead>
<tr>
<th>( v ) (km/h)</th>
<th>60</th>
<th>100</th>
<th>130</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \theta_v ) (degree)</td>
<td>22</td>
<td>34.6</td>
<td>39</td>
</tr>
</tbody>
</table>

Table 1: The relationship between the beamwidth \( \theta_v \) and the velocity of vehicle \( v \)
dBi to 10.5 dBi. This method does not increase the size of the antenna, but it does make the antenna thicker and more difficult to fabricate due to misalignment between layers. The gain of the antenna in [17] was enhanced by 2 dBi thanks to applying a metasurface placed on the main radiation patch. The antennas in [17-22] also implemented a metasurface, but the special feature of these designs is that the metasurface is capable of re-polarization from LP (linear polarization) to CP. Thereby, we can see that using a metasurface is not only to reconfigure the polarization but also to increase gain.

In this study a new unit cell and a metasurface are proposed to improve gain, and AR bandwidth, and to create a low-profile antenna. The structure of the proposed unit cell is shown in Fig. 2(a). It is nut-shaped, made up of two circles of radius $r = 2.1$ mm with a total length of $k = 6$ mm. Each unit cell is printed on an FR-4 substrate with the permittivity $\varepsilon = 4.3$ and thickness of 1.6 mm. Compared to the unit cell in [12] [25], four corners of the unit cell are cut apart as shown in dashed boxes. The unit cell is rotated 45$^\circ$ compared with the Y-axis direction. The proposed unit cell is simulated by CST Studio Software [26] with the boundary condition as shown in Fig. 2(b), where Port 1 is located 4 mm far from the surface of the unit cell, and Port 2 is located at a long distance away because this side of the metasurface is open so it is chosen as one wavelength.

The proposed unit cell is truncated and has a smaller size compared to the non-truncated unit cell (N-T unit cell) in [25], as a result, the mutual coupling between element antennas in the proposed array is reduced. Then, the SLL of the proposed array antenna is enhanced. The performance of the proposed unit cell and metasurface when they are integrated into the element antenna will be presented in the next subsections.

**B. Element antenna**

The element antenna is designed with the metasurface structure proposed in subsection A. The structure of the element antenna is shown in Fig. 3. It has two layers: the lower layer is a reference antenna that was introduced in [12] [25], and the upper layer is the proposed metasurface, which is a $4 \times 4$ unit cell array. The distance between unit cells is $d$. The distance between the two layers is $h$. The size of the ground plane is $W \times W$.

![Fig. 3. Structure of element antenna using the proposed metasurface (a = 10.5, c = 7.5, d = 5, e = 1, fe = 0.7, g1 = 0.5, g2 = 0.7, g3 = 0.3, h = 4, hs = 1.6, p1 = 5, p2 = 7, p3 = 8, p4 = 9, p5 = 9.5, p6 = 11.5, s = 1, W = 33) Unit: mm.](image)

To analyze the role of antenna components, three antenna versions (AN1, AN2, and PROP) in Fig. 4 are simulated and compared with each other. AN1 is a square patch antenna with a diagonal slot in the middle. AN2 consists of AN1 and six parasitic patches, and the final model PROP contains AN2 and the proposed metasurface. PROP is the proposed element antenna. The simulation results of these three antennas are shown in Fig. 5.

Figure 5 reveals that AN1 resonates at 5.7 GHz and 6.2 GHz with $S_11$ values of -7 dB and -8 dB. The lowest axis ratio value is 15 dB at 5.8 GHz while the peak gain is 5.7 dBi at 6.2 GHz. After adding the six isosceles trapezoidal parasitic patches, the AN2 resonates better at 6.2 GHz, while an additional resonance appears at the higher frequency of 7.25 GHz. The AR curve appears with three sharp peaks where there are small AR values of 12 dB, 16.5 dB, and 10.5 dB at 5.8 GHz, 7.2 GHz, and 7.4 GHz. The gain value at the low-frequency band seems to be constant, however, due to
the resonance at 7.2 GHz, the gain at this frequency reaches 6 dBi. It can be seen that AN1 and AN2 have weak resonance, low gain, and no circularly polarized radiation. After adding the proposed metasurface, the impedance matching is greatly improved, and PROP achieves an impedance bandwidth (Imp. BW) of 1.2 GHz (20.34%). At the same time, the elliptical polarization of AN2 is also converted to circular polarization when using the proposed metasurface with an axial ratio bandwidth (AR BW) of 1 GHz (16.39%). In particular, the gain of PROP is significantly improved in the entire working frequency range with a very stable high value in the range of 7±8 dBi (the gain curve is flat as shown in Fig. 5 (c)). Thus, using the proposed metasurface significantly improves the performance of circularly polarized antennas.

