

Higher-order Method of Moments Analysis of Waveguide with Irregular Cross-sections

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Abstract – Antennas fed by waveguides with irregular cross-sections are efficiently simulated through the hybridization of the mode-matching (MM) method and the higher-order method of moments (HOMoM). To obtain the waveguide modes required in the MM method, a 2-D finite element method (FEM) is utilized and combined with the hybrid MM/HOMoM method, which enables the proposed method to model irregular waveports. The accuracy and efficiency of the proposed method are demonstrated by simulating log-periodic antennas (LPAs) and an asymmetric single-ridge slot waveguide antenna.

Index Terms – Eigenvalues, finite element method (FEM), higher-order method of moments (HOMoM), irregular cross-sections, mode-matching (MM), waveports.

I. INTRODUCTION

Waveguides are widely used in antennas due to their high power capabilities and low loss properties. With the development of microwave technology, the structures of microwave devices and waveport aperture surfaces tend to become increasingly complicated. Therefore, the accurate and efficient simulation of microwave devices with waveports has attracted much attention.

For the analysis of waveguide problems, the method of moments (MoM) is widely considered numerically accurate [1]. On the other hand, due to the high efficiency of the mode-matching (MM) method, it has been widely used to design waveguide components. As a result, the MoM and MM method are hybridized to analyze waveguide coupling and radiation problems [2]. In 2000, the MM/MoM hybrid method was applied to analyze the metallic N -port waveguide structures, where the RWG basis functions were used for modeling, and the electric field integral equation (EFIE) was adopted for construction of the impedance matrix [3]. The Poggio-Miller-Chang-Harrington-Wu-

Tsai (PMCHWT) formulation was utilized for analyzing dielectric loaded waveguides [4]. Later, the higher-order vector basis functions modeled with curvilinear triangles were used to improve the simulation efficiency of non-rotationally symmetric structures [5]. In 2015, the MM method was introduced to the higher-order method of moments (HOMoM) for constructing perfectly matching terminators for waveports. The higher-order basis functions modeled with quadrilaterals further reduced the number of unknowns [6]. Recently, a set of coupled integral formulations were derived to handle the loading problem of the metal-dielectric composite structures, and the orders of the basis functions were adaptively adjusted, yielding accurate and effective results [7].

However, the majority of previous investigations focused on regular waveguides, such as rectangular and circular ones. The previous method is no longer applicable when the cross-section of the waveport becomes irregular due to fabrication or architectural requirements, e.g. the coaxial center conductor may be eccentric or non-cylindrical [8]. Therefore, modeling of waveguides with irregular cross-sections based on the hybrid MM/MoM method is worth discussing.

In this paper, the MM/HOMoM method and FEM are hybridized to solve the coupling and radiation problems fed by waveports with irregular cross-sections. The use of higher-order basis function defined on the bilinear quadrilaterals can greatly improve efficiency while maintaining numerical accuracy, and the adoption of FEM extends the flexibility.

II. THEORY AND FORMULATION

A. MM/HOMoM hybrid method

Let us consider an arbitrarily shaped cavity containing several objects connected by N waveports, as depicted in Fig. 1. The object surfaces are classified into three categories: metallic, dielectric, and composite metal-dielectric surfaces [9].

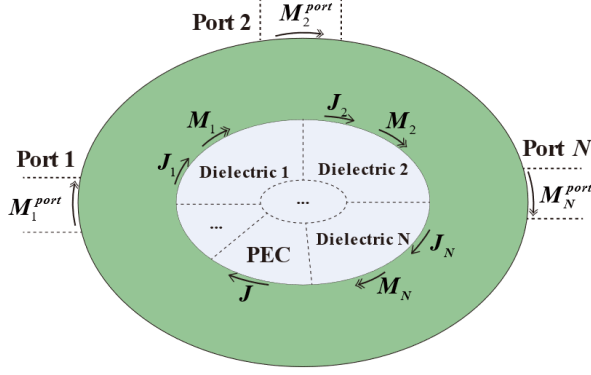


Fig. 1. Multiport cavity structure containing composite objects connected by N waveports.

