



A model-based methodology for rapid designing of hydraulic breakers

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ABSTRACT

The design and dimensioning of a hydraulic breaker with nitrogen spring is often carried out on the base of tradition and empirical considerations. This article proposes a methodology dedicated to such breakers that, with a simplified procedure, allow a rapid determination of the main dimensions of piston and spring, starting from the required performance, namely: the impact energy and work frequency. The method is based on a simplified mathematical model of the breaker and has been validated by means of experimental test on commercial breakers.

ARTICLE HISTORY

Received 4 February 2016
Accepted 6 December 2016

KEYWORDS

Hydraulic breaker; rapid designing; functional design; nitrogen spring; impact energy

1. Introduction

A hydraulic breaker is an indispensable device for demolition of artefacts, construction of any kind of civil infrastructures, mines excavation and is often applied as an excavator tool. It is a machine able to convert the hydraulic energy provided by a supply unit into mechanical energy, which is transmitted to a chisel in terms of cyclical percussions.

In the design and development phase of a new breaker, a dynamic model is able to simulate its behaviour and could be an useful tool, allowing to study and optimise its performance. In this respect, Ficarella *et al.* (2006) highlighted already that scientific literature seems to be very scarce.

Some works are concerned with very detailed models, often implemented in commercial packages for simulation of hydraulic systems, which considers all single components of the device. Yan and Xu (2010) proposed a model realised in ADAMS/Hydraulics, able to investigate the influence of the oil flow, accumulator pressure, etc. on the working course of a piston. Giuffrida and Laforgia (2005) developed a model in the AMESim environment aimed at simulating the hydraulic circuit with reference to the real geometry of a commercial one, taking into account the real dimensions of the parts, the clearances and the body masses. Xu and Zhang (2009) studied the working performance of a hydraulic breaker considering in particular the viscous friction. Although this approach allows to realise very accurate models, their complexity makes it difficult to have a clear view of the main factors that influence the breaker performance.

Vice versa, in the preliminary project phase of a new machine, it may be convenient to make simplifications

aimed at individuating those factors that influence the main breaker characteristics, like the impact energy and the work frequency.

In some cases, the number of parameters has been reduced by means of a dimensionless approach and similarity criteria. Gorodilov (2005) presented techniques of mathematical model building for the hydraulic percussion systems. Gorodilov again (2000) analysed the working cycle of a hydraulic breaker using similar criteria, and the analogy method in which the factors defining the system are not considered separately, but in some combinations in the form of total effects, then deepening, in a subsequent work (2002), also the effect of an ideal distributor. In addition, Gorodilov (2012, 2013) proposed a mathematical model of a two-way hydropercussion.

This paper presents a simplified model of a hydraulic breaker, aimed at supporting the designer in the determination of the main geometrical parameters, namely: the dimensions of the piston and the gas spring. First, a procedure for the functional design of the breaker, supported by a simplified model, is proposed; then, the results of experimental tests for the validation of the design methodology, performed on commercial breakers, are shown.

2. The breaker working principle

This study considers hydraulic breakers whose impact energy is provided by a nitrogen spring. A breaker scheme is depicted in Figure 1.

The working cycle is divided in two phases.

First, by means of the automatic commutation of a valve (not shown in the figure), a hydraulic pump with supplying pressure P_s and flow rate Q_{IN} is connected to

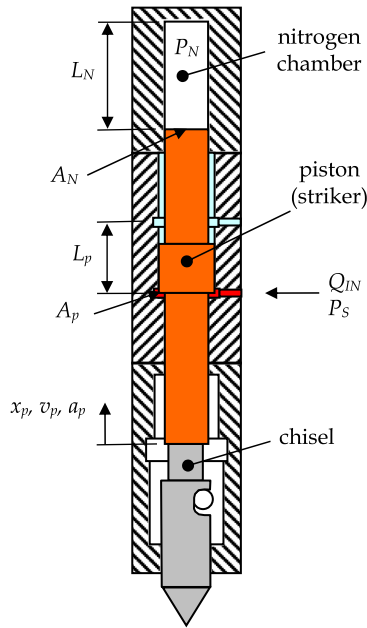


Figure 1. The hydraulic breaker scheme.

the lower chamber of a cylinder, causing the lifting of the piston with active area A_p . During the lifting stroke, a nitrogen chamber, with section A_N and pressure P_N , is charged to act as a gas spring (*phase 1*).

