# ANALYSIS AND CONTROL OF A WATER HYDRAULIC MANIPULATOR FOR ITER DIVERTOR REMOTE MAINTENANCE

Likui Zhai<sup>1</sup>, Tapio Virvalo<sup>1</sup>, Jouni Mattila<sup>1</sup> and Hannu Saarinen<sup>1,2</sup>

<sup>1</sup>Department of Intelligent Hydraulics and Automation, Tampere University of Technology, Tampere, Finland <sup>2</sup>VTT Technical Research Centre of Finland, Tampere, Finland likui.zhai@gmail.com, tapio.virvalo@gmail.com, jouni.mattila@tut.fi, hannu.saarinen@vtt.fi

#### Abstract

This paper focuses on the analysis and control of a water hydraulic manipulator, which is specific for the International Thermonuclear Experimental Reactor (ITER) cassettes' (each weighing 10 tonnes) maintenance tasks. The manipulator comprises a closed-chain main body and an open-chain end-effector. Following a systematic way of analyzing differential kinematics and vibration modes, it is revealed that from a control point of view the manipulator faces two main restrictions. The first one is that the closed-chain structure degrades tracking performances, rising from kinematic coupling. Secondly, as the end-effector drives a very high inertial load instead of a gravitational load, small actuators are used, resulting in low system natural frequency and damping. To solve the first issue, a kinematic model-based decoupling controller is designed. Moreover, to improve the steady-state accuracy in spite of low frequency and damping, acceleration feedback is adopted, achieving higher damping and position loop gains. Experimental results show that decoupling controller brings five times smaller tracking errors, while acceleration feedback controller reaches three times better accuracies than proportional controller. This study also confirms that in spite of using commercially available water hydraulic components, the achieved positioning accuracies and dynamic behavior are competitive with oil hydraulics.

Keywords: hydraulic manipulator, coupling, kinematic model-based decoupling, vibration mode analysis, ITER

## **1** Introduction

ITER is a large-scale scientific experiment aiming to demonstrate the scientific and technological feasibility of fusion energy for commercial energy production (Rebut, 1995). The divertor area of ITER comprises 54 rail-mounted cassettes. Due to the erosion of the plasma-facing components and possible need for improving the design of critical items, these cassettes must be periodically replaced and refurbished every 3-4 years during ITER's 20 years operational time (Palmer et al., 2005). Each cassette has an estimated mass of 10 tonnes with an external dimension of 3.5 m length by 2.0 m height by 0.8 m width. To execute these cassettes remote maintenance tasks, one of the most competitive solutions is to utilize the advantages of hydraulics (high power density, large force/torque, high load stiffness) together with pure water as the

pressure medium (nonflammable, chemically neutral and irradiation resistant) (Raneda et al., 2003).

The installation (or removal) of the cassettes has a motion characteristic that the position change is mainly in a vertical plane, while the orientation varies mostly in a near horizontal plane. Therefore, the designed water hydraulic manipulator comprises a closed-chain main body (so-called Cassette Multi-functional Mover, CMM) and an open-chain end-effector (so-called Second Cassette End-Effector, SCEE) (see Fig. 1). The CMM provides lifting and tilting motions in the vertical plane, with its closed-chain structure improving system stiffness. The SCEE, which consists of cantilever (CRO) and hook-plate (HRO) rotational joints, is mainly devoted to change the cassette's orientation. Lastly, with the aid of electric motor drive, CMM may radially travel on the top of the maintenance tunnel rails.

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Fig. 1: CMM/SCEE and a second cassette

During the installation (or removal) process, in order to avoid any collisions to the surroundings, very high steady-state and follow-up accuracies are desired. The typical desired accuracies are  $\pm 0.07$  degree in joint space. Another requirement is to have reasonably fast response, so a bandwidth of 0.5 Hz is selected.

Like electrical robot manipulators, controlling hydraulic manipulators may use decentralized or centralized control scheme depending on the applications. When the manipulators needs to be controlled at high speed and large bandwidth, the dynamic coupling effects between joints are not negligible, whereas centralized control methods, such as computed torque feedforward control (Wang et al., 2009), inverse dynamics control (Plummer, 2007: Davliakos and Papadopoulos, 2008) and adaptive control (Sirouspour and Salcudean, 2001) have been widely studied. On the other hand, if the manipulators work at low speed and small bandwidth, decentralized control could be adopted, which regards the manipulator as n independent system (n joints) and coupling effects as disturbances (Gunnarsson and Krus, 1994; Edge and Gomes de Almeida, 1995; Gizatullin and Edge, 2006; Guo et al., 2008). For this cassette installation (or removal) process, the desired bandwidth is 0.5 Hz and every joint receives smooth trajectory input of low speed (< 1 deg/s). Therefore, decentralized control approach is utilized to simplify controller design.

In order to analyze how the each joint vibrates and at which natural frequencies, vibration modes analysis becomes important. Linjama and Virvalo (1999) have analyzed the vibration modes of a flexible hydraulic crane to assist controller design. Plummer (2004) has used the vibration modes analysis to optimize the design of a parallel manipulator. In this paper, vibration modes analysis shows CRO joint exhibits very low natural frequency which restricts the desired accuracy. Therefore, to improve the steady-state accuracy, acceleration feedback is adopted, achieving higher damping and position loop gains.

The tracking performances of closed-chain manipulators are very often limited by the kinematic coupling. Besides individual speed feedforward, many researchers have tried to add integrator term to improve the tracking accuracy (Fales, R. 2004; Rokala, 2007). However, this may lead to hunting problem (Virvalo, 2001). In this paper, a kinematic model-based decoupling controller is proposed and tested.

Despite the aforementioned control problems, using water as pressure medium leads to additional issues. So far the choice for water hydraulic components is very limited, and their characteristics are usually worse than those of oil hydraulics. Therefore, this study is also important to (experimentally) confirm that the designed water hydraulic manipulator is competitive with their oil hydraulic counterpart.

