Low Frequency Operation and dsPIC Micro-controller Implementation for Multilevel Quasi Z Source Inverter in Photovoltaic Application

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Abstract

In this paper implementation of a micro-controller based pulse width modulation for multilevel quasi Z source inverter (qZSI) is presented. First implementation of component design of qZSI is taken into consideration with continuous and discontinuous operation mode. In this paper operation of multilevel qZSI with low switching frequency is presented. After this detailed modelling for qZSI is established for implementing of PIC microcontroller (PIC 16F877A) to generate the switching signals. Development of a five-level quasi z-source inverter prototype is done and by proper adjustment of the shoot through (ST) switching state and non-shoot through (NST) switching

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state the control signal to the gate drivers is applied. Effective implementation of the proposed scheme is shown by the hardware result.

Keywords: Quasi-z source inverter, PIC microcontroller, pulse width modulation, multilevel inverter, solar photovoltaic, shoot through (ST) state.

Abbreviations

| qZSI | Quasi Z Source Inverter | VSI | Voltage Source Inverter |
|--------|--|--------------|---------------------------------|
| ZSI | Z Source Inverter | MPPT | Maximum Power Point Tracking |
| PV | Photovoltaic | CCM | Continous Conduction Mode |
| CHBMLI | Cascaded H-Bridge Multi Level Inverter | DCM | Discontinous Conduction Mode |
| DCMLI | Diode Clamp Multi Level Inverter | PWM | Pulse Width Modulation |
| THD | Total Harmonics Distortion | Voc | Open Circuit Voltage |
| NPC | Neutral Point Clamped | Isc | Short Circuit Current |
| PD | Phase Disposition | $I_{\rm rs}$ | Cell Reverse Saturation Current |
| | | | |

1 Introduction

With the increasing dependence on photovoltaic (PV) system in grid connection mode, there is a sharp rise in the advancement of multilevel inverter applications. To process high power at medium voltage another choice is to have multilevel configuration [1]. It utilizes semiconductor devices of lower voltage and current ratings [2]. The multilevel inverter (MLI) topologies have various advantages than two-level configurations. The main advantage includes producing higher output voltages with limited switching device rating, lower dv/dt so lower the EMI, lower switching losses, lower total harmonics distortions and better efficiency [3]. A detailed classification of multilevel topologies is given in Figure 1 [4]. The commonly used Multilevel inverter topologies include active neutral point clamped inverter (ANPC), modular multilevel converters (MMC), packed E cell, packed U cell, flying capacitor (FC), neutral point clamped inverter (NPC) and cascaded H-bridge multilevel inverter (CHB) [2]. Several new topologies also have been presented in recent years [5]. The promising topologies are Cascaded Half-Bridge based Multilevel DC Link (MLDCL) Inverter, series connected switched sources (SCSS) based MLI, switched series/parallel sources (SSPS) based MLI, T-type inverter, cascaded bipolar switched cells (CBSC) based MLI, multilevel module (MLM) based MLI, two-switch enabled levelgeneration (2SELG) based MLI, reversing voltage (RV) topology and packed E-cell topologies. These topologies are created while considering the low



Figure 1 Multilevel inverter classification.

switching device counts, maximum possible number of levels, application oriented etc [6]. Midst the numerous multilevel inverter topologies, the diode clamped multilevel inverter (DCMI) and cascaded H-bridge multilevel inverter (CHB) are the most common configurations which have been an area of active research. For high voltage output, the CHB and DCMI require a large number of modules, more switches, and more number of gate drivers and thus leading to increased cost and complexity [7, 8]. To overcome this limitation, the quasi Z-source (QZS) inverter and high gain Z-source inverter are gaining importance in the multilevel inverter configuration, where dclink voltages have been boosted with the help of an LC-based network. The DC link of conventional VSI is replaced by Z source impedance network in a Quasi Z-source inverter and Z-source inverter which not only provides an additional stage of DC-DC boost to output voltage but also creates a new switching state i.e. shoot-through states [9, 10]. These inverters also provide protective enhancement of the switches without affecting the overall cost and efficiency. Areas such as solar photovoltaic, fuel cell stack, and batteries which require high voltage gain, extract the advantage of ZSI/QZSI. Multilevel ZSI/QZSI are best suited for high power and high voltage demand as there is increase in the number of inverter voltage, output ac waveform have low distortion with reduced blocking voltage across each switch. New PWM techniques based on phase disposition (PD) have been developed for multilevel configurations of ZSI/QZSI to have the gain through ST state. In [9, 10], the PD scheme for three levels NPC-ZSI which infers the boosted output voltage with less number commuted switch count have been discussed. Similarly [11, 12] analyze three-level NPC- QZSI which provide continuous dc source current along with a good boost factor.