The unknown current densities are expanded by a set of linearly independent basis functions f_n and g_n as:

$$\begin{cases} \mathbf{J}^l = \sum_{n=1}^{N_J} \alpha_n f_n & \text{metal/dielectric surfaces} \\ \mathbf{M}^l = \sum_{n=1}^{N_M} \beta_n f_n & \text{dielectric surfaces} \\ \mathbf{M}^{port} = \sum_{n=1}^{N_p} \eta_0 v_n g_n & \text{waveguide apertures} \end{cases}, \quad (1)$$

where η_0 denotes the wave impedance of free space, and N_J , N_M , and N_p represent the number of unknowns in the scattering body and waveguide apertures, respectively. α_n , β_n , and v_n represent the unknown coefficients. f_n is the higher-order basis functions defined on the quadrilaterals, and the definition is given in [10]. g_n denotes the waveguide basis functions defined on the apertures of waveguides, which is expanded using the eigenvectors of different waveport modes.

Since the analysis of conventional scattering problems has been discussed in detail previously [9, 11], this paper discusses only the matrix associated with the waveguide basis functions. According to the equivalence principle, the surface integral equation of the electromagnetic field could be established. The integral equations can be written as follows by applying boundary conditions to the waveguide apertures, the metallic surfaces, and the dielectric surfaces, respectively:

$$\begin{cases} \hat{\mathbf{n}}_i \times \mathbf{E}_i = \hat{\mathbf{n}}_i \times \sum_{j=1}^{\infty} [\eta_0 L(\mathbf{J}_j) - K(\mathbf{M}_j)] = -\zeta \mathbf{M}_i \\ \hat{\mathbf{n}}_i \times \mathbf{H}_i = \mathbf{J}_i \end{cases}, \quad (2)$$

where the real number ζ equals 1.0 when modeling the dielectric surfaces or waveguide apertures and 0 otherwise. The integral operators L and K are the same as [6]. $\mathbf{J}_i$ and $\mathbf{M}_i$ denote the electric and magnetic currents defined on the i -th surface of the elements, which are discretized with the higher-order basis functions defined on bilinear quadrilateral elements, and $\hat{\mathbf{n}}_i$ ($i = 1, 2, 3, \dots$) is the unit normal vector on the i -th surface.

Adopting the MM technique, the electromagnetic field outside the waveport can be written as [6]:

$$\begin{cases} \mathbf{E}^{port} = -\sum_{i=1}^{\infty} \mathbf{e}_i \int_A (\hat{\mathbf{n}} \times \mathbf{e}_i) \cdot \mathbf{M} ds \\ \mathbf{H}^{port} = \frac{2\hat{\mathbf{n}} \times \mathbf{e}_j}{\eta_j} + \sum_{i=1}^{\infty} \frac{\hat{\mathbf{n}} \times \mathbf{e}_i}{\eta_i} \int_A (\hat{\mathbf{n}} \times \mathbf{e}_i) \cdot \mathbf{M} ds \end{cases}, \quad (3)$$

where $\hat{\mathbf{n}}$ is the outer normal vector for each waveport, $\mathbf{e}_i$ is the normalized eigenvector of the waveport, $\mathbf{e}_j$ is the excitation mode, and η_i is the wave impedance of the i -th mode of the waveport.

The whole structure is divided into the scattering body (represented by s) and waveports (denoted by p). Using Galerkin's method to test the above equation with the basis functions of the scatterer body and the basis functions of the waveports, the integral equations of matrix form can be written as:

$$\begin{bmatrix} \mathbf{Z}^{ss} & \mathbf{Z}^{sp} \\ \mathbf{Z}^{ps} & \mathbf{Z}^{pp} \end{bmatrix} \cdot \begin{bmatrix} \mathbf{I}^s \\ \mathbf{I}^p \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{V}^p \end{bmatrix}, \quad (4)$$

where $\mathbf{I}^s$ is the unknown coefficients vector associated with the scattering body, and $\mathbf{I}^p$ is the unknown coefficients vector associated with the waveport aperture. $\mathbf{V}^p$ represents the right-hand vector excited by the waveport. $\mathbf{Z}^{ab}$ represents the impedance matrix resulting from the interaction of structures a and b. Letters a and b can be replaced by s (the scattering body) or p (the waveport).

