

ANALYSIS OF A COMPUTER SYSTEM WITH HARDWARE REPAIR AND SOFTWARE REPLACEMENT SUBJECT TO CONDITIONAL ARRIVAL TIME OF THE SERVER

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Abstract

The focus of this paper is on reliability and profit analysis of a computer system of two identical units- one is initially operative and other is kept as spare in cold standby. In each unit, hardware (h/w) and software (s/w) fail independently from normal mode. There is a single server who is allowed to take some time at s/w failure with the condition that he has to visit the system immediately at h/w failure. The unit is repaired at h/w failure while replacement of the s/w by new one is done by giving some replacement time when s/w fails to execute the required instructions properly. Server can leave the system only after finishing all jobs available to him. All random variables are statistically independent. The time to failure of h/w and s/w is exponentially distributed while the arrival time of the server, repair time of h/w and replacement time of s/w are arbitrarily distributed with different probability density functions (pdf). By adopting semi-Markov process and regenerative point technique, the expressions for various reliability characteristics are derived to make profit analysis. The behaviour of some important measures of system effectiveness has also been shown graphically for a particular case.

Key Words: Computer System, H/w Repair, S/w Replacement, Conditional Arrival Time of the Server, Reliability and Profit Analysis.

1. Introduction

In the modern society, it is hard to imagine any area in which computer systems do not play a dominant role. Computers are being used frequently in most of the critical areas such as aerospace, nuclear power generation and defence. For such applications their reliability is the utmost importance because a computer failure in these areas could be very costly and dangerous to the society. Other factors such as increasing repair costs, harsher operating environments and the existence of bigger systems are also responsible for the increasing emphasis on reliability of computer systems. However, in computers the reliability problem is not only confined to the h/w but also extends to s/w. Both h/w and s/w have to be reliable for successful operation of a computer. Therefore, there is a definite need to place emphasis on the reliability of both the h/w and s/w components. The method of redundancy is one of the best techniques to improve the reliability of any operating systems. Therefore, in recent years, reliability models of two-unit cold standby computer systems having independent h/w and s/w failures have been suggested by some researchers including Malik and Anand [2010] and Malik and Kumar [2011]. Also, Malik and Sureria [2012] analyzed a

cold standby computer system with h/w repair and s/w replacement by a server who visits the system immediately whenever needed. But, sometimes, it becomes complicated for a server to attend the system promptly when needed may because of his pre-occupations. And, in such a situation, the server may take some time to arrive at the system (called arrival time of the server) with the condition that he has to attend immediately the serious technical hitches occurred in the system.

The motive of the present study is to make reliability and profit analysis of a computer system by taking two identical units of it- one is initially operative and the other is kept as spare in cold standby. The computer is considered as a single unit in which h/w and s/w work together and may have independent failure from normal mode. There is a single server who is allowed to take some time at s/w failure with the condition that he has to visit the system immediately at h/w failure. The repair of the unit is done at h/w failure while s/w is replaced by new one by giving some replacement time when it fails to execute the required instructions properly. Server can leave the system only after finishing all the jobs available to him. The random variables are statistically independent. The distribution of failure time of h/w and s/w is taken as negative exponential whereas h/w repair time, s/w replacement time and arrival time of the server are arbitrarily distributed. To meet out the objectives, the expressions for various reliability measures such as mean sojourn times, mean time to system failure (MTSF), availability, busy period of the server due to hardware and software failures, expected number of replacements of the software, expected number of visits by the server and profit are derived using semi-Markov process and regenerative point technique. The graphical study of the results has also been made for a particular case.

2. Notations

| | | |
|--|---|--|
| E | : | The set of regenerative states |
| O | : | The unit is operative and in normal mode |
| Cs | : | The unit is cold standby |
| a/b | : | Probability that the system has hardware / software failure |
| λ_1/λ_2 | : | Constant hardware / software failure rate |
| FHUr/FHUR | : | The unit is failed due to hardware and is under repair / under repair continuously from previous state |
| FHW _r / FHWR | : | The unit is failed due to hardware and is waiting for repair/ waiting for repair continuously from previous state |
| FSUR _p /FSURP | : | The unit is failed due to the software and is under replacement/ |
| FSWR _p /FSWRP | : | under replacement continuously from previous state The unit is failed due to the software and is waiting for replacement / waiting for replacement continuously from previous state |
| w(t) / W(t) | : | pdf / cdf of arrival time of server due to s/w failure |
| f(t) / F(t) | : | pdf / cdf of replacement time of the software |
| g(t) / G(t) | : | pdf / cdf of repair time of the unit due to hardware failure |
| q _{ij} (t)/ Q _{ij} (t) | : | pdf / cdf of passage time from regenerative state i to a regenerative state j or to a failed state j without visiting any other regenerative state in (0, t] |