As mentioned in subsection A, the T unit cell reduces mutual coupling between element antennas. This is proved in Fig. 6 which shows the electric field (E-field) of the element antenna in two cases with the T unit cell and the N-T unit cell. It can be seen that the E-field in the case of the T unit cell is more concentrated in the boresight direction than that in the case of the N-T unit cell. Similarly, $S_{21}$ of two-element antennas is also simulated in these two cases as shown in Fig. 7. At 5.8 GHz, $S_{21}$ is reduced to 3.6 dB. Thus, the SLL of the proposed array is improved by using this T unit cell.

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**Fig. 5.** Simulated results of three antenna versions in (a) $S_{11}$, (b) AR, and (c) gain.
enhancing the AR bandwidth and making the proposed antenna compact. The distance between the element antennas is \( d_e = 37 \) mm and the total length is \( w_g = 80 \) mm. Some fabrication photos of this antenna are shown in Fig. 9. Simulation and measured results in \( S_{11} \), gain, and AR are given in Fig. 10. The measured result in \( S_{11} \) has a good agreement with the simulation ones. Figure 10(b) provides information about the gain, where the maximum gain is 14.3 dBi at 5.8 GHz. The simulated AR bandwidth is 2 GHz (32.5\%). The SLL of the 2×2 array antenna in the case of the T unit cell is lower than that in the case of the N-T unit cell as shown in Fig. 11. The measured radiation patterns agree well with the simulation ones. The HPBW are approximately 34° and the maximum SLL is -15.3 dB. Thus, the performance of the 2×2 array antenna is verified by the measured results with a high gain and wide bandwidth. But, its HPBW are symmetrical, which has not satisfied for requirements of ETC antennas in terms of beamwidths as mentioned above. As a result, the 2×2 array antenna continues to be developed into a 2×4 array antenna presented in subsection D.

C. The proposed 2×2 array antenna

The 2×2 antenna array is designed as shown in Fig. 8. The four-element antennas are fed by the sequential phase rotation feeding network which was introduced in [25]. This feeding network contributes to increasing the AR bandwidth and making the proposed antenna compact. The distance between the element antennas is \( d_e = 37 \) mm and the total length is \( w_g = 80 \) mm. Some fabrication photos of this antenna are shown in Fig. 9. Simulation and measured results in \( S_{11} \), gain, and AR are given in Fig. 10. The measured result in \( S_{11} \) has a good agreement with the simulation ones. Figure 10(b) provides information about the gain, where the maximum gain is 14.3 dBi at 5.8 GHz. The simulated AR bandwidth is 2 GHz (32.5\%). The SLL of the 2×2 array antenna in the case of the T unit cell is lower than that in the case of the N-T unit cell as shown in Fig. 11. The measured radiation patterns agree well with the simulation ones. The HPBW are approximately 34° and the maximum SLL is -15.3 dB. Thus, the performance of the 2×2 array antenna is verified by the measured results with a high gain and wide bandwidth. But, its HPBW are symmetrical, which has not satisfied for requirements of ETC antennas in terms of beamwidths as mentioned above. As a result, the 2×2 array antenna continues to be developed into a 2×4 array antenna presented in subsection D.

D. The proposed 2×4 array antenna

The 2×4 antenna array is proposed in Fig. 12. It consists of three layers: the top layer is metasurface, the middle layer is the 2×4 patch antenna array, and the bottom layer is a T-shaped feeding network. The overall size of the proposed antenna is \( W_t \times L_t \). The distance between two 2×2 arrays is \( d_f \) and the distance between the bottom layer and the middle layer is \( h_a \). The T-shaped feeding network has an input of the 50 Ω line, A \( \lambda/4 \) segment with a characteristic impedance of 35 Ω is used to match impedances for two 50 Ω outputs, which are
Fig. 10. Simulation and measured results of the 2×2 antenna arrays: (a) $S_{11}$, (b) gain, and (c) AR.

Fig. 11. Simulation and measured radiation patterns of the 2 × 2 array antenna in two cases: N-T unit cell and T unit cell in two planes (a) YOZ plane, (b) XOZ plane.

Fig. 12. The proposed 2 × 4 antenna array ($W_t = 160$, $L_t = 80$, $h_a = 7$, $L_w = 17.5$, $W_w = 75$, $d_f = 53$. Unit: mm).
connected to two $2 \times 2$ array antennas by coaxial cables. The size of the feeding network is $W_u \times L_u$. Fabrication photos of the $2 \times 4$ array antenna are shown in Fig. 13.

The simulation and measured results of the $2 \times 4$ array are shown in Figs. 14 and 15, which show the impedance bandwidth of 2.34 GHz (37.56%), and the 3-dB AR bandwidth of 1.865 GHz (30.6%), and the peak gain of 16.6 dBi at 5.8 GHz. The vertical beamwidth ($\phi = 0^\circ$) and the horizontal beamwidth ($\phi = 90^\circ$) are $35^\circ$ and $18.6^\circ$, respectively. The proposed $2 \times 4$ array antenna meets almost all requirements for an ETC antenna, but the SLL of this antenna is -13.3 dB, so is quite high. Therefore, a reflector is added to compress the SLL.