Then, when the piston lifting stroke reaches level L_p , a new automatic commutation of the distributor connects the lower chamber to discharge.

In this moment, since the upward thrust of the pressurised oil is missing, the push of nitrogen on the spring area causes the downward motion of the piston (*phase 2*) which reaches, just before impact, the maximum desired velocity $|v_{pmax}|$.

Finally the piston, acting as a striker, bumps against the chisel, which in turn will hit the object to be demolished, transferring the impact energy. At the end of phase 2, the cycle restarts from the beginning.

From energetic point of view, neglecting losses, first, the hydraulic energy of the supplying pump is transferred to the nitrogen spring in form of potential elastic energy; subsequently, the spring, discharging, gives back its elastic energy to the piston that, in downward stroke, acquires kinetic energy; finally, the piston transfers energy to the chisel that must perform the mechanical demolition work.

3. The functional design

In the first design step of a new hydraulic breaker, once the performance specifications have been defined, it is necessary to individuate the main functional characteristics that will constitute the starting point for the detailed design.

This article proposes a design tool with which the designer can calculate the stroke L_p and section A_p of the piston, the length L_N and section A_N of the nitrogen

spring, starting from the flow characteristic of the supplying pump, in particular the value of the nominal flow rate Q_{IN} , and having fixed as design specifications the value of the impact energy E_i that must be provided by the striker during impact and the desired work frequency f .

Hereinafter, first, a simplified model aimed at the functional design of the breaker is described; then, a dimensionless analysis of the system is presented; finally, a complete designing procedure is proposed and the variation of the functional design parameters versus the dimensionless parameters is analysed.

4. The model

The proposed model considers lumped parameters, with ideal fluid, no mechanical friction and hydraulic resistance. Besides, the operation of the switching valve is not taken into account. The whole modelling is made with the purpose of obtaining a simplified and explicit formulation that can be used as a support for the rapid design of a new breaker.

In phase 1 of the working cycle, the pump supplies an oil flow rate Q_{IN} to the lower chamber of the cylinder; therefore, the piston moves upward at a velocity v_{pu} that approximately can be considered constant. Thus, the raising time t_u of the piston, to perform the upward stroke L_p , can be expressed as:

$$t_u = \frac{L_p A_p}{Q_{IN}} = \frac{L_p}{v_{pu}} \quad (1)$$

where

$$v_{pu} = \frac{Q_{IN}}{A_p} \quad (2)$$

is the average upward speed of piston.

Once the valve has switched, the piston is subjected to the nitrogen spring pressure and starts the downward stroke (*phase 2*). In this condition, the free body diagram of the piston, neglecting weight, frictions, flow forces and back pressures due to resistances of the hydraulic orifices, is the one depicted in Figure 2.

Consequently, the equilibrium equation is simply:

$$p_N A_N + m_p \ddot{x}_p = 0 \quad (3)$$

where m_p is the mass of the piston.

Considering the high working frequency of the hydraulic breaker, the most appropriate model for the nitrogen spring would be adiabatic (Gorodilov 2002, Quaglia *et al.* 2012) or, at most, a polytropic one (Giuffrida and Laforgia 2005, Ferraresi *et al.* 2014). Assuming that the reduction of the chamber volume of a typical hydraulic breaker spring is about 20%, the adoption of an isothermal model rather than an adiabatic one underestimates the maximum pressure of

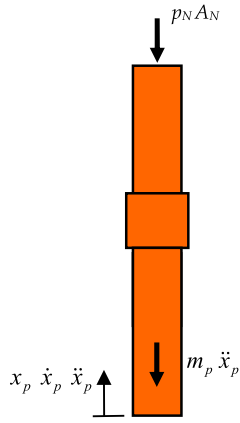


Figure 2. The free body diagram of the piston in phase 2.