- $q_{ij,kr}(t)/Q_{ij,kr}(t)$: pdf/cdf of direct transition time from regenerative state i to a regenerative state j or to a failed state j visiting state k, r once in $(0, t]$
- m_{ij} : Contribution to mean sojourn time (μ_i) in state S_i when system transits directly to state S_j so that $\mu_i = \sum_j m_{ij}$ and $m_{ij} = \int t dQ_{ij}(t) = -q_{ij}^*(0)$
- \otimes / \odot : Symbol for Laplace-Stieltjes convolution/Laplace convolution
- $\sim / *$: Symbol for Laplace Steiltjes Transform (LST) / Laplace Transform (LT)

The following are the possible transition states of the system:

- $S_0 = (O, Cs), S_1 = (O, FHUr), S_2 = (O, FSWRp), S_3 = (O, FSURp),$
 $S_4 = (FHWr, FSURP), S_5 = (FSWRP, FSWRp), S_6 = (FHUr, FSWRp),$
 $S_7 = (FHUR, FSWRp), S_8 = (FHUR, FHWr), S_9 = (FSURp, FSWRp),$
 $S_{10} = (FSURP, FSWRp)$

The state S_0-S_3 is regenerative states while the states S_4-S_{10} are non-regenerative as shown in figure 1.

3. Transition Probabilities and Mean Sojourn Times

Simple probabilistic considerations yield the following expressions for the non-zero elements

$$\begin{aligned}
 p_{ij} &= Q_{ij}(\infty) = \int_0^\infty q_{ij}(t) dt \text{ as} \\
 p_{01} &= \frac{a\lambda_1}{a\lambda_1 + b\lambda_2}, & p_{02} &= \frac{b\lambda_2}{a\lambda_1 + b\lambda_2}, \\
 p_{10} &= g^*(a\lambda_1 + b\lambda_2), & p_{17} &= \frac{b\lambda_2}{a\lambda_1 + b\lambda_2} [1 - g^*(a\lambda_1 + b\lambda_2)], \\
 p_{18} &= \frac{a\lambda_1}{a\lambda_1 + b\lambda_2} [1 - g^*(a\lambda_1 + b\lambda_2)], & p_{23} &= w^*(a\lambda_1 + b\lambda_2), \\
 p_{25} &= \frac{b\lambda_2}{a\lambda_1 + b\lambda_2} [1 - w^*(a\lambda_1 + b\lambda_2)], & p_{26} &= \frac{a\lambda_1}{a\lambda_1 + b\lambda_2} [1 - w^*(a\lambda_1 + b\lambda_2)], \\
 p_{30} &= f^*(a\lambda_1 + b\lambda_2), & p_{34} &= \frac{a\lambda_1}{a\lambda_1 + b\lambda_2} [1 - f^*(a\lambda_1 + b\lambda_2)], \\
 p_{3,10} &= \frac{b\lambda_2}{a\lambda_1 + b\lambda_2} [1 - f^*(a\lambda_1 + b\lambda_2)] \tag{1}
 \end{aligned}$$

For $f(t) = \theta e^{-\theta t}, g(t) = \alpha e^{-\alpha t}$ and $w(t) = \beta e^{-\beta t}$ we have

$$p_{13.7} = \frac{b\lambda_2}{a\lambda_1 + b\lambda_2 + \alpha}, \quad p_{11.8} = \frac{a\lambda_1}{a\lambda_1 + b\lambda_2 + \alpha}, \quad p_{23.59} = \frac{b\lambda_2}{a\lambda_1 + b\lambda_2 + \beta},$$

$$p_{23,6} = \frac{a\lambda_1}{a\lambda_1 + b\lambda_2 + \beta}, p_{31,4} = \frac{a\lambda_1}{a\lambda_1 + b\lambda_2 + \theta}, p_{33,10} = \frac{b\lambda_2}{a\lambda_1 + b\lambda_2 + \theta} \quad (2)$$