Because the manipulator moves at low speed and the motion of lift-tilt mechanism is orthogonal to that of CRO-HRO, for simplicity of later analysis they are regarded as two independent 2DOF systems (see Fig. 2). The rest of the paper is organized as follows: Section 2 presents the kinematic analysis which reveals kinematic coupling in the closed-chain structure. Dynamic model is derived in section 3 and then used for static force and vibration modes analysis. Section 4 introduces the test system and verifies the vibration modes analysis by open loop velocity responses. The design and experimental results of both feedback and feedforward controllers are presented in section 5. The conclusions are drawn in the last section.

### 2 Kinematic Analysis

Figure 2 presents a schematic diagram of the studied manipulator with defined link frames, following a typical convention (Sciavicco and Siciliano, 2000). The Denavit-Hartenberg parameters are specified in Table 1, where  $\theta_i$  denotes the manipulator joint angel between two incident normals of a joint axis,  $a_i$  – the length of link *i*,  $\alpha_i$  – twist angle between two adjacent joint axes,  $d_i$  – translational distance between two incident normals of a joint axis (Tsai, 1999).

 Table 1: Denavit-Hartenberg
 parameters
 of

 CMM/SCEE

Link	<i>a</i> <sub>i</sub> [m]	$\alpha_{\rm i}$ [rad]	$d_{\rm i}$ [m]	$\theta_{\rm i}$ [rad]
1	0	0	$d_1$	0
2	<i>-a</i> <sup>1</sup> (-0.165)	π/2	$d_{1v}(0.795)$	$3\pi/2 + \theta_2$
3	$a_2(1.202)$	0	0	$\theta_3$
4	<i>a</i> <sub>3</sub> (0.701)	-π/2	- <i>d</i> <sub>4</sub> (-0.026)	$\theta_4$
5	$a_4 (0.950)$	0	0	$\theta_5$

The joint-to-Cartesian direct kinematic transformation can be constructed from the homogenous transformation matrices by matrix multiplication

$$y = h_1(\theta) = A_1^0(d_1)A_2^1(\theta_2)A_3^2(\theta_3)A_4^3(\theta_4)A_5^4(\theta_5)$$
(1)



Fig. 2: Schematic diagram of the CMM/SCEE

where y – the position vector in Cartesian coordinate,  $A_i^{i-1}$  - the homogenous transformation matrix

$$\boldsymbol{\mathcal{A}}_{i}^{i-1}(\boldsymbol{\theta}_{i}) = \begin{bmatrix} c\boldsymbol{\theta}_{i} & -s\boldsymbol{\theta}_{i}c\boldsymbol{\alpha}_{i} & s\boldsymbol{\theta}_{i}s\boldsymbol{\alpha}_{i} & \boldsymbol{a}_{i}c\boldsymbol{\theta}_{i} \\ s\boldsymbol{\theta}_{i} & c\boldsymbol{\theta}_{i}c\boldsymbol{\alpha}_{i} & -c\boldsymbol{\theta}_{i}s\boldsymbol{\alpha}_{i} & \boldsymbol{a}_{i}s\boldsymbol{\theta}_{i} \\ 0 & s\boldsymbol{\alpha}_{i} & c\boldsymbol{\alpha}_{i} & \boldsymbol{d}_{i} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(2)

The notations  $s\theta_i$  and  $c\theta_i$  are the abbreviations for  $\sin\theta_i$  and  $\cos\theta_i$ .

In a compact form, the differential kinematic equation can be written as

$$\boldsymbol{v} = \boldsymbol{J}(\boldsymbol{\theta})\dot{\boldsymbol{\theta}} \tag{3}$$

where J - the joint-to-Cartesian Jacobian matrix,  $\dot{\theta}$  - the joint velocity vector, and v – the velocity vector in Cartesian coordinate.

Similarly, the joint-to-actuator transformation and corresponding differential kinematic equation can be expressed as

$$\boldsymbol{z} = \boldsymbol{h}_2(\boldsymbol{\theta}) \tag{4}$$

$$\dot{z} = A_{\rm h}(\theta) \dot{\theta} \tag{5}$$

where  $A_h$  - the joint-to-actuator Jacobian matrix, z - the cylinder length vector, and  $\dot{z}$  - the cylinder velocity vector.

Detailed kinematic equations for both lift-tilt and CRO-HRO 2DOF systems are presented in the appendix.

From Eq. 21 in the appendix, the tilt joint velocity  $\dot{\theta}_3$  is a function of both lift cylinder velocity  $\dot{z}_2$  and tilt cylinder velocity  $\dot{z}_3$ 

$$\dot{\theta}_{3} = \frac{1}{A_{hLT22}} \dot{z}_{3} - \frac{A_{hLT21}}{A_{hLT11}A_{hLT22}} \dot{z}_{2}$$
(6)

In other words, tilt joint velocity is affected by both tilt and lift cylinder velocities. This effect rises from the kinematic coupling of the closed-chain structure in the lift-tilt 2DOF system. This coupling will decrease the tracking performance of tilt joint which is discussed in section 5.2 and 5.3. By comparison, no such kinematic coupling exists in the open-chain CRO-HRO 2DOF system.

## **3** Dynamic Analysis

#### 3.1 Dynamic Motion Equation

Neglecting joint friction and disturbance terms, the dynamic equation of the mechanical mechanism can be derived based on Lagrange's formulation

$$\boldsymbol{M}(\boldsymbol{\theta})\boldsymbol{\ddot{\theta}} + \boldsymbol{V}(\boldsymbol{\theta},\boldsymbol{\dot{\theta}}) + \boldsymbol{G}(\boldsymbol{\theta}) = \boldsymbol{\tau} = \boldsymbol{A}_{\mathrm{h}}^{\mathrm{T}}\boldsymbol{F}_{\mathrm{h}}$$
(7)

where M is the inertia matrix, V is the matrix of centrifugal and Coriolis terms and G is the gravitational torque vector (Sciavicco and Siciliano, 2000). Centrifugal and Coriolis forces are neglected in this study, because the angular velocities are rather low.