![Fabrication photos of the proposed 2×4 array antenna.](image)

Fig. 13. Fabrication photos of the proposed 2×4 array antenna.

Figure 16 shows the $2 \times 4$ array antenna with the reflector. The size of the reflector is $w_r \times L_r \times h_r$. Two metal plates are placed on either side of the antenna, where the SLLs need to be reduced. The height of these two plates $h_r$ is the main parameter affecting the SLL reduction. The larger $h_r$ is, the smaller the sidelobe is. In addition, the wider reflector also helps to reduce the sidelobe.

In the plane $\phi = 0^\circ$, the SLL is significantly reduced from -13.3 dB to -15.7 dB while the SLL is -17.2 dB in the plane $\phi = 90^\circ$ as given in Fig. 15. The vertical beamwidth ($\phi = 0^\circ$) and the horizontal beamwidth ($\phi = 90^\circ$) are $34^\circ$ and $17^\circ$, respectively. The measured radiation patterns are also shown in Fig. 15. There is little difference between the simulation and measured results, which is caused by measurement and fabrication errors.

The effect of this reflector is more clearly shown by simulation results in Fig. 14. Figure 14(a) shows that the impedance bandwidth is almost unchanged while 3-dB AR bandwidth is extended to 2 GHz (32.9%) in Fig. 14(b), and the gain is improved to 17 dBi at 5.8 GHz. In
III. DISCUSSION AND CONCLUSION

Table 2 provides a comparison of the proposed 2×4 array antenna with some recently reported ETC antennas. It can be seen that the proposed antenna has wider impedance bandwidth and AR bandwidth than almost all the other antennas [4,10], except for the antenna [25]. The high gain of 17 dBi is another merit of the proposed antenna compared to the other antennas. Also, unlike the proposed antenna, most of the other antennas do not have optimized beamwidths in order to cover the vehicle’s mileage in a payment cycle. Moreover, the size of the proposed antenna is more compact than the antennas in [5,6]. In summary, a novel nut-shaped unit cell was proposed to improve the proposed array antenna in terms of impedance and AR bandwidths, SLL, and gain in this study. The problem of interference and vehicle speed was considered in designing the proposed array antennas. The vehicle can pass the ETC with a speed of more than 100 Km/h. The SLL of the proposed antenna was optimized to be smaller than -15 dB by adding a reflector. By applying the sequential phase rotation feeding network, the proposed array antenna is low-profile with enhanced AR bandwidth. Moreover, the proposed array antenna was verified by measured results. It is found that the proposed 2×4 array antenna has met most of the requirements for ETC antennas, and therefore, it is a suitable candidate for RSUs in modern ETC systems.

Table 2: A performance comparison between the proposed 2×4 antenna with other studies

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Imp. BW (%)</th>
<th>AR BW (%)</th>
<th>Gain (dBi)</th>
<th>V-H HPBW (degree)</th>
<th>SLL (dB)</th>
<th>Size (mm³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[4]</td>
<td>34.48</td>
<td>19.4</td>
<td>14.7</td>
<td>23-23</td>
<td>-17</td>
<td>172×172×0.8</td>
</tr>
<tr>
<td>[5]</td>
<td>7.86 Nm</td>
<td>16.6</td>
<td>35.4-15.7</td>
<td>-12.5</td>
<td>200×180×0.8</td>
<td></td>
</tr>
<tr>
<td>[10]</td>
<td>30.58</td>
<td>25.5</td>
<td>23.3</td>
<td>-17</td>
<td>192×172×0.8</td>
<td></td>
</tr>
<tr>
<td>[12]</td>
<td>2.58</td>
<td>Not CP</td>
<td>30-40</td>
<td>-10</td>
<td>103×103×13</td>
<td></td>
</tr>
<tr>
<td>[13]</td>
<td>24.58</td>
<td>14.9</td>
<td>33-33</td>
<td>-26</td>
<td>500×400×0.8</td>
<td></td>
</tr>
<tr>
<td>[14]</td>
<td>14.7</td>
<td>19.4</td>
<td>18-18</td>
<td>-16</td>
<td>Nm</td>
<td></td>
</tr>
<tr>
<td>[15]</td>
<td>37.73</td>
<td>18.6</td>
<td>20-20</td>
<td>-15</td>
<td>Nm</td>
<td></td>
</tr>
<tr>
<td>[16]</td>
<td>33.73</td>
<td>17.2</td>
<td>33-17</td>
<td>-13</td>
<td>180×106×30</td>
<td></td>
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<tr>
<td>[17]</td>
<td>37.73</td>
<td>32.9</td>
<td>17-17</td>
<td>-15.7</td>
<td>Nm</td>
<td></td>
</tr>
<tr>
<td>[18]</td>
<td>31.75</td>
<td>35.52</td>
<td>17-17</td>
<td>-13</td>
<td>152×76×6.4</td>
<td></td>
</tr>
</tbody>
</table>

Not mentioned: Nm.

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