Impact Evaluation of an External Point Source to a Generalized Model of the Human Neck

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Abstract – A methodical approach for assessing the effects of an external point source to a non-spherical model of the human neck is presented in this paper. The neck model consists of multilayered spheres to represent the skin, fat, muscle tissues, thyroid, and esophagus. The novel geometry enables the formulation of dyadic Green’s functions to accurately calculate the electric fields, considering the suitable surface boundary conditions and the superposition principle. Numerical outcomes for a Hertz dipole (i.e., a wireless network antenna) at the frequency of 2.4 GHz certify the benefits of the technique and elaborately describe the responsiveness of the neck/thyroid to the selected source.

Index Terms – biomedical engineering, computational electromagnetics, Green’s function methods, wireless body area networks.

I. INTRODUCTION

The rapid evolution of healthcare wireless body area networks (WBANs) reflects the escalating need for real-time smart infrastructures to reliably monitor key gauges of the human body \cite{1, 2}. To this aim, an impressive variety of such systems has been developed in terms of specialized antennas \cite{3, 4} and advanced biomedical applications \cite{6, 7}. On the other hand, the assessment of electromagnetic radiation effects of several WBANs upon the human body and particularly on the thyroid has lately become a critical problem \cite{8, 9}. Existing studies concerning the radiofrequency spectrum focus mainly on thermal analysis \cite{10, 11}. However, there is an ever-increasing demand for simplified, precise, and economical models of the human neck to further explore the thyroid sensitivity to electromagnetic radiation.

This paper presents a systematic technique for the rigorous calculation of electromagnetic fields involving body area networks near the human neck. The proposed model represents abstractly the neck tissues as spherical layers and structures, permitting the parametric study of the thyroid. Concerning the mathematical formulation and the numerical results, the rapid and accurate derivation of the latter is enabled with the introduction of a new set of dyadic Green’s functions (dGFs). In this framework, we define the geometry of the model representing each part of the neck with a spherical body. Then, the electric field is determined using the proposed dGf-based technique. Finally, the results, so derived, are compared and validated through numerical outcomes obtained from a well-known computational package.

II. GEOMETRY OF THE NECK MODEL

The featured model, presented in Fig. 1, consists of the host sphere that has two spherical layers for the representation of the skin ($S_1$) and the fat ($S_2$), while a third cocentric inclusion depicts the muscle tissue ($S_3$). Also, the non-overlapping spherical eccentric inclusions for the right thyroid lobe ($S_4$), the left thyroid lobe ($S_5$), the trachea ($S_6$), the esophagus ($S_7$) and the other neck tissues ($S_8$) render the model non-spherical since the model lacks spherical symmetry. Each inclusion has an outer radius $a_i$ and a thickness $w_i$, for $i = 1, 2, \ldots, 8$, with the cocentric ones centered at origin $O$ and the eccentric ones at $O_j$, defined by vectors $d_{ij}$, for $j = 4, 5, \ldots, 8$. Note that all parts are occupied by a lossy dielectric medium characterized by a complex relative permittivity.
and a wavenumber $k_i = \omega \sqrt{\mu_0 \varepsilon_i}$, for $i = 1, 2, \ldots, 8$ and $\omega$ the angular frequency. Lastly, in our analysis, the free-space wavenumber is $k_0 = \sqrt{\mu_0 \varepsilon_0}$, regarding a typical $e^{-j\omega t}$ time dependence and the coordinate system $(O, r, \theta, \varphi)$ or $(O_i, r_i, \theta_i, \varphi_i)$, for $j = 4, 5, \ldots, 8$, defined at the origin $O$ or $O_j$, respectively.