The inertia matrix is a sum of individual inertia matrices

$$\boldsymbol{M}(\boldsymbol{\theta}) = \sum_{i=1}^{n} m_{l_i} \boldsymbol{J}_{P}^{(l_i)T} \boldsymbol{J}_{P}^{(l_i)}$$
(8)

The vector of generalized toque is expressed as

$$\boldsymbol{G}(\boldsymbol{\theta}) = \sum_{i=1}^{n} m_{l_i} \boldsymbol{g}_0^{\mathrm{T}} \frac{\partial \boldsymbol{p}_{l_i}}{\partial \theta_i}$$
(9)

For each 2DOF system, the derived dynamic equation terms are presented in the appendix.

### 3.2 Effect of Gravitational Torque on the Lift-Tilt 2DOF System

The non-zero gravitational torque in the lift-tilt 2DOF system affects both steady state accuracy  $\Delta y$  and actuator space velocity gain  $K_{qa cyl}$ .

Figures 3 and 4 show the static actuating force on the lift and tilt cylinder in the whole working range. The force variations are 28 kN ( $115 \sim 143$  kN) for lift joint and 61 kN ( $138 \sim 199$  kN) for tilt joint. These results are used for tuning offsets of the servo valves to compensate gravitational torque.



Fig. 3: Static force on lift cylinder



Fig. 4: Static force on tilt cylinder

The velocity gains in actuator space are strongly

affected by gravitational torque; in this case  $K_{qa_cyl}$  in retraction direction is around 1.4 times bigger than that of extension direction for both joints. Even in the same direction the maximum variation of  $K_{qa_cyl}$  is found to be as much as 11.5 % for lift joint and 9.2 % for tilt joint.

#### 3.3 Vibration Mode Analysis

The vibration mode consists of the mode shape, which shows how the system vibrates, and the corresponding natural frequency. The vibration modes for the studied hydraulic manipulator are calculated by only considering the hydraulic fluid compressibility, ignoring linkage flexibility and joint clearances.

Thus the undamped eigenvalue problem of free vibration is analyzed; utilizing the linear model of the mechanism (Linjama, 1998):

$$\boldsymbol{M}_{0}\Delta\boldsymbol{\theta} + \boldsymbol{K}_{0}\Delta\boldsymbol{\theta} = 0 \tag{10}$$

The notations  $M_0(\theta_0) = M_0$ ,  $A_{h0}(\theta_0) = A_{h0}$  are adopted to clarify the equations.

The stiffness matrix  $\mathbf{K}_0$  is expressed as

$$\boldsymbol{K}_{0} = \boldsymbol{A}_{h0}^{T} \operatorname{diag}(\boldsymbol{K}_{hj}) \boldsymbol{A}_{h0}$$
(11)

where diag( $K_{hj}$ ) is an  $n \times n$  diagonal matrix of hydraulic spring constants (Merritt, 1967).

The natural frequencies are derived by

$$\omega_{k} = \sqrt{\lambda_{k} \{\boldsymbol{M}_{0}^{-1} \boldsymbol{K}_{0}\}}$$
(12)

where  $\lambda_k$ {·} is the *k*:th sorted eigenvalue of {·} and  $\omega_k$  is the *k*:th natural frequency. The nonlinearity of the mechanism and actuator dynamics cause natural frequencies to depend strongly on the position and orientation of the manipulator. Figures 5 and 6 illustrate the first and second natural frequencies of the lift-tilt 2DOF system, where the lowest natural frequency is around 5 Hz. The first and second natural frequencies of the CRO-HRO 2DOF system are illustrated in Fig. 7 and 8, with lowest natural frequency around 1 Hz.



Fig. 5: First natural frequencies of lift-tilt 2DOF system



Fig. 6: Second natural frequencies of lift-tilt 2DOF system



Fig. 7: First natural frequencies of CRO-HRO 2DOF system



Fig. 8: Second natural frequencies of CRO-HRO 2DOF system

## 4 Test System and Open-Loop Tests

### 4.1 Test System

A photograph of the experimental setup is given in Fig. 9, where CMM/SCEE carries a 10 tonnes dummy load. The main specifications are listed as follows:

- Supply pressure  $p_{\rm S} = 140$  bar
- Servo valve: Moog 30-417
   Nominal flow Q<sub>N</sub> 6.9 l/min with the nominal pressure drop 35 bar /control notch
   Rated current u<sub>max</sub> = 10 mA

Hysteresis < 3 %

Null point leakage < 4 % ( $Q_N$ ,  $\Delta p_N$ )

Pressure gain  $K_{pg} = (0.4 \times p_S) / (1.2 \% \times u_{max})$ 90° bandwidth > 100 Hz

- Lift cylinder 125 / 80-430
- Tilt cylinder 125 / 80-470
- CRO cylinder 63 / 40-282
- HRO cylinder 63 / 40-395
- Resolver resolution: 0.0055 deg (16 bit)
- Sampling time: 2 ms





### 4.2 Open Loop Tests

Hydraulic position systems are generally described by a third order model with parameters natural frequency  $\omega_n$ , damping ratio  $\delta_n$  and velocity gain  $K_{qa}$ ; therefore the transfer function between valve input and velocity output is of second order. Furthermore, these three system parameters can be identified by analyzing the open loop velocity responses of step valve input. Figures 10 and 11 present the open loop test results of tilt and lift joints where  $\theta_{tilt}$ =-15 deg,  $\theta_{lift}$ = 10 deg,  $\theta_{CRO}$ = 0 deg and  $\theta_{HRO}$ = 0 deg.



Fig. 10: Open loop velocity responses of tilt joint



Fig. 11: Open loop velocity responses of lift joint

Similarly the open loop test results of CRO and HRO joints are shown in Fig. 12 and 13 where  $\theta_{\text{tilt}}$ =-15 deg,  $\theta_{\text{lift}}$ = 10 deg,  $\theta_{\text{CRO}}$ = 40 deg and  $\theta_{\text{HRO}}$ = -20 deg.