It can be easily verified that

$$\begin{aligned} p_{01} + p_{02} &= p_{10} + p_{17} + p_{18} = p_{23} + p_{25} + p_{26} = p_{30} + p_{34} + p_{3,10} = \\ p_{10} + p_{11,8} + p_{13,7} &= p_{23} + p_{23,59} + p_{23,6} = p_{30} + p_{31,4} + p_{33,10} = 1 \end{aligned} \quad (3)$$

The mean sojourn times (μ_i) in the state S_i are

$$\mu_0 = \frac{1}{a\lambda_1 + b\lambda_2}, \mu_1 = \frac{1}{a\lambda_1 + b\lambda_2 + \alpha}, \mu_2 = \frac{1}{a\lambda_1 + b\lambda_2 + \beta}, \mu_3 = \frac{1}{a\lambda_1 + b\lambda_2 + \theta} \quad (4)$$

also

$$\begin{aligned} m_{01} + m_{02} &= \mu_0, m_{10} + m_{17} + m_{18} = \mu_1, m_{23} + m_{25} + m_{26} = \mu_2, \\ m_{30} + m_{34} + m_{3,10} &= \mu_3 \end{aligned} \quad (5)$$

and

$$\begin{aligned} m_{10} + m_{11,8} + m_{13,7} &= \mu'_1, m_{20} + m_{23,6} + m_{23,56} = \mu'_2, \\ m_{30} + m_{31,4} + m_{33,10} &= \mu'_3 \text{ (say)} \end{aligned} \quad (6)$$

For $f(t) = \theta e^{-\theta t}$, $g(t) = \alpha e^{-\alpha t}$ and $w(t) = \beta e^{-\beta t}$

$$\text{we have } \mu_1^1 = \frac{1}{\alpha}, \mu_2^1 = \frac{(\alpha + a\lambda_1)\theta\beta + b\lambda_2\alpha(\beta + \theta)}{\alpha\theta\beta(a\lambda_1 + b\lambda_2 + \beta)}, \mu_3^1 = \frac{1}{\theta} \quad (7)$$

4. Reliability and Mean Time to System Failure (MTSF)

Let $\phi_i(t)$ be the c.d.f. of first passage time from regenerative state i to a failed state. Regarding the failed state as absorbing state, we have the following recursive relations for $\phi_i(t)$:

$$\phi_i(t) = \sum_j Q_{i,j}(t) \phi_j(t) + \sum_k Q_{i,k}(t) \quad (8)$$

where j is an un-failed regenerative state to which the given regenerative state i can transit and k is a failed state to which the state i can transit directly. Taking LST of above relation (8) and solving for $\tilde{\phi}_0(s)$

We have

$$R^*(s) = \frac{1 - \tilde{\phi}_0(s)}{s} \quad (9)$$

The reliability of the system model can be obtained by taking Laplace inverse transform of (9). The mean time to system failure (MTSF) is given by

$$\text{MTSF} = \lim_{s \rightarrow 0} \frac{1 - \tilde{\phi}_0(s)}{s} = \frac{N_1}{D_1}, \text{ where} \quad (10)$$

$$N_1 = \mu_0 + p_{01}\mu_1 + p_{02}\mu_2 + p_{02}p_{23}\mu_3 \text{ and } D_1 = 1 - p_{01}p_{10} - p_{02}p_{23}p_{30}$$

5. Steady State Availability

Let $A_i(t)$ be the probability that the system is in up-state at instant 't' given that the system entered regenerative state i at $t = 0$. The recursive relations for $A_i(t)$ are given as

$$A_i(t) = M_i(t) + \sum_j q_{i,j}^{(n)}(t) \odot A_j(t) \quad (11)$$

where j is any successive regenerative state to which the regenerative state i can transit through n transitions and $M_i(t)$ is the probability that the system is up initially in state $S_i \in E$ is up at time t without visiting to any other regenerative state, we have

$$\begin{aligned} M_0(t) &= e^{-(a\lambda_1+b\lambda_2)t}, M_1(t) = e^{-(a\lambda_1+b\lambda_2)t} \bar{G}(t), M_2(t) = e^{-(a\lambda_1+b\lambda_2)t} \bar{W}(t), \\ M_3(t) &= e^{-(a\lambda_1+b\lambda_2)t} \bar{F}(t) \end{aligned} \quad (12)$$