## III. MATHEMATICAL FORMULATION

Let us assume that $\overline{G}_e^{(0)}$ is the free-space electric-field dGf which provides the electric field of an external point source $s$. In this case, the free-space electric-field dGf, $\overline{G}_e^{(0)}$, manifests as the solution of the dyadic Helmholtz equation $\nabla \times \nabla \times \overline{G}_e^{(0)} - k_0^2 \overline{G}_e^{(0)} = \mathbb{I}_d(r - r')$, where $\mathbb{I}_d$ stands for the unit dyad. By implementing the Ohm-Rayleigh method, discussed in [12], we can derive

$$\overline{G}_e^{(0)} = -\frac{1}{k_0^2} \mathbb{I}_d \delta(r - r') + jk_0 \sum_{mn, \alpha} c_{mn} F_{M,mn}^{(1)} (k_0 r) F_{A,mn}^{(3)} (k_0 r') , \quad (1)$$

where $\mathbb{I}_d$ are the corresponding unit vectors, $m = -n, -n + 1, \ldots, -1, 1, \ldots, n$ for $n = 1, 2, \ldots$ and $c_{mn} = (-1)^m (2n + 1)/n(n + 1) = c_{-m,n}$. It is stressed that in [1], according to the theoretical formulation of Green’s functions, $\alpha$ indicates the respective vector spherical harmonic $M$ or $N$. Therefore, for $\alpha = M, N$, it holds that

$$F_{M,mn}^{(1)} (k_0 r) = M_{mn}^{(1)} (k_0 r) = z_{mn}^{(1)} (k_0 r) \left( jm \frac{P_m^{(1)}(\cos \theta)}{\sin \varphi} - \frac{dP_m^{(1)}(\cos \theta)}{d\varphi} \right) e^{-jmr}, \quad (2)$$

$$F_{N,mn}^{(1)} (k_0 r) = N_{mn}^{(1)} (k_0 r) = \frac{1}{k} \nabla \times M_{mn}^{(1)} (k_0 r), \quad (3)$$

with $z_{mn}^{(1)} (k_0 r)$ being a spherical Bessel function of the first kind (when $t = 1$) or a Hankel function (when $t = 3$) and $P_m^{(1)}(\cos \theta)$ a Legendre function of the first kind [13] [14]. Observe that (1) holds solely for $r \leq r'$, otherwise the $t = 1, 3$ superscripts of $F$ must be reversed.

Regarding the proposed neck model, the desired dGf exhibits a bilocal spatial dependence, as the position vector of its various parts and the source are $r$ and $r'$. Moreover, the latter are likely to not belong to the same coordinate system and/or may not end at the same surface. Consequently, and in terms of [15], we denote as $Q_l$ ($l = 1, 2, \ldots, 8$) the location of the field point of interest, considering that it lies in the region limited by two surfaces, namely $S_{in}$ and $S_{out}$. Therefore, the electric dGf at $Q_l$ is acquired through $\overline{G}_e^{(l)} (r, r') = \overline{G}_e^{(l)}_{in} + \overline{G}_e^{(l)}_{out} + \overline{G}_e^{(l)}_{es}$, with $\overline{G}_e^{(l)}_{in}$ and $\overline{G}_e^{(l)}_{out}$ the respective electric dGfs at the $S_{in}$ and $S_{out}$ of the region where $Q_l$ is located. As a result, the electric-field intensity at $Q_l$ is derived as

$$E^{(l)} (r) = j \omega \mu_0 \iiint_V \overline{G}_e^{(l)} (r, r') \cdot J^{(l)} (r') dV , \quad (4)$$

for $V$ the volume confined between surfaces $S_{in}$ and $S_{out}$ and $J^{(l)} (r')$ the electric current density of the external source at $r'$. In this context, the necessary dGfs at every point of interest, confined between surfaces $S_l$ and $S_{l+1}$ (for $l = 1, 2, \ldots, 8$), as well as those in the free space, are

$$\overline{G}_e^{(0)} = \overline{G}_e^{(0)}_{es} + \overline{G}_e^{(0)}_{in} + \overline{G}_e^{(0)}_{out} , \quad (5)$$

$$\overline{G}_e^{(1)} = \overline{G}_e^{(1)}_{es} + \overline{G}_e^{(1)}_{in} + \overline{G}_e^{(1)}_{out} , \quad (6)$$

$$\overline{G}_e^{(2)} = \overline{G}_e^{(2)}_{es} + \overline{G}_e^{(2)}_{in} + \overline{G}_e^{(2)}_{out} , \quad (7)$$

$$\overline{G}_e^{(3)} = \overline{G}_e^{(3)}_{es} + \overline{G}_e^{(3)}_{in} + \overline{G}_e^{(3)}_{out} , \quad (8)$$