QZSI, in continuous input current mode, is one of the improved topologies of basic ZSI. Based on continuity QZSI can be classified into



Figure 2 (a) Switched inductor cell (b) improved switched inductor cell (c) switched capacitor cell.

Discontinuous QZSI (D-QZSI) & Continuous QZSI(C-QZSI). In D-QZSI, the common mode noise is less as both input source & DC-link has same earthing along with this the component rating is less compared with basic ZSI. C-QZSI possesses all the above merits of D-QZSI in addition it has continuous input current [13, 14]. On the basis of power flow, QZSI can be classified in unidirectional & bidirectional. Inherently QZSI is unidirectional but by replacement of the source diode with a bidirectional switch bidirectional QZSI is designed [15]. Recent literature mostly classifies QZSI based on boosting capacity of output power & dependence of voltage gain on modulation index. Switched inductor QZSI (SL-QZSI), switched Capacitor QZSI (SC-QZSI) and improved switched inductor cell, improved switched inductor cell and switched ccapacitor on the inverter bridge side is replaced by these cells to form SL-QZSI, ISL-QZSI&SC-QZSI respectively [16–18].

Tapped Inductor Topology (TL-QZSI) proposed in [19] comments on the dependence of voltage gain on turn ratio. In cascaded QZSI/Extended boost QZSI, voltage gain is increased without increasing the number of active switches. High frequency Transformer Isolated QZSI (HFTI-QZSI) is proposed in [20, 21] inherits all the merits of QZSI and having electrical isolation between load & source. Detailed topological construction along with comparative assessment of various qZSI's in photovoltaic application is given in [22]. A 9-level inverter design combining hybrid three-level modified-QZSI and a single-phase modified-QZSI is investigated in [20]. A significant boost of almost three times of dc link voltage of each cell and THD level of approximately 3% have been reported from the simulation & experimental results. A new five level QZS-NPC inverter is proposed in [21] having a level shifted carrier wave. The simulated results infer high boosted output voltage and good reactive power capability but it's not validated experimentally. A two stage control method is presented in [22] for QZSI to control the output voltage & current. It also concludes that capacitor voltage controller for ZSI/QZSI is preferred above dc link controller for conventional VSI to boost output voltage. An inverted phase-shifted PWM scheme is employed for a five-level grid-connected QZSI injecting power into the PV-grid at reduced THD level is worked in [23]. The power is controlled using dc-link controller & independent MPPT control. The low switching frequency helps in reducing the switching losses considerably and hence is suited for voltage high power applications [24, 25]. The applications of qZSI have been worked out in various literatures considering the improvements in various parameters in [26-32]. Low switching frequency PWM techniques are useful in operation of voltage source converter as it will reduce the switching losses associated with the turning on and turning off of the semiconductor switches. It improves the overall system reliability. The main low switching frequency techniques available in the literature includes selective harmonics elimination (SHE) [33-41], selective harmonics mitigation (SHM) [42], pulse width amplitude modulation (PWAM) [43], nearest level control (NLC) [44], synchronous optimum pulse width modulation (SOPWM) etc. [45]. The SHE PWM technique has been widely investigated and used in various applications comparison to other low switching frequency techniques [40, 41].