The matrix elements in (4) can be expressed as:

$$\mathbf{Z}_{mn}^{sp} = \left\langle f_i, \left[\frac{\zeta}{2} (\hat{\mathbf{n}} \times \mathbf{M}_j^{port}) + K(\mathbf{M}_j^{port}) \right] \right\rangle, \quad (5)$$

$$\mathbf{Z}_{mn}^{ps} = \langle \mathbf{M}_i^{port}, \hat{\mathbf{n}} \times \mathbf{J}_j \rangle, \quad (6)$$

$$\mathbf{Z}_{mn}^{pp} = \left\langle \mathbf{M}_i^{port}, \frac{\hat{\mathbf{n}} \times \mathbf{e}_j}{\eta_j} \int_A (\hat{\mathbf{n}} \times \mathbf{e}_j) \cdot \mathbf{M}_j^{port} ds \right\rangle, \quad (7)$$

$$\mathbf{V}_m^p = \left\langle \mathbf{M}_i^{port}, \frac{2\hat{\mathbf{n}} \times \mathbf{e}_j}{\eta_j} \right\rangle = -\frac{2\eta_0}{\eta_j} \int_A \mathbf{e}_i \cdot \mathbf{e}_j ds, \quad (8)$$

where m and n denote the row and column numbers of the matrix elements, $\langle \cdot \rangle$ denotes inner product operator, and the definition of ζ is the same as in (2).

B. Analysis of waveguide eigenvalue problem

A variety of methods are used to analyze the waveguide cross-sectional field distribution, including MoM, FDTD, and FEM. Among all these methods, 2-D FEM is the most generally applicable and versatile [12].

Here, to facilitate integrated modeling, the 2-D vector FEM is adopted to analyze the waveguide eigenvalue problems. The tangential electric field $\mathbf{E}_t$ and longitudinal electric field $\mathbf{E}_z$ on the element are defined as follows, where N and $\mathbf{W}$ represent the scalar and vector basis functions, respectively [13, 14]:

$$\mathbf{E}_z = N \mathbf{e}_z = [L_1 L_2 L_3] \mathbf{e}_z, \quad (9)$$

$$\mathbf{E}_t = [\mathbf{W}] \mathbf{e}_t = [\mathbf{W}_{12} \mathbf{W}_{23} \mathbf{W}_{31}] \mathbf{e}_t, \quad (10)$$

$$\mathbf{W}_{ij} = l_{ij} (L_i \nabla_t L_j - L_j \nabla_t L_i), \quad (11)$$

where L_i ($i = 1, 2, 3$) are area coordinates of the element, l_{ij} is length of edge that starts from node i to node j , ∇_t is the gradient operator, and $\mathbf{e}_z$ and $\mathbf{e}_t$ represent the coefficients to be solved for the transverse and direction vectors, respectively.

In order to obtain the eigenvector of the waveguide aperture, the generalized eigenmatrix equation is derived from the Helmholtz equation [12]:

$$\begin{bmatrix} \mathbf{A} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{e}_t \\ \mathbf{e}_z \end{bmatrix} = -\beta^2 \begin{bmatrix} \mathbf{H} & \mathbf{G} \\ \mathbf{G}^T & \mathbf{B} \end{bmatrix} \begin{bmatrix} \mathbf{e}_t \\ \mathbf{e}_z \end{bmatrix}, \quad (12)$$

$$\mathbf{A} = \int_{\Omega} \left[\frac{1}{\mu_r} (\nabla_t \times \mathbf{W})^T (\nabla_t \times \mathbf{W}) - k_0^2 \epsilon_r \mathbf{W}^T \mathbf{W} \right] d\Omega, \quad (13)$$

