

Mutual Coupling Compensation in Receiving Antenna Arrays

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Abstract—Mutual coupling compensation in uniform linear and circular receiving antenna arrays of thin wire dipoles is presented. It was observed that the mutual impedance is independent of the incident angle and depends solely on the geometry of the array. By using only one measurement, decoupling matrix is computed and direction of arrival is estimated.

Index Terms—Direction of Arrival, Method of Moments, Mutual Coupling, Receiving Antenna Arrays, UCA, ULA.

I. INTRODUCTION

Mutual Coupling is responsible for the degradation in antenna array performance, both in transmitting and receiving arrays [1–4]. In direction of arrival (DoA) estimation for receiving antennas, the received voltages must be decoupled in order to estimate the incoming signal DoA. In [5], mutual impedances are calculated when the array is in receiving mode. It has been shown experimentally [6], that this method works well for decoupling with a high resolution. However, measurements are required from various incident angles in order to compute the mutual impedances. This may not be practical for experimental purposes.

In this paper, an array of thin wire dipole antennas is illuminated by a plane wave. The received voltages are decoupled and the DoA is estimated. Examples for Uniform Linear Array (ULA) and Uniform Circular Array (UCA) are presented. Method of moments (MoM) is used to find the currents and voltages on the single mode antennas. Here, we show that the mutual impedance is constant for all angles and depends solely on the geometry of the antenna array. Furthermore, it can be calculated using only one measurement. This reduces the computation complexity and the physical labour in the experiments without degrading the accuracy of the mutual coupling compensation.

II. FORMULATION

Consider an N element array of thin wire dipoles where each element is terminated with a load Z_L . The received voltage at the antenna terminal V_i can be written as:

$$V_i = I_i Z_L. \quad (1)$$

The received voltage is the sum of two voltages, S_i and C_i . S_i is the voltage induced on the i^{th} isolated antenna and C_i is the coupling effect from other elements. Thus (1) can be rewritten as,

$$V_i = S_i + C_i. \quad (2)$$

C_i includes the re-radiation effects from all the other elements of the array on the i^{th} antenna as:

$$C_i = Z^{i,1} I_1 + Z^{i,2} I_2 + \dots + Z^{i,i-1} I_{i-1} + Z^{i,i+1} I_{i+1} + \dots + Z^{i,N} I_N. \quad (3)$$

Here, $Z^{i,j}$ is the mutual impedance between elements i and j and I_j is the current induced at the j^{th} port, given by:

$$I_j = \frac{V_j}{Z_L} \quad \text{for } j = 1, 2, \dots, N. \quad (4)$$

To make the presentation simple, let us assume number of elements of the array $N = 4$. Then, from (2), (3) and (4) we get,

$$V_1 - Z^{1,2} \frac{V_2}{Z_L} - Z^{1,3} \frac{V_3}{Z_L} - Z^{1,4} \frac{V_4}{Z_L} = S_1, \quad (5)$$

$$V_2 - Z^{1,2} \frac{V_1}{Z_L} - Z^{2,3} \frac{V_3}{Z_L} - Z^{2,4} \frac{V_4}{Z_L} = S_2, \quad (6)$$

$$V_3 - Z^{1,3} \frac{V_1}{Z_L} - Z^{2,3} \frac{V_2}{Z_L} - Z^{3,4} \frac{V_4}{Z_L} = S_3, \quad (7)$$

$$V_4 - Z^{1,4} \frac{V_1}{Z_L} - Z^{2,4} \frac{V_2}{Z_L} - Z^{3,4} \frac{V_3}{Z_L} = S_4. \quad (8)$$

Due to the symmetry of the problems investigated, the mutual impedance matrix is Toeplitz. This property is used in the above equations. There are three unknowns, $Z^{1,2}$, $Z^{1,3}$ and $Z^{1,4}$ which can be solved by applying least square (LS) method to the above over-determined system for a single incident angle. Once the mutual impedances are found, the decoupling matrix can be found as follows,

$$\begin{bmatrix} 1 & -\frac{Z^{1,2}}{Z_L} & -\frac{Z^{1,3}}{Z_L} & -\frac{Z^{1,4}}{Z_L} \\ -\frac{Z^{1,2}}{Z_L} & 1 & -\frac{Z^{1,2}}{Z_L} & -\frac{Z^{1,3}}{Z_L} \\ -\frac{Z^{1,3}}{Z_L} & -\frac{Z^{1,2}}{Z_L} & 1 & -\frac{Z^{1,2}}{Z_L} \\ -\frac{Z^{1,4}}{Z_L} & -\frac{Z^{1,3}}{Z_L} & -\frac{Z^{1,2}}{Z_L} & 1 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \end{bmatrix} = \begin{bmatrix} S_1 \\ S_2 \\ S_3 \\ S_4 \end{bmatrix}. \quad (9)$$

III. NUMERICAL EXAMPLES

In this section, examples of four-element ULA and UCA are presented. The computations are done using MoM as mentioned in [1], [7]. The mutual impedances calculated by the proposed method are compared with those of [5]. The DoA is estimated for two-coherent sources using the decoupled voltages.