$$\overline{G}_e^{(4)} = \overline{G}_e^{(4)}_{es} + \overline{G}_e^{(4)}_{in} + \overline{G}_e^{(4)}_{out} , \quad (9)$$

$$\overline{G}_e^{(5)} = \overline{G}_e^{(5)}_{es} + \overline{G}_e^{(5)}_{in} + \overline{G}_e^{(5)}_{out} , \quad (10)$$

$$\overline{G}_e^{(6)} = \overline{G}_e^{(6)}_{es} + \overline{G}_e^{(6)}_{in} + \overline{G}_e^{(6)}_{out} , \quad (11)$$

$$\overline{G}_e^{(7)} = \overline{G}_e^{(7)}_{es} + \overline{G}_e^{(7)}_{in} + \overline{G}_e^{(7)}_{out} , \quad (12)$$

$$\overline{G}_e^{(8)} = \overline{G}_e^{(8)}_{es} + \overline{G}_e^{(8)}_{in} + \overline{G}_e^{(8)}_{out} , \quad (13)$$

Using the free-space dyad, the above system becomes

$$\overline{G}_e^{(0)} = \overline{G}_e^{(0)}_{es} + j \frac{k_0}{4\pi} \sum_{nm, \alpha} \left[ F_{A,mn}^{(3)} (k_0 r) A_{A,mn}^{(0)} (r') \right] , \quad (14)$$

$$\overline{G}_e^{(1)} = j \frac{k_1}{4\pi} \sum_{nm, \alpha} \left[ F_{A,mn}^{(3)} (k_1 r) C_{A,mn}^{(1)} (r') \right] , \quad (15)$$

$$\overline{G}_e^{(2)} = j \frac{k_2}{4\pi} \sum_{nm, \alpha} \left[ F_{A,mn}^{(3)} (k_2 r) C_{A,mn}^{(2)} (r') \right] , \quad (16)$$

$$\overline{G}_e^{(3)} = j \frac{k_3}{4\pi} \sum_{nm, \alpha} \left[ F_{A,mn}^{(3)} (k_3 r) C_{A,mn}^{(3)} (r') \right] . \quad (17)$$
n the EFI magnitude at can be several times larger (the sense of a wireless network antenna) with a parallel field. In particular, for the incident field, the value of terms, relative permittivities and hence the abruptly varying spher-
tric media properties of its various parts, at the frequency at the 

\[
\begin{align*}
G_e^{(4)} &= \frac{k_4}{4\pi} \sum_{n,m} F^{(1)}_{\alpha,\alpha,\alpha} (k_4 r_4) C^{(4)}_{\alpha,\alpha,\alpha} (r') , \\
G_e^{(5)} &= \frac{k_5}{4\pi} \sum_{n,m} F^{(1)}_{\alpha,\alpha,\alpha} (k_5 r_5) C^{(5)}_{\alpha,\alpha,\alpha} (r') , \\
G_e^{(6)} &= \frac{k_6}{4\pi} \sum_{n,m} F^{(1)}_{\alpha,\alpha,\alpha} (k_6 r_6) C^{(6)}_{\alpha,\alpha,\alpha} (r') , \\
G_e^{(7)} &= \frac{k_7}{4\pi} \sum_{n,m} F^{(1)}_{\alpha,\alpha,\alpha} (k_7 r_7) C^{(7)}_{\alpha,\alpha,\alpha} (r') , \\
G_e^{(8)} &= \frac{k_8}{4\pi} \sum_{n,m} F^{(1)}_{\alpha,\alpha,\alpha} (k_8 r_8) C^{(8)}_{\alpha,\alpha,\alpha} (r') ,
\end{align*}
\]

where \(A^{(\alpha)}_{\alpha,\alpha,\alpha} (r)\) and \(C^{(\alpha)}_{\alpha,\alpha,\alpha} (r')\) are the unknown wave amplitudes. Following the technique described in [13][16], we then solve the system of \([14][22]\) and obtain the required wave amplitudes, which, in turn, allows us to calculate the electric field given by \([5]\).