$$\mathbf{H} = \int_{\Omega} \left[\frac{1}{\mu_r} \mathbf{W}^T \mathbf{W} \right] d\Omega, \quad (14)$$

$$\mathbf{B} = \int_{\Omega} \left[\frac{1}{\mu_r} (\nabla_t N)^T \cdot (\nabla_t N) - k_0^2 \epsilon_r N^T N \right] d\Omega, \quad (15)$$

$$\mathbf{G} = \int_{\Omega} \left[\frac{1}{\mu_r} \mathbf{W}^T (\nabla_t N) \right] d\Omega, \quad (16)$$

where ϵ_r and μ_r represent relative permeability and permittivity of the medium corresponding with the waveguide, β is the propagation constant, k_0 is the wave number of free space, Ω is the cross-section of the waveguide apertures, and N and $\mathbf{W}$ represent the scalar and vector basis functions [10, 11].

According to (18), the orthonormal modal field distributions on quadrilaterals are obtained through the operation, $\mathbf{e}_i$ is the i -th mode normalized eigenvector of the waveguide, $\mathbf{e}_j$ is the excitation mode, and δ_{ij} is Kronecker delta:

$$\int_S \mathbf{e}_i \cdot \mathbf{e}_j dS = \delta_{ij} = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases}. \quad (17)$$

Finally, by using nested one-dimensional Gaussian sampling on the quadrilaterals, we obtain the modal field distribution at the Gaussian sampling points of the waveguide aperture. Applying the results to matrix elements, the 2-D FEM is associated with the MM/HOMoM hybrid method, making the method more flexible.

III. NUMERICAL EXAMPLE

Simulation examples are given in this section to validate the accuracy and computational efficiency of the proposed method, and all simulations employ double-precision numerical accuracy. The computational platform used in these examples is a workstation with two Intel Xeon(R) Gold 5118 CPUs and 512 GB RAM.

A. Asymmetrical single-ridged slotted waveguide antenna

Due to the advantages of easy fabrication and low loss, slotted waveguide antennas have been widely used. Among these, the asymmetrical slotted waveguide antenna is not only small in size, but also has good low sidelobe characteristics [15, 16]. Firstly, a slotted antenna fed by an asymmetrical single-ridged waveguide is analyzed to demonstrate the flexibility of the proposed method. As shown in Fig. 2 and Table 1, the dimensions of the waveport aperture and antenna model are given

here, and all slots are the same size. The other side of the antenna waveguide port is connected to a matched terminator.

The S11 is computed from 8.5 to 9.5 GHz (11 frequency points). The model is discretized into 7774 quadrilateral elements and expanded into 15418 unknowns using the proposed method. When using triangles for modeling in FEKO, the antenna is discretized into 17187 meshes and 26949 RWG-MoM unknowns when using a $\lambda/12$ mesh size.

The S parameter and computational statistics comparison are depicted in Fig. 3 and Table 2. The proposed method's efficiency is much greater than the RWG-MoM

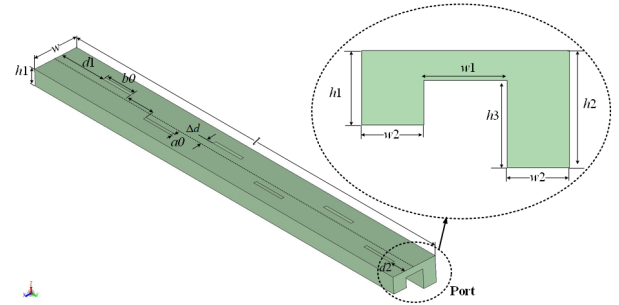


Fig. 2. 3-D model of the slotted waveguide antenna and dimensions of the single-ridged waveport cross-section.