In the manuscript, a quasi Z source based multilevel inverter configuration with a low switching frequency for solar photovoltaic operation is presented. The proposed technique decreases the switching losses and henceforth results in better reliability and efficiency of the power converters switches. The proposed model have been implemented using the dspic based microcontroller (PIC 16F877A), which is a low cost controller and thus results in cost effective solution. The dynamics modeling alongwith component design in continuous and discontinuous mode of operation for quasi network is provided for effective closed loop operation of the proposed low switching frequency technique. The five level qZSI prototype by having two H-bridge modules have been developed in the laboratory and PWM signals are applied by suitable adjustment of the shoot through switching states and non-shoot through switching states. The computational and hardware result display the effective implementation of the presented scheme. The PWM signals have been shown in separate figures to clearly identify the shoot through state and non-shoot through state of each power electronics switches and to indicate the switching frequency of the qZSI. The paper is divided as follows: Section 2 demonstrates the mathematical modeling of the solar photovoltaic system and qZSI alongwith CCM and DCM operation components design. Simulation and hardware results are obtained in Section 3. At the end Section 4 concludes the work done.

2 Mathematical Modelling

2.1 Solar Cell

Solar panels are constructed with solar cells as a basic component. Several solar cells are arranged in series and parallel combination to get desired voltage and currents at the output. The single solar cell diode model is the combination of a diode, two resistors, and a current source. To obtain the I-V, characteristics, the required expression can be derived and can be expressed by (1). From the expression, it is clear that the photocurrent is dependent on the solar irradiance and temperature of cell and therefore, it can be represented by (2).

$$I_{ph} = [I_{sc} + k_i \cdot (T - 298)] \cdot \frac{G}{1000}$$
(1)

$$I_O = I_{rs} \cdot \left(\frac{T}{T_n}\right)^3 \cdot \exp\left[\frac{q \cdot E_{go} \cdot \left(\frac{1}{T_n} - \frac{1}{T}\right)}{n \cdot K}\right]$$
(2)

Here I_{SC} is at 25°C short circuit current, T is the temperature of cell and k_i is the temperature coefficient of short circuit current. Diode current or the cell saturation current depends on cell temperature and is given by (3), I_{rs} is the cell's reverse saturation current at reference solar radiation and temperature and E_{go} represents the band gap energy of semiconductor utilized for manufacturing the cell. Also, the reverse saturation current is the current through the shunt resistor. The expression for the shunt current and the load current can be given by (4)–(5).

$$I_{rs} = \frac{I_{sc}}{-1 + e^{\left(\frac{q \cdot V_{oc}}{n \cdot N_S \cdot K \cdot T}\right)}}$$
(3)

$$I_{sh} = \left(\frac{V + I \cdot R_s}{R_{sh}}\right) \tag{4}$$

$$I = I_{ph} - I_O \cdot \left[\exp\left(\frac{q \cdot (V + I \cdot R_s)}{n \cdot K \cdot N_s \cdot T}\right) - 1 \right] - I_{sh}$$
(5)

Where $I_{\rm ph}$ is the generated current or photo current, $I_{\rm O}$ is the current saturation and $R_{\rm S}$ is resistance in series. Based on the mathematical modelling of single diode photovoltaic cell, the simulation model of PV cell is developed and the I-V, PV characteristics have been shown in Figure 3 for various values of Irradiance and temperatures.



Figure 3 TRINA solar TSM-250PA05.08 characteristics.

2.2 Quasi Z Source Inverter

Buck or boost voltage operation for a single stage control is achieved in quasi Z-source inverter. In qZSI topology the controlled semiconductor switches can be simultaneously turned ON in the same leg and thus provides the gain in the output voltage. Also, it will remove the requirement of the dead time in practical implementation of the converter and therefore offers simplifications in control design. The single cell of the qZSI topology is given in Figure 4(a). For the construction of quasi network, two inductors and two capacitors are required. The shoot through (same switches in the leg are turned on), null and non-shoot through states or active states will charge or discharge these components based on the gain required in the output voltage. In the null state, simultaneous turning off of all the switches causes no power transfer from the input to the output side takes place. The equivalent circuit [46] of the qZSI in the non-shoot-through state and in the shoot-through state are shown in Figures 4(b) and 4(c), respectively.