nitrogen spring by approximately 8%. With the aim to simplify the model, we considered acceptable such an error in the case under study, and we decided to use an isothermal transformation for the nitrogen spring. Said P_{N0} the initial nitrogen pressure, $V_{N0} = A_N L_N$ the initial spring volume, i.e. with piston fully lowered, one has:

$$P_N V_N = P_{N0} V_{N0} \quad (4)$$

hence, considering that:

$$V_N = V_{N0} - A_N x_p = A_N L_N - A_N x_p \quad (5)$$

the absolute spring pressure, at a generic position x_p of the piston, can be expressed as:

$$P_N = \frac{P_{N0}}{1 - x_p/L_N} \quad (6)$$

By substituting Equation (6) into (3) and confusing the relative with the absolute pressure (acceptable assumption for quite high pressure in nitrogen chamber), it is possible to express the piston acceleration \ddot{x}_p in the downward stroke, at a generic position x_p of the piston:

$$\ddot{x}_p = - \frac{P_{N0} A_N}{(1 - x_p/L_N) m_p} \quad (7)$$

Integration of Equation (7) leads to the downward velocity $v_p = \dot{x}_p$ of the piston, a generic position x_p :

$$\int_0^{v_p} v_p dv_p = - \frac{P_{N0} A_N}{m_p} \int_{L_p}^{x_p} \frac{1}{1 - x_p/L_N} dx_p \quad (8)$$

one has:

$$v_p = - \sqrt{\frac{2P_{N0} A_N L_N}{m_p} \ln \left(\frac{1 - x_p/L_N}{1 - L_p/L_N} \right)} \quad (9)$$

Since the impact of the striker to the chisel occurs at the end of the downward stroke, imposing in Equation

(9) the conditions of null stroke $x_p = 0$ and maximum velocity $v_p = v_{p\max}$, the impact energy can be expressed as:

$$E_i = \frac{1}{2} m_p v_{p\max}^2 = P_{N0} A_N L_N \ln \frac{1}{1 - L_p/L_N} \quad (10)$$

Finally, to express the falling time t_d of the piston, it is necessary to integrate the velocity as expressed in Equation (9):

$$t_d = \sqrt{\frac{m_p}{2P_{N0} A_N L_N}} \int_{0.95 L_p}^0 \frac{1}{\sqrt{\ln \left(\frac{1 - x_p/L_N}{1 - L_p/L_N} \right)}} dx_p \quad (11)$$

Unfortunately, the integral in Equation (11) cannot be solved in explicit form. With the aim of finding a compromise between accuracy and simplicity in modelling, we decided to assume a linear relation between the piston velocity v_p and its position x_p :

$$v_p = v_{p\max} \left(1 - x_p/L_p \right) \quad (12)$$

In order to calculate the falling time of the piston t_d , the velocity expressed by Equation (12) must be integrated. Taking into account that the falling velocity of the piston is null at the higher piston position L_p , the integral must be evaluated from a starting position close to the extreme one. Obviously, the falling time t_d depends on the choice of the integration limits. From the analysis of experimental tests, described in Section 7, it was found that choosing the starting position of the piston equal to the 95% of the total stroke L_p , the calculated falling times were consistent with the real ones.

$$t_d \approx \int_{0.95 L_p}^0 \frac{1}{v_{p\max} \left(1 - x_p/L_p \right)} dx_p \approx -3 \frac{L_p}{v_{p\max}} \quad (13)$$

Remembering Equation (10), one obtains:

$$t_d \approx \frac{3L_p}{\sqrt{\frac{2E_i}{m_p}}} \quad (14)$$

Through Equations (1) and (14), the working frequency can be derived:

$$f = \frac{1}{t_u + t_d} \quad (15)$$

Finally, using the approximate expression (12) for the velocity v_p , through integration, it is possible to express, as a function of time, the piston position during the downward stroke:

$$x_p \approx L_p \left(1 - 0.05 e^{-\frac{v_{p\max}}{L_p} t} \right) \quad (16)$$