Fig. 12: Open loop velocity responses of CRO joint



Fig. 13: Open loop velocity responses of HRO joint

For the lift-tilt 2DOF system by comparing Fig. 5 and 6 with Fig 10 and 11, it can be seen that the velocity responses of the tilt joint have a combination of the first and second vibration modes, and is dominated by the first natural frequency. The lift joint responses are mostly dominated by the second natural frequency. Similarly, for the CRO-HRO 2DOF system, Fig. 12 and 13 show that the first natural frequency is the dominating frequency for the CRO joint, while the second one is for the HRO joint. When the open loop tests are carried out at other positions and orientations, the same conclusion can be still be drawn with varied natural frequencies.

## 5 Controller Design and Experimental Results

### 5.1 System Requirements

The smallest clearance between the cassette and the service port (floor and ceiling) is about 20 mm, requiring a very high positioning accuracy (typical desired accuracy  $\leq \pm 0.07$  deg in joint space).

One practical performance specification for this kind of position feedback system may include a desired bandwidth  $\omega_{BW}$ , an allowable steady-state and tracking errors  $\Delta y$  and a peak magnitude of closed loop frequency response  $M_r$ . For this application, the specifications are:  $\omega_{BW} \ge 3$  rad/s,  $\Delta y \le 0.05$  deg and  $M_r \le 1$  dB.

The steady state position accuracy  $\Delta y$  is mostly affected by valve hysteresis *H*/100 (< 3 %) and external force *F*<sub>L</sub>. The desired steady state accuracy  $\Delta y$  defines the desired position feedback gain *KP*<sub>des</sub>

$$KP_{des} = u_{max} \cdot \left(\frac{H}{100 \cdot \Delta y} + \frac{F_{L}}{20(A_{1} + A_{2})p_{s} \cdot \Delta y}\right)$$
(13)

where  $u_{\text{max}}$  denotes rated valve input,  $A_1$ ,  $A_2$  - the areas of cylinder piston and rod sides,  $p_s$  – supply pressure. In this case, the estimated  $KP_{\text{des}}$  is 3 mA/deg.

Regarding position system as a linear third order transfer function, a rule of thumb to estimate position feedback gain KP with  $M_r \leq 1$  dB is

 $KP = 2 \cdot \delta_n \cdot \omega_n / (3K_{qa})$  (Virvalo and Mattila, 2007). The estimated KP for the four joints are  $KP_{tilt} = 13$  mA/deg,  $KP_{lift} = 18$  mA/deg,  $KP_{CRO} =$ 1.6 mA/deg,  $KP_{HRO} = 15$  mA/deg. Comparing them with the desired position feedback gain  $KP_{des}$ , it is foreseen that it is relatively easy to achieve high steady-state accuracy for lift, tilt and HRO joints, but not for CRO joint.

### 5.2 Controller Design for Lift-Tilt 2DOF System

Based on the estimation in the previous section, phase lag P-controller (or phase lag compensator) is selected as the lift and tilt joint controller. The design methods are presented as follows.

$$C_{i}(s) = \frac{KP_{i}}{\tau_{i}s + 1}$$
  

$$\tau_{i} = 2 / \omega_{ni,min}$$
  

$$KP_{i} = 1 / (K_{qai} \cdot 5 \cdot \tau_{i})$$
(14)

In this case, the lowest natural frequency is chosen to be 3.5 Hz for both controller design of Eq. 14, which significantly decreases the coupling effects and still achieves desired steady-state accuracy. The tuned position loop gains for both joints are listed in Table 2.

Table 2: Main controller gains for four joints

	KP <sub>p</sub> [mA/deg]	KP <sub>n</sub> [mA/deg]	$K_{\rm a}$ [mA·s <sup>2</sup> /deg]
HRO	4.2	5.2	0
CRO	3.2	3.6	0.013
Tilt	40	17	0
Lift	24	10	0

Step responses of both joints are presented in Fig. 14 and 15. The steady state position errors are less than  $\pm 0.01$  deg for both joints.



Fig. 14: Position error responses of tilt joint (Phase lag P-controller, step)

To improve the tracking performance, individual velocity feedforward gains are tuned for lift and tilt joints,  $P_{dlift} = 9.6 \text{ mA·s/deg}$ ,  $P_{dtilt} = 21 \text{ mA·s/deg}$ . First

the lift joint is kept stationary and tracking performances of the tilt joint are analyzed ( $\dot{\theta}_{\text{lift}} = 0$  deg/s,  $\dot{\theta}_{\text{tilt}} = \pm 0.05$  deg/s). Fig 16 shows the position and position error responses of tilt joint. It can be seen that the steady state error is very small (< 0.01 deg) and tracking errors are less than  $\pm 0.025$  deg (velocity/tracking error = 2 deg/s/deg). Steady state error of lift joint is also very small (< 0.01 deg), and the motion of tilt joint has no effect on lift joint.



Fig. 15: Position error responses of lift joint (Phase lag P-controller, step)



Fig. 16: Position and position error responses of tilt joint (lift stationary)

Then tilt angle is kept stationary and the tracking performances of both joints are analyzed ( $\theta_{\text{lift}} = \pm 0.1$ deg/s,  $\theta_{\text{tilt}} = 0$  deg/s). Figures 17 and 18 show the position and position error responses of lift and tilt joints. It can be seen that the tracking errors are less  $\pm 0.03$ deg (velocity/tracking error than 3.3 deg/s/deg) for lift joint, however, the tracking errors of tilt joint are as big as  $\pm$  0.1 deg (velocity/tracking error = 1 deg/s/deg). The reason of this is the kinematic coupling rising from the closed-chain structure (see Eq. 5 in section 2). To improve the follow-up accuracies of the tilt joint, a kinematic model based-decoupling controller is designed in the next section.



**Fig. 17:** Position and position error responses of lift joint (coupled tracking)



Fig. 18: Position and position error responses of tilt joint (coupled tracking)

### 5.3 Kinematic Model-based Decoupling Controller Design for Lift-Tilt 2DOF System

A simplified model for hydraulic cylinder drive is that cylinder velocity is proportional to valve input:

$$\dot{z}_2 = K_{qa\_cyl2} \cdot u_2$$

$$\dot{z}_3 = K_{ga\_cyl3} \cdot u_3$$
(15)

where  $K_{qa_{cyl}}$  is the cylinder velocity gain in actuator space.