A. Four-element ULA

A ULA with four dipole antennas at 2.4 GHz is considered with spacing $d = 0.2\lambda_0$, length $l = 0.48\lambda_0$ and $l/a = 100$, where a is the radius and λ_0 is the free space wavelength. Each antenna is terminated with $Z_L = 50 \Omega$ load impedance. The array is excited by a plane wave with $\theta = 90^\circ$ and $\phi = 90^\circ$, where θ and ϕ are measured from positive z and positive

x directions, respectively. These angles are chosen because coupling effect is maximum for the ULA. Using MoM, we find the received voltages at each antenna terminal, which is the coupled voltage. Then, the isolated voltages are computed by considering one antenna at a time in the absence of the others. Solving (5) to (8), we find the mutual impedances which are shown in Table I. It should be noted that in the proposed method, only one measurement angle (θ, ϕ) was used to compute the mutual impedances, whereas in [5] at least 10 angles were required to compute the same mutual impedances. It was observed that the mutual impedances found in the proposed method are more accurate than in [5]. Since mutual impedance is independent of the angle of arrival, the decoupling matrix of the proposed method can decouple any voltage irrespective of the incident angle, whereas [5] limits itself to a fixed elevation angle. The real and imaginary mutual impedances are shown in Fig. 1, which are constant for all angles (θ, ϕ).

B. DoA Estimation of Two Sources

Here, two cases for DoA estimation are discussed. In case I, the ULA was excited by two plane waves, with fixed $\phi = 90^\circ$ and different elevation angles, $\theta_1 = 45^\circ$ and $\theta_2 = 75^\circ$. The uncoupled voltages were computed using the mutual impedances of Table I. The isolated, coupled and uncoupled voltages were given as an input to MUSIC algorithm [5] with forward-only spatial smoothing due to the coherent sources as plane wave. In case II, the plane waves were incident from a fixed $\theta = 90^\circ$ but different azimuth angles $\phi_1 = 45^\circ$ and $\phi_2 = 75^\circ$. As Fig. 2 shows, both of the DoAs are successfully detected.

C. Four-element UCA

The same dipole antennas are arranged in a UCA with a radius of $\lambda_0/8$ and excited by the plane wave with $\theta = 90^\circ$, $\phi = 90^\circ$. The coupled and isolated voltages are calculated and then the mutual impedances are computed which are compared in Table I. As an example, the UCA was excited by two incident

TABLE I. RECEIVED MUTUAL IMPEDANCES

Comparison	ULA		
	$Z^{1,2}$	$Z^{1,3}$	$Z^{1,4}$
Proposed	$-19.26 + 11.13i$	$0.0675 + 15.38i$	$10.39 + 4.866i$
Ref [5]	$-18.47 + 10.94i$	$0.0263 + 15.61i$	$10.72 + 4.732i$
UCA			
Proposed	$-21.56 + 9.238i$	$-14.52 + 14.12i$	$-21.74 + 9.371i$
Ref [5]	$-21.95 + 10.62i$	$-12.39 + 15.71i$	$-21.95 + 10.62i$

TABLE II. ISOLATED, COUPLED AND UNCOUPLED VOLTAGES

Ports	UCA		
	Isolated [mV]	Coupled [mV]	Uncoupled [mV]
V_1	$31.7\angle 14.0^\circ$	$29\angle 31.8^\circ$	$31.7\angle 14.0^\circ$
V_2	$31.7\angle -49.1^\circ$	$18\angle -101.2^\circ$	$31.7\angle -49.1^\circ$
V_3	$31.7\angle -43.6^\circ$	$16.6\angle -83.9^\circ$	$31.7\angle -43.6^\circ$
V_4	$31.7\angle 19.5^\circ$	$31.4\angle 39.7^\circ$	$31.7\angle 19.5^\circ$

plane waves with $\theta = 90^\circ$ and $\phi_1 = 35^\circ$ and $\phi_2 = 45^\circ$. The isolated, coupled and uncoupled voltages are shown in Table II. It can be seen that mutual coupling has been successfully compensated.

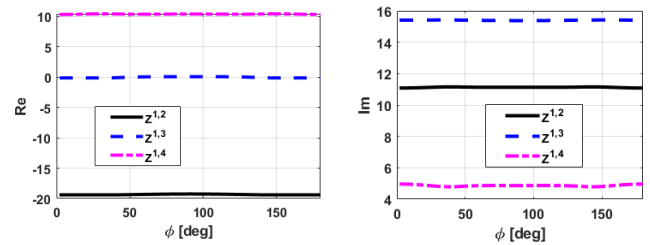


Fig. 1. Mutual impedance (left) real and (right) imaginary for four elements ULA, for all elevation angles.

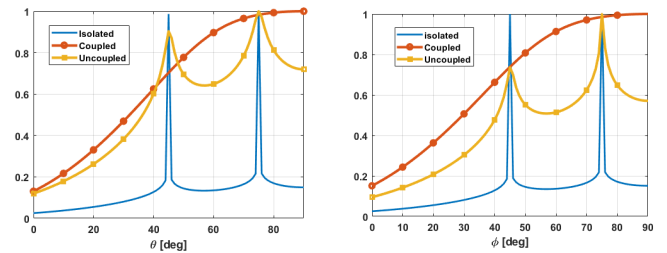


Fig. 2. Spatial spectrum of MUSIC algorithm for DoA detection of two coherent signals from. (Left): $\phi = 90^\circ$, $\theta_1 = 45^\circ$, $\theta_2 = 75^\circ$. (Right): $\theta = 90^\circ$, $\phi_1 = 45^\circ$, $\phi_2 = 75^\circ$.

IV. CONCLUSION

Mutual coupling in receiving antenna arrays of thin wire dipoles has been compensated by using only one measurement. It was observed that the mutual impedance depends only on the geometry of the structure and is independent of the incident angle.

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