Taking LT of above relations (11) and solving for $A_0^*(s)$, the steady state availability is given by

$$A_0(\infty) = \lim_{s \rightarrow 0} s A_0^*(s) = \frac{N_2}{D_2}, \text{ where} \quad (13)$$

$$\begin{aligned} N_2 &= [p_{30}(1-p_{11.8}) + p_{10} p_{31.4}] \mu_0 + [p_{31.4} + p_{01} p_{30}] \mu_1 + p_{02} [p_{30}(1-p_{11.8}) + p_{10} p_{31.4}] \mu_2 \\ &\quad + [p_{31.7} + p_{02} p_{10}] \mu_3 \\ D_2 &= [p_{30}(1-p_{11.8}) + p_{10} p_{31.4}] \mu_0 + [p_{31.4} + p_{01} p_{30}] \mu_1' + p_{02} [p_{30}(1-p_{11.8}) + p_{10} p_{31.4}] \mu_2' \\ &\quad + [p_{31.7} + p_{02} p_{10}] \mu_3' \end{aligned}$$

6. Busy Period Analysis for Server

(a) Due to Hardware Repair

Let $B_i^H(t)$ be the probability that the server is busy in repairing the unit due to hardware failure at an instant 't' given that the system entered state i at $t = 0$. The recursive relations $B_i^H(t)$ for are as follows:

$$B_i^H(t) = W_i^H(t) + \sum_j q_{i,j}^{(n)}(t) \odot B_j^H(t) \quad (14)$$

where j is any successive regenerative state to which the regenerative state i can transit through n transitions and $W_i^H(t)$ be the probability that the server is busy in state S_i due to hardware failure up to time t without making any transition to any other regenerative state or returning to the same via one or more non-regenerative states and so

$$W_i^H(t) = e^{-(a\lambda_1+b\lambda_2)t} \bar{G}(t) + [a\lambda_1 e^{-(a\lambda_1+b\lambda_2)t} \odot 1] \bar{G}(t) + [b\lambda_2 e^{-(a\lambda_1+b\lambda_2)t} \odot 1] \bar{G}(t) \quad (15)$$

(b) Due to Replacement of the Software

Let $B_i^S(t)$ be the probability that the server is busy due to replacement of the software at an instant 't' given that the system entered the regenerative state i at $t = 0$. We have the following recursive relations for $B_i^S(t)$:

$$B_i^S(t) = W_i^S(t) + \sum_j q_{i,j}^{(n)}(t) \odot B_j^S(t) \quad (16)$$

where j is any successive regenerative state to which the regenerative state i can transit through n transitions and $W_i^S(t)$ be the probability that the server is busy in state S_i due to replacement of the software up to time t without making any transition to any other regenerative state or returning to the same via one or more non-regenerative states and so

$$W_3^S(t) = e^{-(a\lambda_1 + b\lambda_2)t} \overline{F}(t) + (a\lambda_1 e^{-(a\lambda_1 + b\lambda_2)t} \odot 1) \overline{F}(t) + (b\lambda_2 e^{-(a\lambda_1 + b\lambda_2)t} \odot 1) \overline{F}(t) \quad (17)$$

Taking LT of above relations (14) and (16) and solving for $B_0^{*H}(s)$ and $B_0^{*S}(s)$, the time for which server is busy due to repair and replacements respectively is given by

$$B_0^H = \lim_{s \rightarrow 0} s B_0^{*H}(s) = \frac{N_3^H}{D_2} \quad (18)$$

$$B_0^S = \lim_{s \rightarrow 0} s B_0^{*S}(s) = \frac{N_3^S}{D_2}, \text{ where} \quad (19)$$

$N_3^H = [p_{01}(1 - p_{33.10}) + p_{02}p_{31.4}] \tilde{W}_1^H(0)$, $N_3^S = [p_{01}p_{31.4} + p_{02}p_{11.8}] \tilde{W}_3^S(0)$ and D_2 is already mentioned.