Lift joint (rotational) velocity  $\theta_2$  is a function of lift cylinder velocity  $\dot{z}_2$  and its joint geometry

$$\dot{\theta}_2 = \frac{1}{A_{\text{hLT11}}} \dot{z}_2 \tag{16}$$

From Eq. 5, 15 and 16, it can be derived that

$$\dot{\theta}_{3} = \frac{1}{A_{\rm hLT22}} K_{\rm qa\_cyl3} \cdot u_{3} - \frac{A_{\rm hLT21}}{A_{\rm hLT22}} \dot{\theta}_{2} \tag{17}$$

Therefore, to eliminate the coupling term in Eq. 17, a model-based decoupling controller should be defined as

$$u_{3} = C_{3} \cdot \Delta \theta_{3} + \frac{A_{\text{hLT21}}}{K_{\text{qa\_cyl3}}} \dot{\theta}_{2}$$
(18)

where the first term in Eq. 18 is the position controller for tilt joint (in this case a phase-lag P-controller), the second term denotes the decoupling term ( in this case velocity feedforward from lift joint). Furthermore, when cylinder velocity gain  $K_{qa\_cyl3}$  is assumed to be constant, the decoupling term depends only on the kinematic parameters  $A_{hLT21}$ , which is derived from the kinematic model of Eq. 21.

With this kinematic model-based decoupling controller in Eq. 18, again, tilt angle is kept stationary and the tracking performances of both joints are analyzed  $(\dot{\theta}_{\text{lift}} = \pm 0.1 \text{ deg/s}, \dot{\theta}_{\text{tilt}} = 0 \text{ deg/s})$ . Figures 19 and 20 show the position and position error responses of both joints. It can be seen that the tracking errors are less than  $\pm 0.03$  deg for lift joint (velocity/tracking error = 3.3 deg/s/deg), and the tracking errors of tilt joint are less than  $\pm 0.02$  deg (velocity/tracking error = 5 deg/s/deg), which are 5 times smaller than the coupled case in Fig. 18.



Fig. 19: Position and position error responses of lift joint (decoupled tracking)



Fig. 20: Position and position error responses of tilt joint (decoupled tracking)

#### 5.4 Controller Design for CRO-HRO 2DOF System

Based on the estimation in section 5.1, phase lag controller can still be applied to HRO joint, however, the available position open loop gain K of CRO joint is limited by the rather low natural frequency (1 Hz). To increase the open loop gain K, one effective way is to increase the damping ratio  $\delta_n$  using acceleration feedback  $K_a$  (as shown in Fig. 21).



Fig. 21: Hydraulic actuator model with acceleration feedback

The effective damping ratio with acceleration feedback is expressed as

$$\delta = \delta_{\rm n} + \frac{K_{\rm qa} \cdot K_{\rm a} \cdot \omega_{\rm n}}{2} \tag{19}$$

In this case, the effective damping ratio is tuned to be 0.5, and the corresponding position loop gain is increased twice.

The chosen lowest natural frequency for HRO phase lag P-controller design is 3 Hz, which can significantly decrease the coupling effects and still achieve desired steady-state accuracy. The controller gains for CRO and HRO joints are listed in Table 2.

The step responses of CRO joint with proportional controller and acceleration feedback controller are presented in Fig 22. It can be seen that the steady-state error of P-controller exceeds  $\pm$  0.05 deg. By contrast, acceleration feedback controller achieves faster responses and three times better accuracies ( $\leq \pm 0.015$  deg).



Fig. 22: Position error responses of CRO joint (P- and acceleration feedback controller, step input)

The step responses of HRO joint with phase lag P-controller are presented in Fig 23. The steady state position errors are less than  $\pm 0.01$  deg.

To improve the tracking performance individual velocity feedforward gains are tuned for CRO and

HRO joints,  $P_{dCRO} = 1.6$  mA·s/deg,  $P_{dHRO} = 2.1$  mA·s/deg. Figures 24 and 25 show the tracking performances of both joints with sinusoidal inputs ( $\bar{v} = 0.3$  deg/s)



**Fig. 23:** Position error responses of HRO joint (*P*-controller, step)



Fig. 24: Position and position error responses of CRO joint (Sine wave tracking)



Fig. 25: Position and position error responses of HRO joint (Sine wave tracking)

The tracking errors of CRO joint are less than  $\pm 0.03$  deg (velocity/tracking error = 10 deg/s/deg),

while the errors are less than  $\pm$  0.05 deg for HRO joint (velocity/tracking error = 7.5 deg/s/deg).

## 6 Conclusion

Decentralized approach is used for individual joint controller design, resulting in phase lag P-controllers for the lift, tilt and HRO joints and acceleration feedback controller for the CRO joint. The performances of corresponding controller design are evaluated by step and waveform inputs. Due to the kinematic coupling effect of lift joint, poor tracking performance is observed in tilt joint. Consequently, a model-based decoupling controller is designed and tested, achieving five times smaller tracking errors. For each joint, the achieved steady state accuracy is better than  $\pm 0.02$  deg, and follow-up accuracy is better than  $\pm\,0.05$  deg. In the ideal case (no manufacturing tolerances, no uncertainties in deflections), ± 5 mm positioning accuracy can be reached at the farthest point of the cassette in Cartesian space. Therefore, this study confirms that in spite of using commercially available water hydraulic components, the achieved positioning accuracies and dynamic behavior are competitive with their oil hydraulic counterpart.

Currently the study of fault tolerant control of this manipulator is being carried out. The durability of crucial water hydraulic components, such as servo valve, is also important and needs to be tested in the future. At very low speed, the nonlinear friction force causes stick-slip in cylinder motion, which may need friction modelling and compensation.