All the currents and the voltages are well-defined in the given figures and arrows represent the polarities. T is the time of one switching cycle, T_0 is the shoot-through state time interval, T_1 , the non-shoot-through state time interval, hence $T = T_0 + T_1$, and $D = \frac{T_0}{T}$ is the shoot-through duty ratio.



Figure 4 qZSI (a) circuit (b) equivalent circuit NST state(c) equivalent circuit ST state.

Thus, for the non-shoot-through (NST) state time interval T_1 , we get (6) and (7).

$$V_{L1} = V_{in} - V_{C1}; \quad V_{L2} = -V_{C2} \tag{6}$$

$$V_{PN} = V_{C1} - V_{L2} = V_{C1} + V_{C2}; \quad V_{diode} = 0$$
(7)

For the shoot-through (ST) state time interval T_O , one can get (8)

$$V_{L1} = V_{C2} + V_{in}; \quad V_{L2} = V_{C1}$$

 $V_{PN} = 0; \quad V_{diode} = V_{C1} + V_{C2}$ (8)

The inductors average voltage at steady state over one switching cycle is zero. Therefore, we get (9) and on solving we can have (10).

$$V_{L1} = \overline{v_{L1}} = \frac{T_O(V_{C2} + V_{in}) + T_1(V_{in} - V_{C1})}{T} = 0$$

$$V_{L2} = \overline{v_{L2}} = \frac{T_O(V_{C1}) + T_1(-V_{C2})}{T} = 0$$
(9)

Thus,

$$V_{C1} = \frac{T_1}{T_1 - T_O} V_{in}, \quad V_{C2} = \frac{T_O}{T_1 - T_O} V_{in}$$
(10)

The inverter bridge's peak dc-link voltage is,

$$V_{PNpeak} = V_{C1} + V_{C2} = \frac{T}{T_1 - T_O}, V_{IN} = \frac{1}{1 - 2\frac{T_0}{T}} V_{in} = BV_{in}$$
(11)

Here, B is the qZSI boost factor. This is also the diode peak voltage. The inductor L_1, L_2 average current is calculated from the power rating P of the system

$$I_{L1} = I_{L2} = I_{in} = \frac{P}{V_{in}}$$
(12)

As per Kirchhoff's current law and from the above equation (13), we can also get that

$$I_{C1} = I_{C2} = I_{PN} - I_{L1}, \quad I_D = 2I_{L1} - I_{PN}$$
(13)

The current and voltage stress of the ZSI and qZSI are compared and have been shown in given in Table 1.

Here, m is the modulation index, P is the power rating of system and \hat{V}_{in} is the ac peak phase voltage. The relationships between modulation index and boost factor is given in (14).

$$m = \frac{T_1}{T_1 - T_0}; \quad n = \frac{T_O}{T_1 - T_O}; \quad \text{thus } m > 1; m - n = 1;$$

$$B = \frac{T}{T_1 - T_O}, \quad \text{hence } m + n = B, \ 1 < m < B.$$
(14)

| | $V_{L1} = V_{L2}$ | | V_{PN} | | V_{diode} | |
|------|-------------------|--------------------|----------|--------------|----------------------|-------|
| | T_O | T_1 | T_O | T_1 | T_O | T_1 |
| ZSI | mV_{in} | $-nV_{in}$ | 0 | BV_{in} | BV_{in} | 0 |
| qZSI | mV_{in} | $-nV_{in}$ | 0 | BV_{in} | BV_{in} | 0 |
| | V_{C1} | | | V_{C2} | \widehat{V}_{in} | |
| ZSI | m | V_{in} | n | nV_{in} | $\frac{MBV_{in}}{2}$ | |
| qZSI | m | V_{in} | n | V_{in} | $\frac{MBV_{in}}{2}$ | |
| | $I_{IN} = I$ | $I_{L1} = I_{L2}$ | I_{C1} | $=I_{C2}$ | I_D | |
| ZSI | ī | $\frac{P}{V_{in}}$ | I_{PN} | $I - I_{L1}$ | $2I_{L1} - I_{PN}$ | |
| qZSI | Ī | $\frac{P}{V_{in}}$ | I_{PN} | $-I_{L1}$ | $2I_{L1} - I_{PN}$ | |