IV. NUMERICAL VERIFICATION

The computation of the electric-field intensity (EFI) at the \(yOz\) (namely, at the neck middle cross-section) plane is deemed an essential step for the validation of the new technique. Thus, for a regular male neck model, as the one in Fig.1[1], the average dimensions and the dielectric media properties of its various parts, at the frequency of 2.4 GHz, are given in Table I. Actually, this structure is fairly challenging owing to the different complex relative permittivities and hence the abruptly varying spherical media interfaces. Also, in \([14][22]\), the number of terms, \(n\), needed for the convergence of the infinite sums is up to the order of tens, depending on the type of the field. In particular, for the incident field, the value of \(n\) can be several times larger (\(n = 35-40\)) than the value for the scattered field (\(n = 10-15\)), since the former is evaluated near the point source where field fluctuations are more abrupt. The main setup involves a Hertz dipole (in the sense of a wireless network antenna) with a parallel (along the y-axis) and a perpendicular (along the x-axis) polarization relative to the neck surface. For our comparisons, the exact same model has been numerically simulated by the CST Microwave Studio \([17]\). This package employs the finite integration technique and the finite-difference time-domain method in a domain discretized into adaptive hexahedral cells.

A. Electric field calculation

Based on the above aspects, Figs. 2 and 3 illustrate the EFI magnitude at \(r \sim 1.5a_1\) (yOz plane) for a Hertz dipole (placed on the x-axis: \(r_0 = 1.5a_1, \theta_0 = 90^\circ\), \(\phi_0 = 0^\circ\)) at 2.4 GHz, in the absence and presence of the featured neck model, respectively. As promptly detected, the accuracy of our technique is promising, since in both scenarios the retrieved results are certainly in very good agreement with those of the computational package. This deduction is deemed even more important, considering the complicated geometry of the entire neck model, the multitude of materials, and the two different dipole polarizations. In fact, recalling the complex relative permittivities of Table I one can comprehend that the generalized dGF-based method is capable of successfully treating strongly dissimilar media (even when rather different \(\varepsilon_r\) imaginary parts are involved). Concerning the consistency of our scheme, the inlet figure of Fig. 3 shows
Table 1: Average dimensions and material properties for the different parts of the proposed male neck model

<table>
<thead>
<tr>
<th>Neck Model Part</th>
<th>Outer Radius $a_i$ (mm)</th>
<th>Thickness/Distance $w_i/d_i$ (mm)</th>
<th>Complex rel Permittivity $\varepsilon_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Skin</td>
<td>70</td>
<td>$w_1 = 1$</td>
<td>$40 + j12.5$</td>
</tr>
<tr>
<td>Fat</td>
<td>69</td>
<td>$w_2 = 3$</td>
<td>$4.8 + j9.5$</td>
</tr>
<tr>
<td>Muscle</td>
<td>66</td>
<td></td>
<td>$60.5 + j22.8$</td>
</tr>
<tr>
<td>Right lobe</td>
<td>7</td>
<td>$d_4 = 59$</td>
<td>$56.4 + j15.5$</td>
</tr>
<tr>
<td>Left lobe</td>
<td>7</td>
<td>$d_5 = 59$</td>
<td>$56.4 + j15.5$</td>
</tr>
<tr>
<td>Trachea</td>
<td>11</td>
<td>$d_6 = 44.8$</td>
<td>$36.3 + j11$</td>
</tr>
<tr>
<td>Esophagus</td>
<td>10</td>
<td>$d_7 \cong 23.9$</td>
<td>$68 + j19$</td>
</tr>
<tr>
<td>Organs of the neck</td>
<td>41.8</td>
<td>$d_8 \cong 28.3$</td>
<td>$42.4 + j14.1$</td>
</tr>
</tbody>
</table>

the EFI map at the $xO_3y$ plane for a $y$-oriented Hertz dipole. Observe the smoothness of the plot along with the absence of any nonphysical numerical artifacts due to scattered waves in the vicinity of the source and at the different media interfaces.

Moreover, Fig. 4 presents the EFI magnitude along the perimeter of the neck middle cross-section at $r \sim 1.5a_1$ ($yO_2z$ plane), owing to its critical significance at such studies. Note the promising agreement of the results with those of the computational package, despite the demanding configuration of the problem. On the other hand, these outcomes reveal a strong dependence of the EFI magnitude from the polarization of the Hertz dipole. Specifically, the EFI magnitude of the parallel dipole is larger than that of its perpendicular counterpart, for certain values of angle $\theta$. Finally, it should be mentioned that the proposed algorithm is very fast, owing to the straightforward implementation of the dGfs.