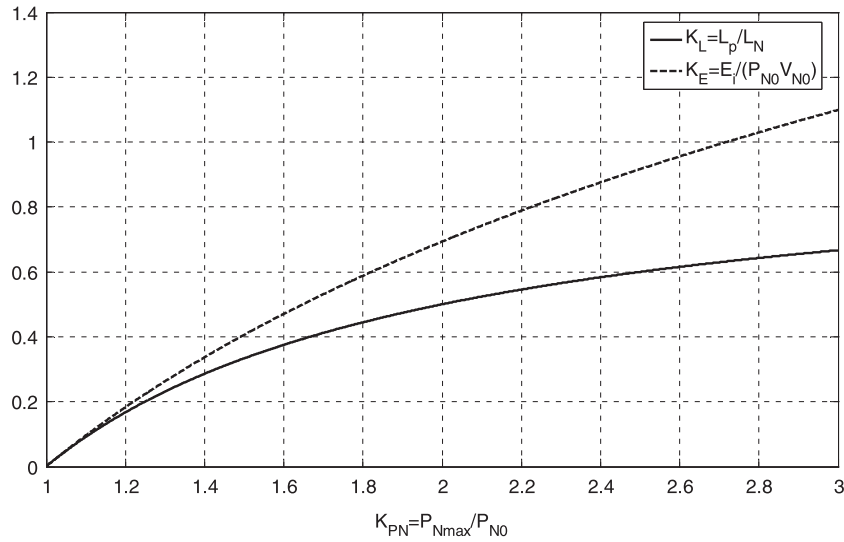


Figure 3. The dimensionless piston stroke K_L and the dimensionless impact energy K_E versus the dimensionless maximum pressure K_{PN} of the nitrogen spring.

5. The dimensionless model

In order to simplify the procedure for functional modelling, some dimensionless quantities are introduced in this section.

From Equation (6), it is possible to express the dimensionless stroke of the piston $K_L = L_p/L_N$ as a function of the maximum dimensionless pressure of the nitrogen spring $K_{PN} = P_{Nmax}/P_{N0}$, P_{Nmax} being the maximum pressure in the spring, reached at the piston maximum stroke $x_p = L_p$:

$$K_L = \frac{L_p}{L_N} = \frac{P_{Nmax}/P_{N0} - 1}{P_{Nmax}/P_{N0}} = \frac{K_{PN} - 1}{K_{PN}} \quad (17)$$

From (10), again as a function of the maximum dimensionless spring pressure K_{PN} , the dimensionless impact energy K_E can be derived:

$$K_E = \frac{E_i}{P_{N0} A_N L_N} = \frac{E_i}{P_{N0} V_{N0}} = \ln K_{PN} \quad (18)$$

The courses of K_L and K_E versus K_{PN} are reported in Figure 3.

Now the velocity gain K_v is introduced, expressed as:

$$K_v = \frac{|v_{pmax}|}{v_{pu}} = \sqrt{\frac{E_i}{E_{pu}}} \quad (19)$$

which consists in the square root of ratio between the impact energy E_i obtainable from the analysed breaker with respect to the impact energy E_{pu} obtainable from the same striker directly connected to the hydraulic supply unit.

The velocity gain allows to define two more dimensionless quantities related to the dynamics of the system. First, the dimensionless working frequency, representing

the ratio between the piston rising time and the whole cycle period:

$$K_f = \frac{t_u}{t_u + t_d} = \frac{f}{1/t_u} = \frac{1}{1 + 3/K_v} \quad (20)$$

and also the ratio between raising and falling times K_t :

$$K_t = \frac{t_u}{t_d} = \frac{K_v}{3} \quad (21)$$

The course of dimensionless frequency K_f and the up/down time ratio K_t versus the gain velocity K_v are traced in Figure 4.

6. The procedure for the functional design

Starting from the relationships of previous sections, a rapid design methodology has been conceived. It is depicted in Figure 5 and is divided into two stages.

In the first stage, the maximum dimensionless pressure of the nitrogen spring K_{PN} and the velocity ratio K_v must be fixed. The choice of initial value of these two parameters is a critical matter and claims for some discussion.

The value of K_{PN} is correlated with the impact energy E_i (see Equation (18)). Therefore, this latter benefits from high values of K_{PN} , once the value of preload energy of the nitrogen spring has been fixed. However, the increasing pressure cannot overcome some limits related to the system safety. Usual values for K_{PN} can be said as 1.3–1.5.

Also, K_v is correlated with the breaker impact energy (see Equation (19)). High values of this parameter correspond to large E_p for a defined hydraulic power unit. However, when hydraulic unit has been defined, increasing values of K_v determine lower working frequencies,