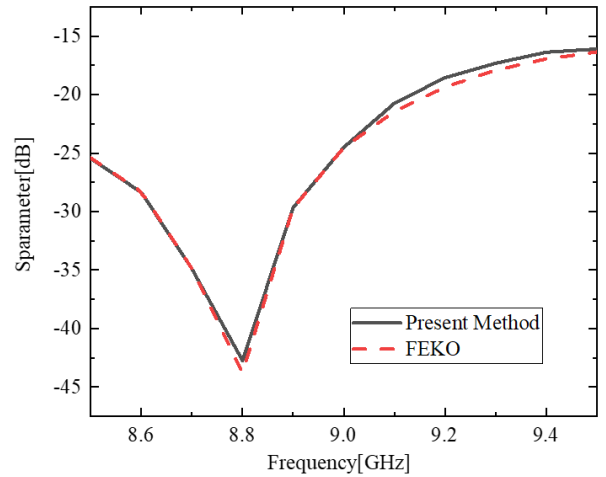


Fig. 3. Comparison of S parameters of the slotted waveguide antenna.

Table 1: Geometrical parameters of the slotted waveguide antenna. All dimensions are in millimeters (mm)

w	$w1$	$w2$	l	$d1$	$d2$
13.72	5.48	4.12	131.9	15.7	4.55
$a0$	$b0$	$h1$	$h2$	$h3$	Δd
0.9	10.15	4.93	7.76	5.79	4.41

Table 2: Computational statistics of the slotted waveguide antenna when 24 cores are used

Method	Present Method	FEKO ($\lambda/12$)
Number of Unknowns	15418	26949
Memory [GB]	3.5	10.8
Time [s]	1071	4554

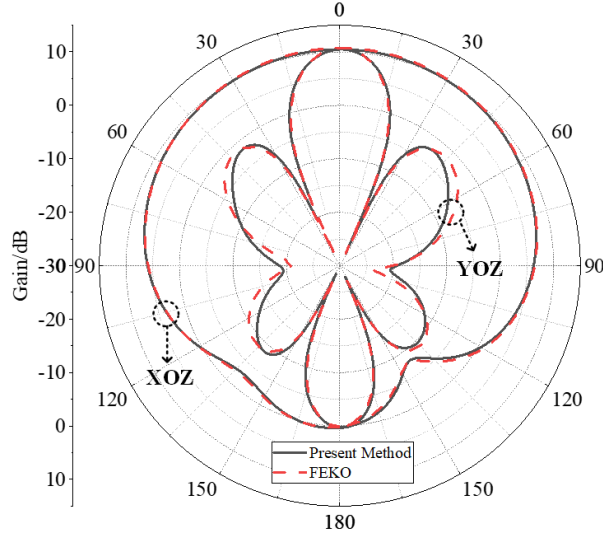


Fig. 4. Radiation pattern of the single-ridged waveguide antenna.

in FEKO. Moreover, the radiation pattern of the slotted antenna is computed. The operating frequency is set to 8.8 GHz, which is the resonant frequency of the waveguide. As seen in the Fig. 4, the gain of the xoz plane and the yoz plane agree well.

B. Log-periodic antennas

A log-periodic antenna (LPA) is then analyzed to illustrate the accuracy and efficiency of the proposed method. The 3-D model of the antenna is shown in Fig. 5, and the dimensions of the antenna are listed in Table 3. The antenna consists of two orthogonal linear polarization elements and a perfect electric conductor (PEC) reflector plane. The antenna has the following parameters: number of elements $N = 18$, scaling factor $\tau = 0.77$, and spacing factor $\sigma = 0.125$. The lengths (l_n), widths (w_n), and spacings (r_n) of the antenna decrease logarithmically as defined by the geometric ratio τ and the spacing factor σ [17, 18]. The top two identical waveguide ports are arranged orthogonally as feeders:

$$\tau = l_{n+1}/l_n = w_{n+1}/w_n, \quad (18)$$

$$\sigma = r_n/4l_n. \quad (19)$$

The operating frequency of the simulation is carried out in 1.0 GHz, and the model is discretized into 6140