 Table 1
 Current and voltage stress in ZSI and qZSI

From Table 1 it is clear qZSI has all advantages of ZSI. By a given boost factor it is possible to buck or boost voltage. ZSI can handle a shootthrough state, and thus has reliability greater than the traditional VSI. As compared to qZSI, ZSI has some exceptional merits i.e., ZSI sustains the same high voltage because of the presence of two capacitors while the voltage on capacitor C_2 in qZSI is lower, which means capacitor rating is lower. Also in the boost mode of ZSI, input current is discontinuous while there is continuous input current in qZSI due to the input inductor L_1 , which will minimise input stress. Also, there are less EMI problems.

2.3 CCM and DCM Analysis of qZSI

The performance of qZSI is affected by CCM and DCM conduction mode as the circuitry of qZSI internally has a DC-DC voltage boost structure with capacitors and inductors present intrinsically. The governing equations of qZSI are valid only in continuous conduction mode. However for DCM we need to formulate the new governing equations [47]. To yield the desirable results, the CCM and DCM operations are used to design the qZSI. The input inductor in the qZSI varies the source current of the qZSI network. Thus when during ST state the input current never drops to zero, the qZSI network can operate in CCM. In CCM operation input voltage stress is minimised that has significance in power electronic applications. Even if the inductance is large, with the decrease in load the converters enter into DCM mode. In other words, under large load change the converter changes from CCM to DCM or vice-versa.

2.4 Operation Analysis in CCM

In one switching cycle the CCM operating state of the qZSI consists of ST state and NST state. $T = D_0 + D_1$, where, D_0 and D_1 represents ST and NST duty ratio, respectively. By the circuit analysis on the equivalent circuit of qZSI in ST state a first order differential equation is obtained and is given in Figure 2(c). The state space equation in matrix form is given by (15).

$$\begin{bmatrix} L_{1} & 0 & 0 & 0 \\ 0 & L_{2} & 0 & 0 \\ 0 & 0 & C_{1} & 0 \\ 0 & 0 & 0 & C_{2} \end{bmatrix} \begin{bmatrix} i_{L1}(t) \\ i_{L2}(t) \\ v_{C1}(t) \\ v_{C2}(t) \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{L1}(t) \\ i_{L2}(t) \\ v_{C1}(t) \\ v_{C2}(t) \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{in}(t) \\ i_{0}(t) \end{bmatrix}$$
(15)

Where i_{L1} is the inductor-1 current, i_{L2} is inductor-2 current, i_{C1} is the capacitor-1 current, i_{C2} is the capacitor-2 current, v_{L1} is the inductor-1 voltage, v_{L2} is the inductor-2 voltage, V_{in} is input voltage and I_0 is the output dc current. $V_{dc} = 0$ in ST state DC link voltage. Now from NST state circuit analysis shown in Figure 2(b), we get the expression as shown in (16) [48, 49].

$$\begin{bmatrix} L_{1} & 0 & 0 & 0 \\ 0 & L_{2} & 0 & 0 \\ 0 & 0 & C_{1} & 0 \\ 0 & 0 & 0 & C_{2} \end{bmatrix} \begin{bmatrix} i_{L1}(t) \\ i_{L2}(t) \\ \dot{v}_{C1}(t) \\ \dot{v}_{C2}(t) \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{L1}(t) \\ i_{L2}(t) \\ v_{C1}(t) \\ v_{C2}(t) \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 0 \\ 0 & -1 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} v_{in}(t) \\ i_{0}(t) \end{bmatrix}$$
(16)