B. Parameterization of the source location

Having validated the accuracy and efficiency of the featured technique, we, now, concentrate on the impact of the Hertz dipole source on the new neck model.

Fig. 5. Magnitude of the electric-field intensity, $|E^{(0)}(r)|$, at the neck middle cross-section ($yO_2z$) plane vs angle $\theta$ for different polarizations of the Hertz dipole, when $z = 0$, $y = 1.1a_1$, and $x \in [0 \text{ mm}, 70 \text{ mm}]$. (a) Parallel to $y$-axis and (b) parallel to $x$-axis. Angle $\theta$ is measured clockwise from the $z$-axis on the $yO_2z$ plane, while the inlet figures are magnified plots of the results in the dotted areas.

To this objective, we compute the electric-field intensity around the neck middle cross-section ($yO_2z$ plane) for various locations and polarizations of the Hertz dipole.

In this framework, Fig. 5 depicts the EFI magnitude around the neck middle cross-section in the case of a Hertz dipole parallel to $y$-axis and $x$-axis, respectively. The source moves along the $x$-axis; in particular $x \in [0 \text{ mm}, 70 \text{ mm}]$, with its other coordinates fixed at $z = 0$ and $y = 1.1a_1$. It should be stressed that since in our numerical simulations, the Hertz dipole is not considered as a point source, its coordinates are measured from the edge that it is closest to the neck model. Consequently, the EFI magnitude around the neck middle cross-section increases as the point source approaches the model and decreases when it departs. Moreover, the shape of the curves in Fig. 5 (and magnified regions) is not seriously affected since the dipole moves along the $x$-axis.
Fig. 6. Magnitude of the electric-field intensity, \( |\mathbf{E}(r)| \), at the neck middle cross-section (\( yOz \)) plane vs angle \( \theta \) for different polarizations of the Hertz dipole, when \( z = 0, x = 0, \) and \( y \in [75 \text{ mm}, 110 \text{ mm}] \). (a) Parallel to \( y \)-axis and (b) parallel to \( x \)-axis. Angle \( \theta \) is measured clockwise from the \( z \)-axis on the \( yOz \) plane, while the inlet figures are magnified plots of the results in the dotted areas.

Fig. 7. Electric-field intensity map at a cross-section of the proposed neck model in Fig. 1. The source is represented as a dot on the right-hand side.

Conversely, Fig. 6 examines the scenario of a Hertz dipole (for both polarizations) which moves along the \( y \)-axis; explicitly \( y \in [75 \text{ mm}, 110 \text{ mm}] \) and \( x = z = 0 \) for its other coordinates. It is deduced that, now, the EFI magnitude increases and decreases drastically in terms of the distance between the neck model and the dipole. Indeed, the shape of the plots in Fig. 6 is affected, as the dipole moves along the \( y \)-axis and the vertical distance from the middle neck augments rapidly.

C. Radiation penetration

The EFI map of Fig. 7 clearly indicates that the majority of the radiation, which penetrates the skin, is absorbed by the multilayered host sphere (i.e., skin, fat, and muscle tissues), leaving a relatively small percentage to penetrate the inner organs. When these organs are surrounded by a very thin (practically negligible) muscle layer, similarly to the thyroid, the radiation absorbed by the tissues increases. So, the maximum limit of the radiation levels on the surface of the thyroid is almost equivalent to the radiation measured at the locations where the thyroid is in contact with the middle neck.

V. CONCLUSION

A precise, fast, and computationally economical algorithm has been introduced in this paper, for the electromagnetic analysis of a generalized non-spherical human neck model. The latter structure provides a robust representation of the neck tissues as spherical layers and employs a set of properly-formulated dyadic Green’s functions with bilocal spatial dependence to compute the desired electric field intensity. Numerical results, concerning the bioelectromagnetic impact evaluation from several wireless network antenna configurations, were in very satisfactory agreement with the reference data obtained from a popular computational package. Lastly, it must be stated that the featured technique can be easily extended at the entire radiofrequency spectrum, taking into account that the electric properties of every tissue can vary with respect to frequency, namely considering the dispersive nature of the involved media.

REFERENCES

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