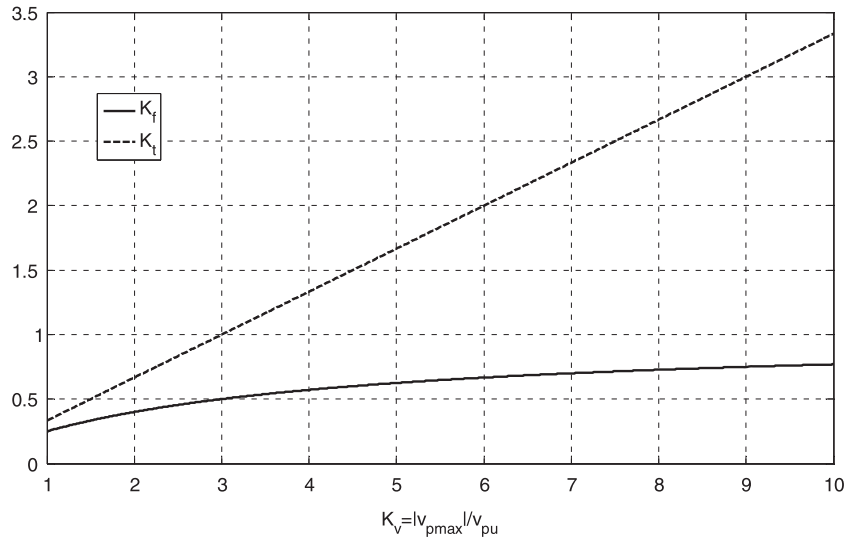


Figure 4. The dimensionless frequency K_f and the up/down time ratio K_t versus the gain velocity K_v .

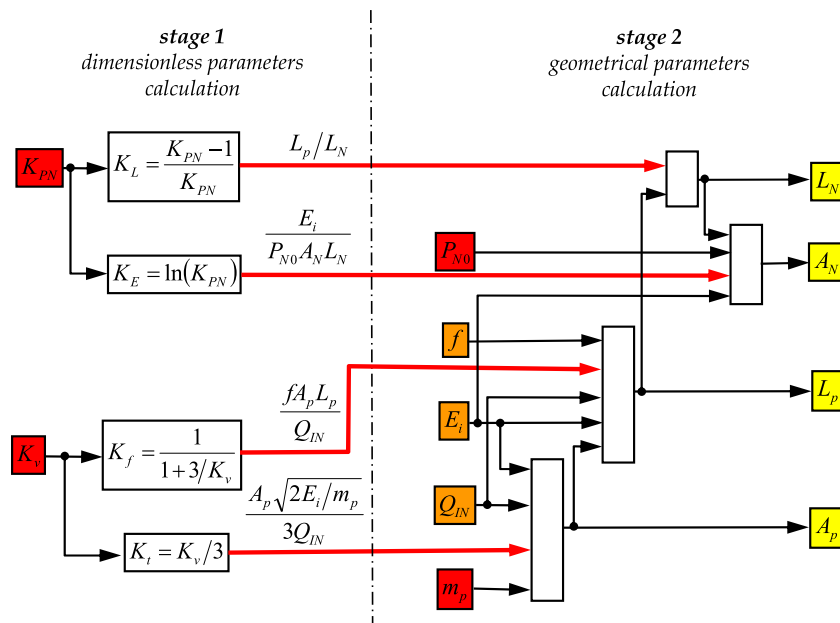


Figure 5. Block scheme of the rapid design process.

as evidenced by in Equations (19) and (20). Also, in this case, the value of K_v will be chosen on the base of a compromise. The order of magnitude for K_v can be said around 10.

Once the initial values of K_{PN} and K_v have been fixed, through Equations (17), (18), (20) and (21), one can calculate the dimensionless stroke K_L , the dimensionless energy K_E , the dimensionless frequency K_f and the up/down time ratio K_t .

In the second stage, the basic geometry of the breaker is determined. First, the designer must impose the performance characteristics, namely: the desired impact energy E_i and the working frequency f , together with the flow rate Q_{IN} of the supply unit. At the same time, it is necessary to choose the initial pressure P_{N0} in the nitrogen spring and a tentative striker mass m_p .

By means of the mathematical relationships of the model, reported in Figure 5, it is then possible to calculate the geometrical parameters of the breaker, as concerns the piston (stroke L_p and active area A_p of the piston) and the nitrogen spring (length L_N and area A_N of the chamber).

7. Experimental validation

Some experimental tests have been carried out with the aim to verify the effectiveness of the rapid design process. The tests are related to a hydraulic breaker with nitrogen spring Vistarini VH160 installed on excavator Bobcat 331.