 $V_{dc} = V_{c1} + V_{c2}$ in NST state. We know that the inductor current and the capacitor voltage cannot vary instantaneously. Thus, in steady-state



Figure 5 Inductor voltage and inductor current waveforms at boundary conditions.

condition in one switching cycle, the average voltage across the inductor and the average current that flows in the capacitor is equal to zero [50]. The average values are given by (17).

$$\begin{cases} \langle V_{L1} \rangle = D_0 T (V_{IN} + V_{C2}) + D_1 T (V_{IN} - V_{C1}) \\ \langle V_{L2} \rangle = D_0 T (V_{C1}) + D_1 T (-V_{C2}) \\ \langle I_{C1} \rangle = D_0 T (-i_{L2}) + D_1 T (i_{L1} - i_0) \\ \langle I_{C2} \rangle = D_0 T (-i_{L1}) + D_1 T (i_{L2} - i_0) \end{cases}$$

$$(17)$$

The steady state inductor current relationship, the capacitor voltages, the input voltage and DC- link voltages with respect to D_0 is obtained by equating our above equations to zero and thus we obtain the (18) [51–53]. Here, qZSI power input is given by P and load resistance is represented by R. The inductor voltages have been analyzed before. We know the current through an inductor lacks the capability of changing instantaneously. Because of this the ST characteristics impart ripple effect in the inductor current. We for analysis have assumed for our system to be in steady state, increase in ripple current that happens in shoot-through state is shown as positive and is equal to decrease in ripple current in non-shoot through state which is negative. If $L_1 = L_2$ and switching frequency is f_s , ΔI_{L1} and ΔI_{L2} are obtained as (19) and (20) respectively. The voltage across inductors and current through inductors for boundary cases has been shown in Figure 5.

$$I_{L1} = I_{L2} = \frac{P}{V_{in}} = \frac{(MV_{dc})^2}{V_{in}R}$$
$$\frac{V_{C1}}{V_{in}} = \frac{(1 - D_0)}{(1 - 2D_0)}$$
$$\frac{V_{C2}}{V_{in}} = \frac{D_0}{(1 - 2D_0)}$$

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$$\frac{V_{DC}}{V_{in}} = \beta = \frac{1}{(1 - 2D_0)}$$
(18)

$$\Delta I_{L1} = \frac{1}{L} \int_0^{t_0 = D_0 T} V_{L1} dt = \frac{1}{L} \int_{t_1 = D_0 T}^T V_{L1} dt$$
$$\Delta I_{L1} = \frac{(V_{in} + V_{C2})(D_O)}{L f_s}$$
(19)

$$\Delta I_{L2} = \frac{1}{L} \int_{0}^{t_0 = D_0 T} V_{L2} dt = \frac{1}{L} \int_{t_1 = D_0 T}^{T} V_{L2} dt$$
$$\Delta I_{L2} = \frac{(V_{C1})(D_O)}{L f_s}$$
(20)

The boundary inductor current is half the ripple current as given below,

$$I_{LB} = \frac{1}{2}\Delta I_L$$

The boundary currents for both the inductors will be given by (21).

$$I_{LB1} = I_{LB2} = \frac{(V_{in} + V_{C2})(D_O)}{2Lf_s} = \frac{(V_{C1})(D_O)}{2Lf_s}$$
(21)

For the proposed in continuous conduction mode, $I_L \ge I_{LB}$, for the proposed inverter to work in DCM $I_L < I_{LB}$, Therefore the condition can be established as given in (22) and (23) respectively.

$$I_{LB} \ge \frac{(V_{in} + V_{C2})(D_O)}{2Lf_s} \quad \text{or} \quad \frac{(V_{C1})(D_O)}{2Lf_s}$$
(22)

$$L \ge \frac{(V_{in} + V_{C2})(D_O)}{2I_{LB}f_s} \quad \text{or} \quad \frac{(V_{C1})(D_O)}{2I_{LB}f_s}$$
(23)



Figure 6 Inductor voltage and current waveforms for discontinuous conduction mode.