7. Expected Number of Replacements of the Software

Let $R_i^S(t)$ be the expected number of replacements of the failed software by the server in $(0, t]$ given that the system entered the regenerative state i at $t = 0$. The recursive relations for $R_i^S(t)$ are given as

$$R_i^S(t) = \sum_j Q_{i,j}^{(n)}(t)(S) [\delta_j + R_j^S(t)] \quad (20)$$

Where j is any regenerative state to which the given regenerative state i transits and $\delta_j = 1$, if j is the regenerative state where the server does job afresh, otherwise $\delta_j = 0$.

Taking LST of relations (20) and solving for $\tilde{R}_0^S(s)$. The expected number of replacements per unit time to the software failures is given by

$$R_0(\infty) = \lim_{s \rightarrow 0} s \tilde{R}_0^S(s) = \frac{N_4}{D_2}, \text{ where} \quad (21)$$

$N_4 = p_{01}p_{13.7} + p_{02}p_{11.8}$ and D_2 is already mentioned.

8. Expected Number of Visits by the Server

Let $N_i(t)$ be the expected number of visits by the server in $(0, t]$ given that the system entered the regenerative state i at $t = 0$. The recursive relations for $N_i(t)$ are given as

$$N_i(t) = \sum_j Q_{i,j}^{(n)}(t)(S) [\delta_j + N_j(t)] \quad (22)$$

where j is any regenerative state to which the given regenerative state i transits and $\delta_j = 1$, if j is the regenerative state where the server does job afresh, otherwise $\delta_j = 0$.

Taking LST of relation (22) and solving for $\tilde{N}_0(s)$. The expected numbers of visits per unit time by the server are given by

$$N_0(\infty) = \lim_{s \rightarrow 0} s \tilde{N}_0(s) = \frac{N_5}{D_2}, \text{ where} \quad (23)$$

$N_5 = (1 - p_{11.8})(1 - p_{33.10}) - p_{13.7} p_{3,10}$ and D_2 is already specified.

9. Profit Analysis

The profit incurred to the system model in steady state can be obtained as

$$P = K_0 A_0 - K_1 B_0^H - K_2 B_0^S - K_3 R_0 - K_4 N_0 \quad (24)$$

where

K_0 = Revenue per unit up-time of the system

K_1 = Cost per unit time for which server is busy due to hardware repair

K_2 = Cost per unit time for which server is busy due to software replacement

K_3 = Cost per unit replacement of the failed software

K_4 = Cost per unit visit by the server and $A_0, B_0^H, B_0^S, R_0, N_0$ are already defined.

10. Particular Case

Suppose $g(t) = \alpha e^{-\alpha t}$, $f(t) = \theta e^{-\theta t}$ and $w(t) = \beta e^{-\beta t}$

We can obtain the following results

$$N_1 = \frac{(a\lambda_1 + b\lambda_2 + \beta)(a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \alpha) + a\lambda_1(a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \beta) + b\lambda_2(a\lambda_1 + b\lambda_2 + \alpha)(a\lambda_1 + b\lambda_2 + \theta) + b\lambda_2\beta(a\lambda_1 + b\lambda_2 + \beta)}{R_1}$$

$$R_1 = (a\lambda_1 + b\lambda_2)(a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \alpha)(a\lambda_1 + b\lambda_2 + \beta)$$

$$D_1 = \frac{R_1 - \theta\beta b\lambda_2(a\lambda_1 + b\lambda_2 + \alpha) - a\lambda_1\alpha(a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \beta)}{R_1}$$

$$D_2 = \frac{\theta\alpha\beta(a\lambda_1 + b\lambda_2 + \beta)[(\alpha + b\lambda_2)\theta + a\lambda_1\alpha] + (a\lambda_1 + b\lambda_2 + \alpha)(a\lambda_1 + b\lambda_2 + \beta)(a\lambda_1 + b\lambda_2 + \theta)\beta[\alpha b\lambda_2 + \theta] + b\lambda_2[\theta(\alpha + b\lambda_2) + \alpha a\lambda_1][\beta\theta(\alpha + a\lambda_1) + b\lambda_2\alpha(\beta + \theta)]}{\alpha\beta\theta R_1}$$

$$N_2 = \frac{(a\lambda_1 + 2b\lambda_2 + \beta)[(\alpha + b\lambda_2)\theta + a\lambda_1\alpha] + b\lambda_2(a\lambda_1 + b\lambda_2 + \alpha)(a\lambda_1 + b\lambda_2 + \beta) + a\lambda_1(a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \beta)}{R_1}$$