As concerns instrumentation, the nitrogen pressure P_N has been measured with a pressure transducer Parker

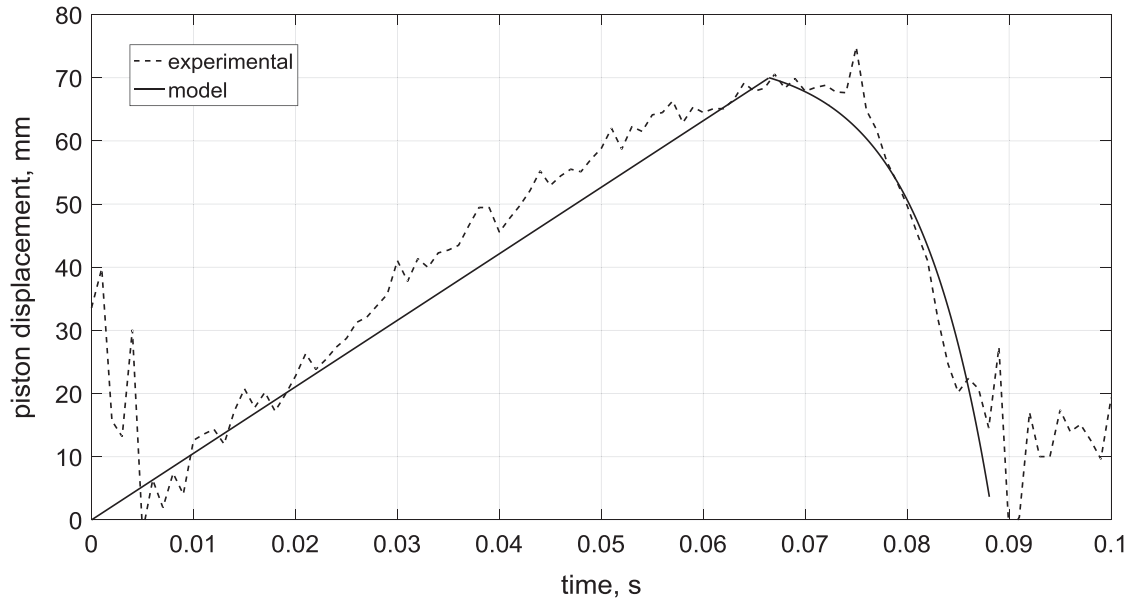


Figure 6. Comparison between the experimental and theoretical displacement of the piston.

PTDVB250 (full scale 100 bar; linearity $\pm 0.05\%$ f.s.; time response 1 ms); the supply flow rate Q_{IN} has been measured with a turbine flow sensor Flo-tech PFM6-60 (range $12 \div 227$ l/min, accuracy $\pm 1\%$ f.s.); and the field signals have been acquired by means of National Instruments Board type DAQPad-6015 (BNC).

In the first step, it has been necessary to validate the mathematical model of the breaker. To do that, starting from the experimental course of the nitrogen spring pressure, the piston position has been evaluated through Equation (6); this allowed in turn to evaluate the experimental velocity and, from its maximum value, the impact energy.

On the other side, the model evaluated the theoretical position of piston in upward stroke assuming uniform linear motion, with velocity v_{pu} expressed by Equation (2); conversely, the theoretical position in downward stroke has been calculated by Equation (16).

Figure 6 reports the course of the piston position as experimentally evaluated and theoretically calculated by the model. The good correspondence as concerns, in particular the maximum values and the average dynamic trend, certifies the validity of the mathematical model.

The experimental tests allowed also to complete the knowledge of the main functional parameters of the breaker, reported in Table 1. In particular, by post-processing the experimental pressure measures, it was possible to obtain the initial nitrogen spring pressure P_{N0} , the maximum nitrogen spring pressure P_{Nmax} and to calculate the dimensionless nitrogen spring pressure K_{PN} . The piston mass m_p was calculated from the drawings of the hammer. The mean up-velocity of the piston v_{pu} and the impact velocity of the piston v_{max} were numerically calculated starting from the experimental displacement of the piston, and consequently the velocity gain K_v and the energy impact E_i were calculated. The experimental

Table 1. The main functional parameters of the real breaker Vistarini VH160.

P_{N0}	$21.0 \cdot 10^5$ Pa	K_v	8.88
P_{Nmax}	$29.0 \cdot 10^5$ Pa	f	12.6 Hz
K_{PN}	1.38	E_i	413 J
v_{pu}	1.05 m/s	Q_{IN}	$5.66 \cdot 10^{-4}$ m ³ /s
v_{max}	9.33 m/s	m_p	9.5 kg

Table 2. Theoretical and real design parameters for a nitrogen spring breaker Vistarini VH160.