Therefore for a known inductance minimum inductor current before DCM starts will be given by (24).

$$I_{LB\min} = \frac{(V_{in} + V_{C2})(D_O)}{2Lf_s} \quad \text{or} \quad \frac{(V_{C1})(D_O)}{2Lf_s}$$
(24)

2.5 DCM Operation Analysis

In DCM the steady- state voltage conversion equation used earlier does not hold. For analysis we need to use inductor waveform of DCM. The inductor current thus obtained will be given by (25)

$$I_L = \frac{1}{2} \times \frac{1}{T} \times \Delta I_L \times \left(D_O T + \frac{V_{in} + V_{C2}}{V_{in} - V_{C1}} D_O T \right)$$
(25)

By performing substitutions we obtain the voltage ratio as given in (26).

$$\frac{V_{dc}}{V_{in}} = \frac{D_O}{1 - D_O} \sqrt{\frac{R \left(D_O - 1 \right)}{2L f_s \left(D_O \right)}}$$
(26)

After the above analysis it is inferred that in DCM, the voltage conversion ratio is dependent on V_{in} , D_O , L and R. Thus the transition from CCM to DCM depends on resistance and load. Below given are the output current and voltage equations,

$$V_{Orms} = \frac{MV_{dc}}{\sqrt{2}}$$
$$I_{Orms} = \frac{I_{Opeak}}{\sqrt{2}}$$

for M = 1; $\frac{Lf_s I_O}{V_{in}} = D - D^2$

$$V_{in} = 2\frac{\hat{V}_{in}}{M}$$
$$150 = 2\frac{\hat{V}_{in}}{0.9}$$
$$\hat{V}_{in} = 67.5 V$$

Where the minimum value of input voltage is 150 V, therefore we obtain the following values after computation.

$$G = \frac{M}{\sqrt{3}M - 1} = \frac{0.9}{(\sqrt{3} \times 0.9) - 1} = 1.61$$
$$M_{\min} = \frac{G_{\max}}{\sqrt{3}G_{\max} - 1} = \frac{1.61}{\sqrt{3}(1.61) - 1} \approx 0.9$$
$$B_{\max} = \frac{1}{\sqrt{3}M_{\min} - 1} = \frac{1}{\sqrt{3}(0.9) - 1} \approx 1.78$$
$$\hat{V}_{PN} = B_{\max}V_{in}$$
$$\hat{V}_{PN} \approx 267V$$

Thuson Inverter Bridge, 267 V is the maximum voltage stress. Let the system be of power rating 1 KW.

$$I_{in} = I_{L1} = I_{L2} = \frac{P}{V_{in}} = \frac{1 \times 10^3}{150} = 6.67 A$$

 I_{in} is maximum current flowing in an inductor. The inductor voltage and current waveforms for discontinuous conduction mode are shown in Figure 6.

2.6 Inductor and Capacitor Selection

For the qZSI inverter working in the boost mode of conversion, the potential maximum interval of the shoot-through state when is calculated as:

$$T_{0\,\text{max}} = \frac{2 - \sqrt{3}M_{\text{min}}}{f_s} = \frac{2 - \sqrt{3}(0_9)}{20 \times 10^3} \approx 2.2 \text{ ms}$$

If Peak to peak ripple $r_c\%$ is having value as 20% for the proposed system, the inductance can be calculated as:

$$L_1 = L_2 = \frac{V_L \Delta T}{\Delta I} = \frac{mV_{in}}{I_L \max r_c \%} \cdot \frac{1}{2} T_{0-\max}$$

From the observations done earlier, capacitor voltage C_1 is 250 V. Therefore,

$$mV_{in} = V_{C1}$$

$$m(150) = 250$$

$$m = 1.66$$

$$L_1 = L_2 = \frac{1.66 \times 150}{6.67 \times 0.2} \times \frac{1}{2} \times 2.2 \times 10^{-3} \approx 2.05 \times 10^{-3} \approx 2.05 \ mH$$