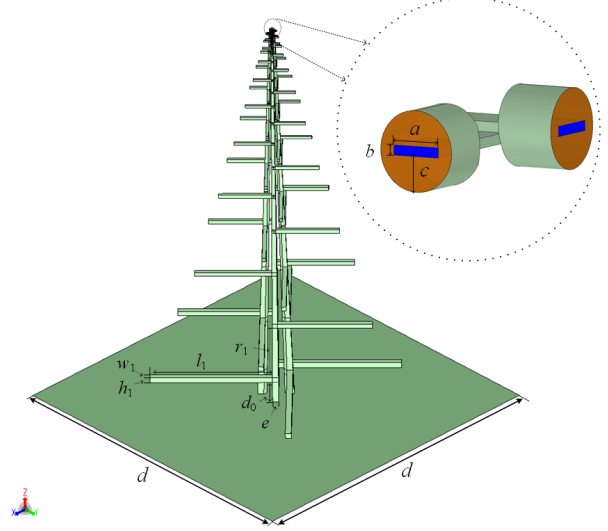


Fig. 5. 3-D model of the log-periodic antenna.

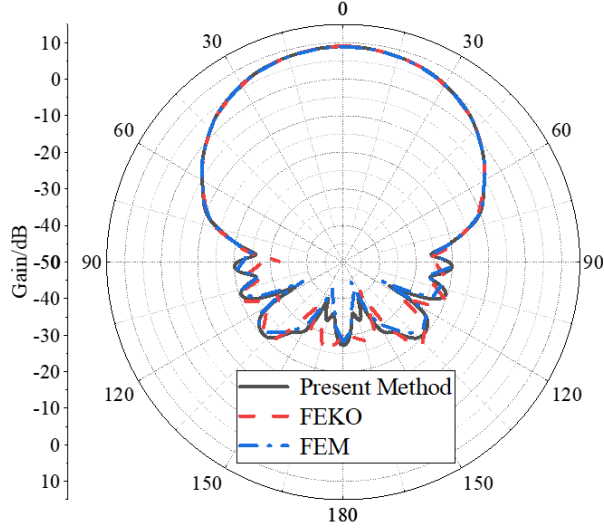
Table 3: Geometrical parameters of the log-periodic antenna. All dimensions are in millimeters (mm)

a	b	c	d	e
2.5	0.5	3.6	1000.0	18.0
l_1	h_1	w_1	r_1	d_0
350.0	17.0	16.8	178.0	66.0

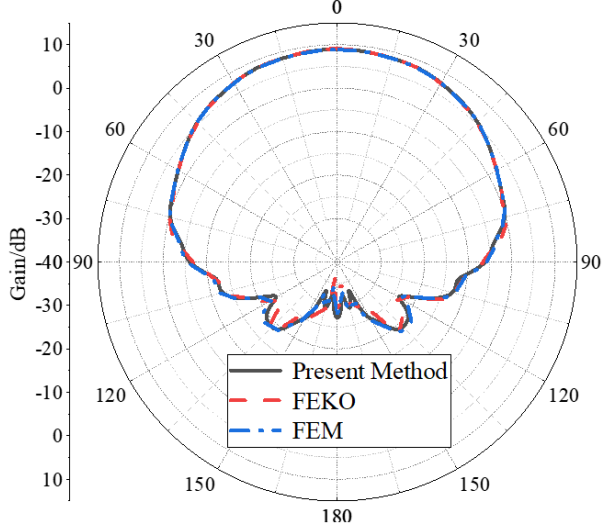
bilinear quadrilaterals and 12290 unknowns when using the proposed method. The model was discretized into 13926 triangular patches in FEKO, and the mesh size was $\lambda/12$, yielding 20869 RWG-MoM unknowns. For comparison, the result of FEM is also given to verify the correctness of the proposed method, in which the residual is set to 0.005.

Figure 6 shows a comparison of the radiation pattern results. It can be observed that the presented method in this paper has great agreement with FEKO and FEM within the main lobe, with a small difference below -20 dB. The computational statistics are summarized in Table 4. Due to the use of higher-order basis functions, the number of unknowns can be effectively reduced in the proposed method compared to the RWG-MoM without losing numerical accuracy. Furthermore, the proposed method has advantages in memory and solution time.