	Theoretical value (mm)	Real value (mm)	Difference %
Φ_p	64.2	65.5	-1.9
L_p	62.3	62.0	+0.5
Φ_N	58.6	60.0	-2.3
L_N	225.8	304.1	-34.7

tests permitted also to measure the breaker working frequency f and the supply pump flow rate Q_{IN} .

This enabled to apply the rapid design procedure described in section 3.3. Starting from the data of Table 1, which constitute the design parameters, the geometrical characteristics of the breaker VH160 have been calculated in the way described above.

Table 2 reports the values of the four design parameters both as evaluated by the theoretical procedure and as detected from the real breaker. The third column reports the per cent difference. There is a very good correspondence as regards the piston and the nitrogen spring area; the volume of the spring is quite underestimated, but in the complex, the effectiveness of the rapid design procedure can be confirmed.

A further validation of the methodology for rapid designing was made on another breaker model, the Vistarini VHX331; in this case, starting from product catalogue data (working frequency f , impact energy E_i and supply pump flow rate Q_{IN}), manufacturer data (initial P_{N0} and maximum P_{Nmax} nitrogen spring pressure)

Table 3. The main functional parameters of the real breaker Vistarini VH331.

P_{N0}	22.0 10^5 Pa	K_v	10.12
P_{Nmax}	29.0 10^5 Pa	f_v	13.2 Hz
K_{PN}	1.32	E_i	785 J
v_{pu}	1.22 m/s	Q_{IN}	$1.25 \cdot 10^{-3}$ m ³ /s
v_{max}	12.35 m/s	m_p	10.3 kg

Table 4. Theoretical and real design parameters for a nitrogen spring breaker Vistarini VH331.

	Theoretical value (mm)	Real value (mm)	Difference %
Φ_p	83.0	70.0	+15.7
L_p	71.0	68.0	+4.2
Φ_N	74.7	60.0	+19.7
L_N	294.2	303.1	-3.0

and data taken from drawings (mass and dimensions). The mean up-velocity piston v_{pu} was calculated using Equation (2), knowing the pump flow rate Q_{IN} and the piston area A_p . The impact velocity of the piston v_{pmax} was calculated using the Equation (10), knowing the catalogue impact energy E_i and the piston mass m_p . Finally, starting from these data, the dimensionless nitrogen

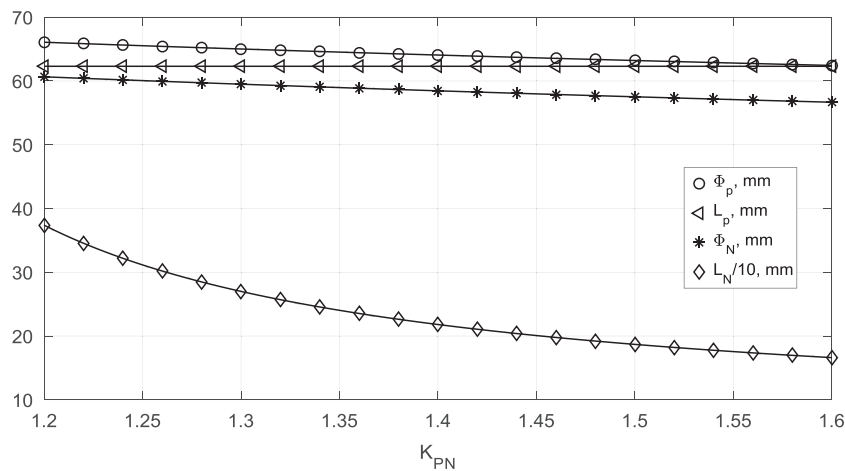
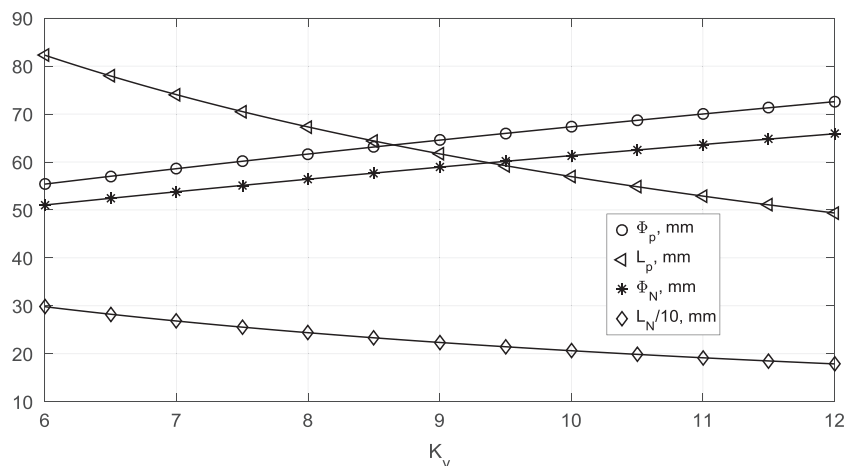
spring pressure K_{PN} and the velocity gain K_v were calculated (Table 3).