$$N_3^H = [a\lambda_1(\theta + \beta + a\lambda_1) + a\lambda_1 b\lambda_2] / \alpha(a\lambda_1 + b\lambda_2)(\theta + a\lambda_1 + b\lambda_2)$$

$$N_3^S = 2a\lambda_1 b\lambda_2 / \theta(a\lambda_1 + b\lambda_2)(\alpha + a\lambda_1 + b\lambda_2),$$

$$N_4 = 2a\lambda_1 b\lambda_2 / (a\lambda_1 + b\lambda_2)(\alpha + a\lambda_1 + b\lambda_2)$$

$$N_5 = [(\alpha + b\lambda_2)(\theta + a\lambda_1) - a\lambda_1 b\lambda_2] / (a\lambda_1 + b\lambda_2 + \theta)(a\lambda_1 + b\lambda_2 + \alpha)$$

11. State Transition Diagram

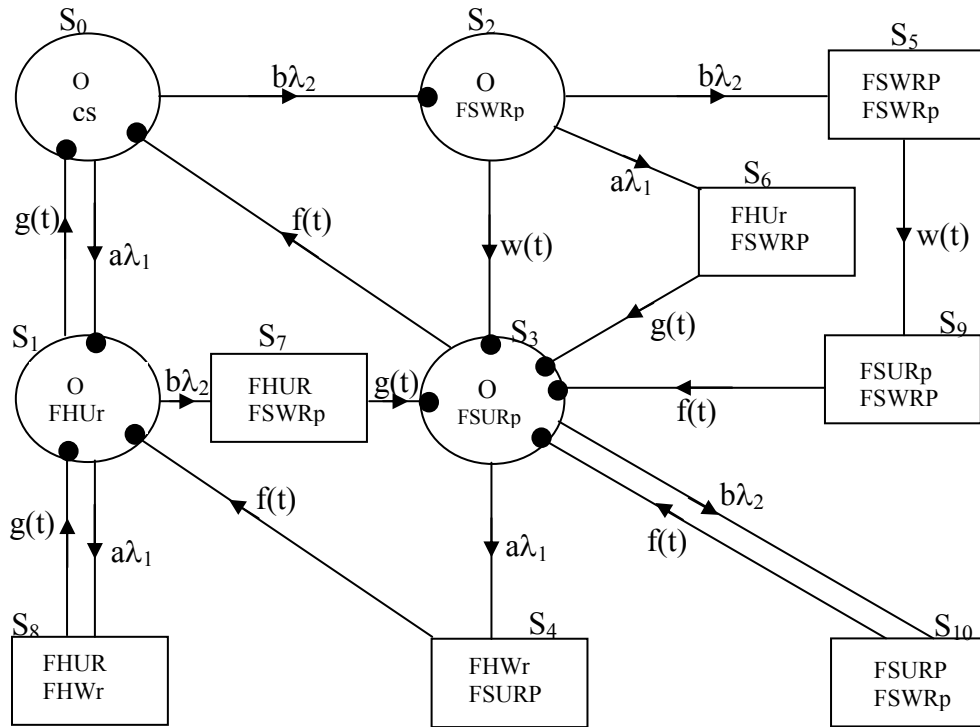


Fig. 1

○ Up-state □ Failed state ● Regenerative point

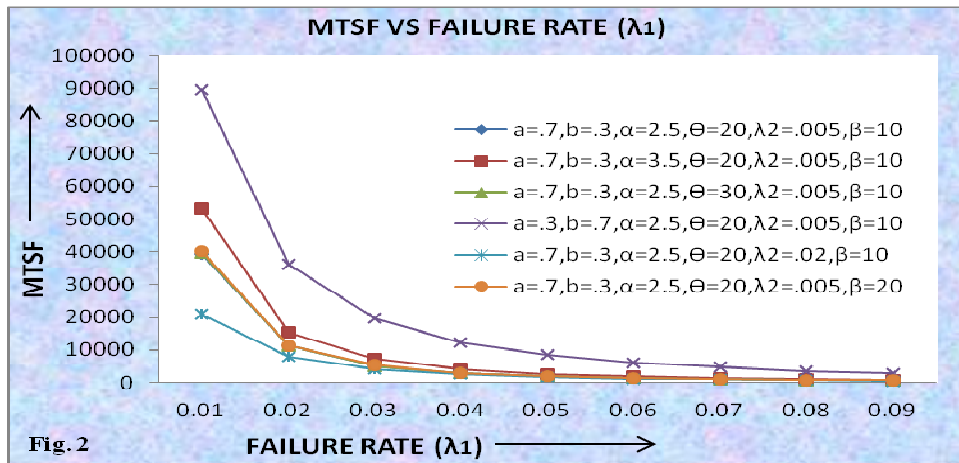
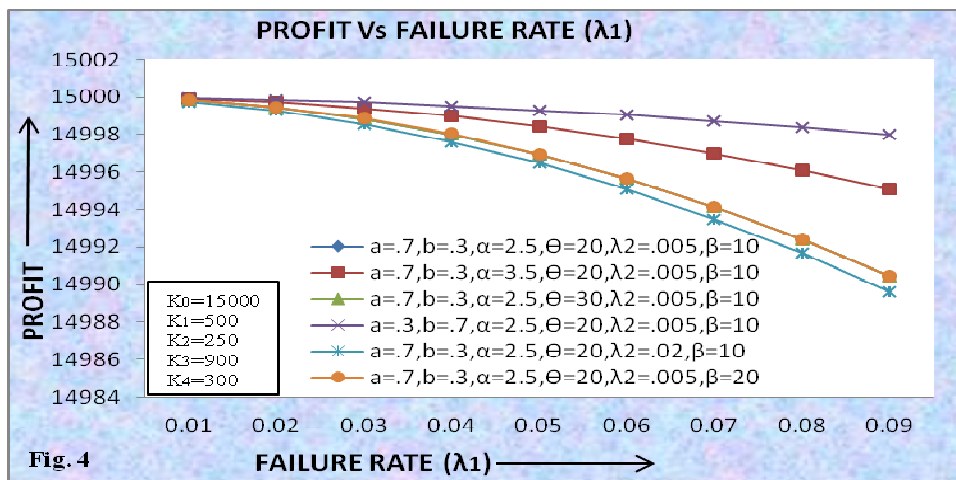
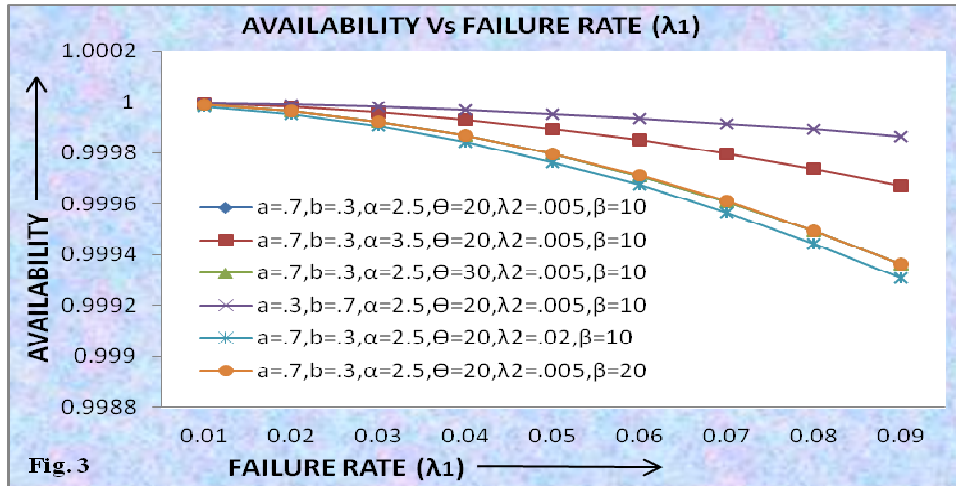


Fig. 2



11. Conclusion

From the Figures 2, 3 and 4, we found that MTSF, availability and profit of the system model go on decreasing with the increase of h/w and s/w failure rates (λ_1 and λ_2) for fixed values of other parameters including $a=.7$ and $b=.3$. However, their values increase with the increase of h/w repair rate (α), s/w replacement rate (θ) and arrival rate of the server (β). Further, the values of their parameters increase by interchanging the values of a and b i.e., $a=.3, b=.7$.

Thus, for a particular case, it is concluded that profit of a computer system in which chances of h/w failure are higher can be improved up to a considerable level by increasing the arrival rate of the server at s/w failure.

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