To further illustrate the effectiveness of the current approach, we present an example of an LPA array. This array consists of the five antenna elements mentioned above and a PEC reflector with a side length of 2000 mm. Figure 7 and Table 5 show the 3-D model of the array and the distribution in the xoy plane. Figure 8 gives the comparison of the radiation pattern between the present



(a)



(b)

Fig. 6. Radiation patterns of the log-periodic antenna:(a) xoz plane (b) yoz plane.

Table 4: Computational statistics of the log-periodic antenna when eight cores are used

Method	Present Method	FEKO ($\lambda/12$)
Number of Unknowns	12290	20869
Memory [GB]	2.3	6.5
Time [s]	119	437

method and FEKO. Additionally, as indicated in Table 6, the proposed method outperforms RWG-MoM in terms of memory usage and time required.

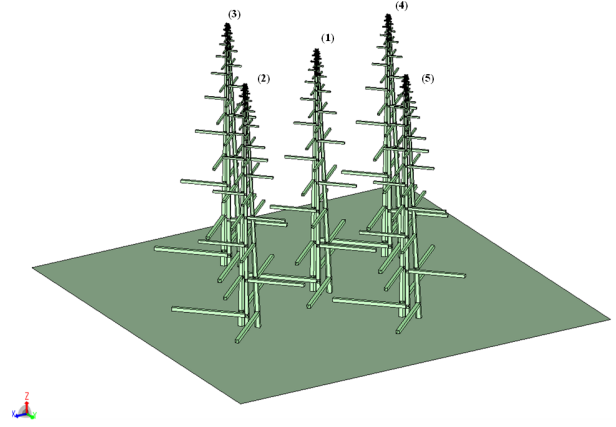


Fig. 7. 3-D model of the log-periodic antenna array.

Table 5: Distribution of the log-periodic antenna in the xoy plane. All dimensions are in millimeters (mm)

Index	Coordinates
(1)	(0, 0)
(2)	(500, 200)
(3)	(200, -500)
(4)	(-500, -200)
(5)	(-200, 500)

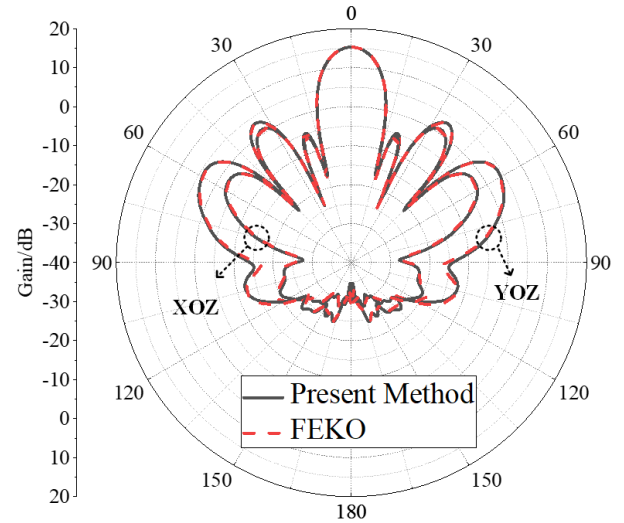


Fig. 8. Radiation pattern of the log-periodic antenna array.

Table 6: Computational statistics of the log-periodic antenna array when 24 cores are used

Method	Present Method	FEKO ($\lambda/12$)
Number of Unknowns	58332	102799
Memory [GB]	50.7	157.5
Time [s]	1619	14025

IV. CONCLUSION

The MM/HOMoM method and FEM are hybridized to analyze waveguide problems with irregular cross-sections. In order to facilitate integrated modeling, 2-D FEM is used to solve the eigenvalue problem of the waveguide. In addition, higher-order basis functions are used to reduce the unknowns effectively. Results show that the proposed method has the advantage of high efficiency and high numerical accuracy.

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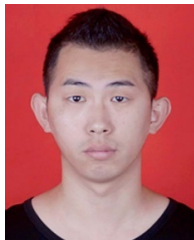
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