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## Nomenclature

$A_1$	Area of cylinder piston side	$[m^{2}]$
$A_2$	Area of cylinder rod side	$[m^2]$
$m{A}_{ m i}^{ m i-1}$	Homogeneous transformation matrix	[-]
$A_{ m h}$	Joint-to-actuator Jacobian matrix	[-]
$A_{ m h0}$	Joint-to-actuator Jacobian matrix at the linearization point	[-]
$A_{\rm hLT}$	Joint-to-actuator Jacobian matrix for LIFT and TILT joints	[-]
$A_{ m hCH}$	Joint-to-actuator Jacobian matrix for CRO and HRO	[-]

	joints	
$m{F}_{ m h}$	Vector of cylinder forces with	[-]
	friction force	
$F_{\rm L}$	External force	[N]
G	Vector of gravitational torque	[-]
$G_{ m LT}$	Vector of gravitational torque	[-]
_	for lift-tilt 2DOF system	
$G_{\rm CH}$	Vector of gravitational torque	[-]
	for CRO-HRO 2DOF system	
H	Valve hysteresis	[%]
J	Joint-to-Cartesian Jacobian	[-]
(1)	matrix	
$J_P^{(l_i)}$	Jacobian of link i	[-]
K	Position open loop gain	[1/s]
K	Stiffness matrix	[-]
$\mathbf{K}_0$	Stiffness matrix at the lineari-	[-]
17	zation point	F A 2/1 3
$K_a$	Acceleration feedback gain	[mA·s <sup>2</sup> /deg]
$K_{\rm hj}$	Spring constant of cylinder j	[N/m]
$K_{\rm pg}$	Pressure gain of the servo	[bar/mA]
V	valve	F1 / / A3
$K_{qa}$	Velocity gain in joint space	[deg/s/mA]
$K_{qa_{in}}$	Retracting velocity gain in	[deg/s/mA]
V	joint space	
$\kappa_{qa_{cyl}}$	Future dia a sucleasity agin in	[m/s/mA]
$\Lambda_{qa_{out}}$	Extending velocity gain in	[deg/s/mA]
VD	D controller coin	
	P-controller gain Desired position loop gain	[mA/deg]
KP	Desired position loop gain <b>B</b> controller gain in extension	[mA/deg]
М <sub>р</sub>	direction	[IIIA/deg]
KP	P_controller gain in retraction	[mA/dea]
m n	r-controller gain in retraction	[IIIA/ucg]
	direction	
М	direction Mass of the cassette	[ka]
M M	direction Mass of the cassette Inertia matrix	[kg] [-]
М М Мо	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza-	[kg] [-] [-]
$egin{array}{c} M \ oldsymbol{M} \ oldsymb$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point	[kg] [-] [-]
М М М <sub>0</sub>	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF	[kg] [-] [-]
$egin{array}{c} M \ M \ M \ M_0 \ M_{ m LT} \end{array}$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system	[kg] [-] [-]
$egin{array}{c} M & M & M & M & M & M & M & M & M & M $	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO	[kg] [-] [-] [-]
М М М <sub>0</sub> М <sub>LT</sub>	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system	[kg] [-] [-] [-]
М М М <sub>0</sub> М <sub>LT</sub> М <sub>CH</sub>	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i	[kg] [-] [-] [-] [-]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain	[kg] [-] [-] [-] [-] [mA·s/deg]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_S$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure	[kg] [-] [-] [-] [-] [mA·s/deg] [bar]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_S$ $Q_N$ $V$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_S$ $Q_N$ $V$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-]
$M$ $M_{0}$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_{d}$ $P_{S}$ $Q_{N}$ $V$ $a_{i}$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m]
$M$ $M_{\rm M}$ $M_{\rm 0}$ $M_{\rm LT}$ $M_{\rm CH}$ $P_{\rm Ci}$ $P_{\rm d}$ $p_{\rm S}$ $Q_{\rm N}$ $V$ $a_{\rm i}$ $d_{\rm i}$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m]
$M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_S$ $Q_N$ $V$ $a_i$ $d_i$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m]
$M$ $M_{0}$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_{d}$ $P_{S}$ $Q_{N}$ $V$ $a_{i}$ $d_{i}$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m]
$M$ $M_{\rm M}$ $M_{\rm 0}$ $M_{\rm LT}$ $M_{\rm CH}$ $P_{\rm Ci}$ $P_{\rm d}$ $p_{\rm S}$ $Q_{\rm N}$ $V$ $a_{\rm i}$ $d_{\rm i}$ $f$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m]
$M$ $M_{M_0}$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_{d}$ $P_{S}$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m]
$M$ $M_{M_0}$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_{d}$ $P_{S}$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [m] [-] [-]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [Hz] [-] [-]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [m] [-] [-] [-] [-]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [-] [-] [-] [-] [-] [-]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i	[kg] [-] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [m] [-] [-] [-] [-] [-] [kg]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$ $u$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i Valve input	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [m] [-] [-] [-] [-] [-] [kg] [mA]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$ $u$ $u_i$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i Valve input Valve input of cylinder i	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [-] [-] [-] [-] [-] [kg] [mA]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$ $u$ $u_i$ $u_{max}$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i Valve input Valve input	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [Hz] [-] [-] [-] [-] [-] [-] [kg] [mA]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$ $u$ $u_i$ $u_{max}$ $V$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i Valve input Valve input Velocity vector in Cartesian	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [-] [-] [-] [-] [-] [kg] [mA] [-]
$M$ $M$ $M_0$ $M_{LT}$ $M_{CH}$ $P_{Ci}$ $P_d$ $P_s$ $Q_N$ $V$ $a_i$ $d_i$ $f$ $g_0$ $h_1$ $h_2$ $m_h$ $u$ $u_i$ $u_{max}$ $V$	direction Mass of the cassette Inertia matrix Inertia matrix at the lineariza- tion point Inertia matrix for lift-tilt 2DOF system Inertia matrix for CRO-HRO 2DOF system Position vector of link i Speed feedforward gain Supply pressure Nominal flow rate Centrifugal and Coriolis terms matrix Length of link i Translational distance between two incident normals of a joint axis Natural frequency Gravity acceleration vector in the base frame Joint-to-Cartesian position transformation matrix Joint-to-actuator position transformation matrix Mass of link i Valve input Valve input Velocity vector in Cartesian coordinate	[kg] [-] [-] [-] [mA·s/deg] [bar] [m <sup>3</sup> /s] [-] [m] [m] [m] [m] [-] [-] [-] [-] [kg] [mA] [-]