The capacitance of two capacitors is:

$$C_1 = C_2 = \frac{2 \cdot I_L \Delta T}{\Delta (V_{C1} + V_{C2})} = 2 \cdot \frac{I_L}{B V_{in} r_v \%} \cdot \frac{1}{2} T_{0-\max}$$

Where $r_v \% = 0.017$ (assumed). The capacitance of two capacitors is:

$$\Rightarrow C_1 = C_2 = 2 \cdot \frac{6.67}{1.78 \times 150 \times 0.017} \times \frac{1}{2} \times 2.2 \times 10^{-3} \approx 646.5 \mu F$$

Thus, $L_1 = L_2 \approx 2.05 \ mH$

$$C_1 = C_2 \approx 646.5 \ \mu F$$

3 Experimental Setup and Hardware Results

The hardware setup of the presented system is developed to obtain the practical results and all the components have been shown in Figure 7. For proof of the proposed concept, the actual panels have been replaced with dc link voltages and battery system by a resistive load.

The dspic microcontroller board (PIC16F877A) have been used to generate PWM signal. The dspic signal is provided to gate drives circuit which isolates and amplifies the signals to a suitable value for turning ON the semiconductor switches. The PWM signals with proper ST and NST states have been depicted in Figure 8. The low frequency control is obtained on the basis of the mathematical model done in the paper. The gating signals for individual cells are shown in (6). The stable operation is ensured by adjusting the gain of the controller. The proposed scheme has been implemented in grid connection mode and the complete schematic has been shown in (7). In the proposed scheme, into the grid the current is injected at unity power factor and the harmonics content is minimum. For this purpose there is only β -current component (*sin* ω t) and thus α -current component is created for necessary transformations. The transformation into d-q coordinates results into dc component.

The required ρ angle is chosen between $\alpha\beta$ and d-q co-ordinates axes. In order to keep $v_q * = 0$, the ρ value is chosen so that dq-axis aligns with the v_d .







Therefore, the v_{α}^* and v_{β}^* will work as reference and its comparison is done with a triangular signal and on the basis of this logic there is generation of PWM pulses. The ST reference line is adjusted so that the required boost is obtained at the output. Only v_{β}^* component is required in this case as v_{β} and i_{β} are already known and $v_{\beta}*$ component is calculated. Here the PV generated power injected in the grid will be proportionate to the current d-axis current i_d as grid voltage is fixed. Hence, the d-axis reference current i_d^* is fixed and it is obtained from the MPPT algorithm. The control system design is



Figure 9 Control system design.

represented in Figure 9 whereas the pin configuration of the microcontroller used in generation of the PWM signal for the semiconductor devices is shown in Figure 10.

So i_d^* is nothing but the output current from the MPPT algorithm and it will try to track the d-axis current i_d . The Pin numbers in for generating all the eight PWM pulses is shown in Table 2. The main programme for generating PWM pulses in dspic microcontroller is shown in Table 3. The gate pulses to various semiconductor switches, module output voltage and multilevel

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Figure 10 Pin configurations of dsPIC micro controller.

 Table 3
 Controller code for PWM signal generation







Figure 11 Output gate pulses, module output and multilevel output voltage.

output voltage have been shown in Figure 11(a) to Figure 11(i) respectively. The hardware results validate the proposed concept in this paper. The total harmonics distortion has been found in the output waveform is 14.03%.

4 Conclusion

A novel microcontroller based low switching frequency-based pulse width modulation technique for Multi level quasi Z source inverter (qZSI) has been investigated in paper. First the component design of qZSI with continuous and discontinuous operation modes is considered. Then for effective implementation of PIC microcontroller (PIC 16F877A) detailed modeling for qZSI is established for generating the PWM pulses. The five level quasi z-source inverter prototype by having two H-bridge modules have been developed and PWM signals are applied by suitable adjustment of the ST switching states and NST switching state. The proposed algorithm is extremely useful in solar photovoltaic system and application in variable speed drives. The low switching frequency scheme minimizes the switching losses and thus improves the efficiency and reliability of the overall system. The computational and hardware result depicts the effective implementation of the presented scheme.

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