The methodology for rapid designing, applied to the Vistarini VH331 hammer, starting from the data of Table 3, permitted to calculate the main geometrical characteristics of the breaker and to compare them to the real values (Table 4).

Also, in this case, in the complex, the effectiveness of the rapid design procedure can be confirmed. It must be indeed taken into account that the methodology allowed to calculate the main geometrical parameters of the Vistarini VH331 hydraulic breaker with discrete approximation, although starting from necessarily uncertain initial data.

8. Influence of the dimensionless parameters on the functional parameters

The procedure of the functional design, described in Section 6 and resumed in Figure 5, provides that the dimensionless parameters K_{PN} and K_v must be chosen a priori. In order to highlight the influence of these parameters on the functional geometrical dimensions of the

**Figure 7.** Design parameters of the nitrogen spring breaker Vistarini VH160 versus the dimensionless parameter K_{PN} .**Figure 8.** Design parameters of the nitrogen spring breaker Vistarini VH160 versus the dimensionless parameter K_v .

hammer, the rapid design procedure has been applied assuming the design parameters collected in Table 1, and varying the values of K_{PN} and K_v . Figure 7 reports the trend of the design parameters of the nitrogen spring breaker Vistarini VH160 versus the dimensionless nitrogen spring pressure K_{PN} .

Figure 8 shows the behaviour of the design parameters of the nitrogen spring breaker Vistarini VH160 versus the dimensionless velocity ratio K_v .

From this analysis, it is clear that the nitrogen spring height L_N depends strongly on the dimensionless nitrogen spring pressure K_{PN} , while all the design parameters (L_N, L_p, Φ_N, Φ_p) are heavily influenced by the velocity gain K_v . Therefore, high errors on the calculation of any of the geometrical functional design parameters can be caused by wrong estimation of the dimensionless parameters K_{PN} and K_v , as well as by neglecting friction and other possible losses.

9. Conclusions

In this work, first, a simplified mathematical model of a hydraulic breaker with nitrogen spring has been realised; then, the model has been used as the base of a procedure for the rapid design of new breakers. The procedure supports the designer in the definition of some parameters which are very influent on the dynamical performance of the breaker, like impact energy and working frequency.

Both the mathematical model and the rapid design procedure have been experimentally verified. The model has proved capable of simulating with good correspondence the dynamical course of the piston position during the working cycle. The design procedure allowed to foresee the dimensions of two-piston striker and nitrogen spring with a maximum difference of 34% with respect to the real dimensions of a commercial breaker.

In conclusion, the procedure was capable to individuate with acceptable accuracy a direct correlation between the main operating performances and some critical design parameters, and therefore could be adopted as a useful support in the first step of a new breaker development.

Nomenclature

A lowercase p indicates relative pressures; an uppercase P indicates absolute pressures. In the notation table, only absolute pressures are reported.

A_N	nitrogen spring area
A_p	piston area
E_i	impact energy
E_{pu}	impact energy of a hydraulic striker
f	working frequency
K_f	dimensionless working frequency
K_L	dimensionless piston stroke
K_{PN}	dimensionless nitrogen spring pressure
K_t	up-down time ratio
K_v	velocity gain
L_N	nitrogen spring height
L_p	piston stroke
m_p	piston mass
P_N	nitrogen spring pressure
P_{NO}	initial nitrogen spring pressure
P_s	supply pressure

Q_{IN}	supply pump flow rate
t_d	down time (falling time)
t_u	up time (rising time)
V_N	nitrogen spring actual volume
V_{NO}	nitrogen spring initial volume
v_p	piston velocity
v_{pmax}	impact piston velocity
v_{pu}	mean up-velocity of the piston
x_p	piston position
Φ_N	nitrogen spring diameter
Φ_p	piston diameter

subscripts	
0	initial condition
N	nitrogen
i	impact
p	piston
u	up
d	down

Disclosure statement

No potential conflict of interest was reported by the authors.

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