	coordinate	
$z_{i}$	Link length of cylinder i	[m]
ż,	Velocity of cylinder i	[m/s]
z	Vector of cylinder length	[-]
ż	Vector of cylinder velocity	[-]
$\delta$	Effective damping ratio	[-]
$\delta_{\mathrm{n}}$	Damping ratio	[-]
$\Delta p_{ m N}$	Nominal pressure drop	[bar]
$\Delta y$	Position error	[deg]
$\alpha_{\rm i}$	Twist angle between two ad-	[rad]
	jacent joint axes,	
$\theta_{i}$	Angle of joint i	[rad]
$\dot{\theta}_{i}$	Angular velocity of joint i	[rad/s]
$\theta$	Vector of joint angle	[-]
$\dot{ heta}$	Vector of joint angular veloc-	[-]
	ity	
$\lambda_k\{\cdot\}$	<i>k</i> :th eigenvalue of square ma-	[-]
	trix	
$ au_{ m i}$	Time constant of phase lag P	[s]
	control	
τ	Vector of joint torque	[-]
$\omega_{ m BW}$	Desired bandwidth	[rad/s]
$\omega_{\rm n}$	Natural frequency	[rad/s]
$\omega_{ m k}$	k:th natural frequency	[rad/s]

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## Appendix

## Variable definitions

For the derivation of the kinematic and dynamic equations, the schematic diagram in Fig. 2 is used with variables defined as follows:

$L_1 = AD = 1.080 \text{ m}$	$m_3 = 371 \text{ kg}$
$L_2 = GJ = 0.376 \text{ m}$	$m_4 = 89  \mathrm{kg}$
$a_{22} = AF = 0.975 \text{ m}$	M = 9000  kg
$a_{23} = AE = 1.024$ m	$\varphi_1 = \angle BAF = 5.48^\circ$
$a_{33} = \underline{BC} = 1.134 \text{ m}$	$\varphi_2 = \angle ADz_0 - axis = 100^\circ$
$a_{44} = GK = 0.349 \text{ m}$	$\varphi_3 = \angle CBO_3 = 78.8^{\circ}$
$a_{45} = GL = 0.613 \text{ m}$	$\varphi_4 = \angle EAz_0 - axis = 21.2^\circ$

$$\begin{array}{ll} a_{55} = \overline{HI} = 0.386 \text{ m} & \varphi_5 = \angle MBO_3 = 10.5^{\circ} \\ r_2 = \underline{Bm_2} = 0.856 \text{ m} & \varphi_6 = \angle m_2BO_3 = 29.8^{\circ} \\ r_3 = \underline{Gm_3} = 0.216 \text{ m} & \varphi_7 = \angle LHI = 77.4^{\circ} \\ r_4 = \underline{Hm_4} = 0.154 \text{ m} & \varphi_8 = \angle JGH = 74.3^{\circ} \\ R_1 = \underline{BM} = 2.662 \text{ m} & \varphi_9 = \angle m_3GH = 12.2^{\circ} \\ R_2 = HM = 1.082 \text{ m} & \varphi_{10} = \angle m_4HN = 47.4^{\circ} \\ m_1 = 306 \text{ kg} & \varphi_{11} = \angle m_4HM = 0^{\circ} \\ m_2 = 1250 \text{ kg} & \varphi_{13} = \angle KGy_0 - axis = 13.2^{\circ} \\ z_2 = \underline{EF} = \text{lift cylinder length} \\ z_3 = \underline{DC} = \text{tilt cylinder length} \\ z_4 = \underline{KL} = \text{CRO cylinder length} \\ z_5 = \overline{JI} = \text{HRO cylinder length} \end{array}$$

## Kinematics of the Lift-tilt 2DOF System

The joint-to-actuator transformation and corresponding differential kinematic equations are derived as

$$z_{2} = \sqrt{a_{22}^{2} + a_{23}^{2} - 2a_{22}a_{23}\cos(\theta_{2} - \varphi_{1} + \varphi_{4})}$$

$$z_{3} = \sqrt{L_{1}^{2} + 2L_{1}a_{33}\cos(\varphi_{2} - \theta_{2} - \theta_{3} + \varphi_{3}) + a_{2}^{2} + a_{33}^{2}} + 2a_{2}a_{33}\cos(\varphi_{3} - \theta_{3}) + 2L_{1}a_{2}\cos(\varphi_{2} - \theta_{2})}$$
(20)

$$\begin{bmatrix} \dot{z}_2\\ \dot{z}_3 \end{bmatrix} = \begin{bmatrix} A_{hLT11} & 0\\ A_{hLT21} & A_{hLT22} \end{bmatrix} \begin{bmatrix} \dot{\theta}_2\\ \dot{\theta}_3 \end{bmatrix}$$
(21)

where

$$A_{hLT11} = (a_{22}a_{23}\sin(\theta_2 - \varphi_1 + \varphi_4))/z_2$$

$$A_{hLT12} = 0$$

$$A_{hLT21} = (L_1a_2\sin(\varphi_2 - \theta_2) + L_1a_{33}\sin(\varphi_2 - \theta_2) - \theta_3 + \varphi_3)/z_3$$

$$A_{hLT22} = (L_1a_{33}\sin(\varphi_2 - \theta_2 - \theta_3 + \varphi_3) + a_2a_{33}\sin(\varphi_3 - \theta_3))/z_3$$
(22)

### Kinematics of the CRO-HRO 2DOF System

The joint-to-actuator transformation and corresponding differential kinematic equations are expressed as

$$z_{4} = \sqrt{\frac{a_{44}^{2} + a_{45}^{2} - 2a_{44}a_{45}\cos(\pi/2 - \varphi_{8} + \theta_{4})}{+\varphi_{12} + \varphi_{13}}}$$

$$z_{5} = \sqrt{\frac{L_{2}^{2} - 2L_{2}a_{4}\cos(\varphi_{8}) + a_{4}^{2} + a_{5}^{2} + 2a_{4}a_{5}}{\cos(\varphi_{7} - \theta_{5}) - 2L_{2}a_{5}\cos(\varphi_{8} - \varphi_{7} + \theta_{5})}}$$
(23)

$$\begin{bmatrix} \dot{z}_4 \\ \dot{z}_5 \end{bmatrix} = \begin{bmatrix} A_{\text{hCH11}} & 0 \\ 0 & A_{\text{hCH22}} \end{bmatrix} \begin{bmatrix} \dot{\theta}_4 \\ \dot{\theta}_5 \end{bmatrix}$$
(24)

where

$$A_{\text{hCH11}} = (a_{44}a_{45}\sin(\pi/2 - \varphi_8 + \theta_4 + \varphi_{12} + \varphi_{13}))/z_4$$
  

$$A_{\text{hCH22}} = (L_2a_5\sin(\pi - \varphi_8 - \theta_5 + \varphi_7) + a_4a_5\sin(\varphi_7 \qquad (25))/z_5$$

### Dynamics of the Lift-tilt 2DOF System

For the lift-tilt 2DOF system, the terms of the dynamic equation are derived at 0 rotation of the cassette, which is regarded as the worst case scenario of the vibration modes analysis. The inertia matrix and gravitational torque vector are derived based on Eq. 8 and 9

$$\boldsymbol{M}_{\rm LT} = \begin{bmatrix} \boldsymbol{M}_{\rm LT11} & \boldsymbol{M}_{\rm LT12} \\ \boldsymbol{M}_{\rm LT21} & \boldsymbol{M}_{\rm LT22} \end{bmatrix}$$
(26)

$$M_{LT11} = m_{1}r_{1}^{2} + m_{2}(a_{2}^{2} + 2a_{2}r_{2} \cos(\theta_{3} - \varphi_{6}) + r_{2}^{2}) + M(a_{2}^{2} + 2a_{2}R_{1} \cos(\theta_{3} + \varphi_{5}) + R_{1}^{2})$$

$$M_{LT12} = m_{2}(a_{2}r_{2} \cos(\theta_{3} - \varphi_{6}) + r_{2}^{2}) + M(a_{2} R_{1} \cos(\theta_{3} + \varphi_{5}) + R_{1}^{2})$$

$$M_{LT21} = M_{LT12}$$

$$M_{LT22} = m_{2}r_{2}^{2} + MR_{1}^{2}$$
(27)

$$\boldsymbol{G}_{\text{LT}} = \begin{bmatrix} \boldsymbol{G}_{\text{LT}} & \boldsymbol{G}_{\text{LT}} \end{bmatrix}^{\text{T}}$$
(28)

$$G_{LT1} = m_{1}gr_{1}\sin(\theta_{2}) + m_{2}g(a_{2}\cos(\theta_{2}) + r_{2})$$

$$\cos(\theta_{2} + \theta_{3} - \varphi_{6}) + Mg(a_{2}\cos(\theta_{2}) + R_{1})$$

$$\cos(\theta_{2} + \theta_{3} + \varphi_{5}))$$

$$G_{LT2} = m_{2}r_{2}g\cos(\theta_{2} + \theta_{3} - \varphi_{6}) + MR_{1}g$$

$$\cos(\theta_{2} + \theta_{3} + \varphi_{5})$$
(29)

### **Dynamics of the CRO-HRO 2DOF System**

Similarly, the inertia matrix and gravitational torque vector for CRO-HRO 2DOF system are derived as follows.

$$\boldsymbol{M}_{\rm CH} = \begin{bmatrix} M_{\rm CH11} & M_{\rm CH12} \\ M_{\rm CH21} & M_{\rm CH22} \end{bmatrix}$$
(30)

$$M_{CH11} = m_{3}r_{3}^{2} + m_{4}(a_{4}^{2} + 2a_{4}r_{4}\cos(\theta_{5} - \varphi_{10}) + r_{4}^{2}) + M(a_{4}^{2} + 2a_{4}R_{2}\cos(\theta_{5} - \varphi_{11}) + R_{2}^{2})$$

$$M_{CH12} = m_{4}(a_{4}r_{4}\cos(\theta_{5} - \varphi_{10}) + r_{4}^{2}) + M$$

$$(a_{4}R_{2}\cos(\theta_{5} - \varphi_{11}) + R_{2}^{2})$$

$$M_{CH21} = M_{CH12}$$

$$M_{CH22} = m_{4}r_{4}^{2} + MR_{2}^{2}$$
(31)

$$\boldsymbol{G}_{\rm CH} = \begin{bmatrix} 0 & 0 \end{bmatrix}^{\rm I} \tag{32}$$



#### Likui Zhai

Born in Xintai, China, 1981, he received his BS and MS in mechanical engineering from Nanjing University of Sci & Tech (China) in 2004 and Zhejiang University (China) in 2006 respectively. He is now a postgraduate student in Tampere University of Technology (Finland). His main research fields are modelling and control of electrohydraulic servo system.

### Tapio Virvalo



He received his MS in mechanical engineering from Helsinki University of Technology, Finland in 1967, and PhD degree from Tampere University of Technology, Finland in 1995. He is presently as the professor of machine automation in Department of Intelligent Hydraulics and Automation (IHA) at Tampere University of Technology. His current research interests are motion control, especially, in fluid power applications including pneumatics and water hydraulics. His long term interests have also been in mechatronics and control engineering.

### Jouni Mattila



He received his PhD degree (2000) in mechanical engineering from Tampere University of Technology. At present he is a senior researcher and project manager of FU-SION/DTP2 in Department of Intelligent Hydraulics and Automation (IHA) at Tampere University of Technology. His research interests have been in robotics and control engineering.



#### Hannu Saarinen

Born in Finland, 1967. He received his MS (1993) in mechanical engineering from Tampere University of Technology. Currently he is a senior research scientist working at the ROVIR team of VTT, where he is coordinating the tasks for designing and developing CMM control software. His scientific interests include robotics, virtual reality and real-time control systems.